Strengths and Weaknesses of Quantitative Climate Reconstructions Based on Late-Quaternary Biological Proxies

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Abstract: The importance of reconstructing past environments quantitatively in palaeoecology is reviewed by showing that many ecological questions asked of palaeoecological data commonly involve the reconstructions of past environment. Three basic approaches to reconstructing past climate from palaeoecological data are outlined and discussed in terms of their assumptions, strengths, and weaknesses. These approaches are the indicator-species approach involving bioclimate-envelope modelling; the assemblage approach involving modern analogue techniques and response surfaces; and the multivariate calibration-function approach. Topics common to all approaches are reviewed – presentation and interpretation, evaluation and validation, comparison, and general limitations of climate reconstructions. Challenges and possible future developments are presented and the potential future role of quantitative climate reconstructions in palaeoecology is summarised.

Keywords: Bayesian approaches, bioclimate-envelope modelling, climate, climate reconstruction, indicator species, modern analogue technique, mutual climate range methods, niche, palaeoecology, reconstruction evaluation, reconstruction presentation, reconstruction validation, response surfaces, spatial autocorrelation, weighted averaging, weighted averaging partial least squares.

INTRODUCTION

Palaeoecology is the ecology of the past (Birks & Birks 1980) or as Rull (2010) proposes, it is “the branch of ecology that studies past ecological systems and their trends in time using fossils and other proxies”. Studies of ecological systems, past, present, or future, require consideration not only of their biotic components (e.g. species, populations, communities, biotic interactions, human activities) but also their abiotic components (e.g. climate, soil, topography, water chemistry, water temperature). If aspects of the abiotic component in a past ecosystem can be studied directly or reconstructed indirectly, these variables can be regarded as a set of predictors or forcing functions within the past ecological system under study. The biotic components of the system can thus be viewed as response variables. Important ecological processes and properties such as ecosystem variability, rates and nature of biotic response to environmental change, base-line conditions, thresholds, resilience, and ecosystem novelty can then be deduced from the palaeoecological record (Willis et al. 2010a). These are all important topics in current biodiversity conservation research with its increasing focus on the need for the conservation of ecological and evolutionary processes in the face of global climate and related changes (Klein et al. 2009). Care must, of course, be taken to avoid circularity of argument where the abiotic aspects of a past ecological system are reconstructed from a set of biological variables, and the resulting reconstructions are then used to ‘explain’ the observed changes in the biological proxies used in the reconstructions. All reconstructions of the past environment must be independent of any response variables being used to study biotic responses to environmental change (Flessa & Jackson 2005a).

The development of quantitative techniques for inferring past environments from palaeoecological data (e.g. Birks 1995) and of multi-proxy studies in palaeoecology (Birks & Birks 2006) allows direct studies of biotic responses to
environmental change over a range of time scales in the past (Flessa & Jackson 2005a, 2005b). In multi-proxy studies, several palaeoecological variables are studied and one or a few are used as predictor variables to reconstruct major aspects of the past environment (e.g. climate, lake-water pH, catchment vegetation) and the other variables are analysed as response variables. This multi-proxy approach can allow the direct study of biotic responses to climate change in the past (e.g. Birks & Birks 2008) and the testing of hypotheses about, for example, the relative roles of climate and catchment variables in influencing within-lake biotic and abiotic records (e.g. Lotter & Birks 2003).

Palaeoecological records abound with examples of biotic responses to past environmental changes, but this wealth of information has rarely been exploited to answer ecological questions. Recent advances in palaeoecology (quantitative environmental reconstruction procedures; multi-proxy studies; improved fine-scale and fine-resolution sampling; improved understanding of the spatial scales of palaeoecological data; appropriate and powerful numerical techniques for data summarisation and synthesis; improved taxonomic resolution; improved chronological tools; increasing concern about site selection, problem formulation, and testable hypotheses; realisation that lake sediments are archives of a vast array of palaeoecological, biological, chemical, and physical variables; increasing realisation of the central importance of spatial and temporal scales in data interpretation – see, for example, Birks (1998), Seppä and Bennett (2003) Jackson and Williams (2004), Flessa and Jackson (2005a), Birks and Birks (2006), Smol (2008), and Jackson et al. (2009) for reviews of some of these advances) now allow palaeoecologists to explore many critical ecological questions, answers to which require the unique long-term temporal perspective provided by palaeoecology. What are the rates and nature of changes in ecological processes in response to environmental change? Which combination of abiotic and biotic processes results in a given ecological threshold being crossed? What ecological processes increase resilience to environmental change? Did novel ecosystems, so-called non-analogue systems, occur in the past? What combination of abiotic and biotic processes resulted in such novel ecosystems (Willis et al. 2010a)? Answers to these and related questions (Froyd & Willis 2008; MacDonald et al. 2008; Willis & Bhagwat 2010; Willis et al. 2010b) highlight the contributions that palaeoecological including environmental reconstructions can make not only in understanding ecological and evolutionary processes responsible for biodiversity patterns, but also in determining current and future management strategies necessary to ensure biodiversity conservation (Willis et al. 2010a).

Other ecological questions that palaeoecology can contribute insights to include the following. What are the major drivers of ecosystem dynamics at different time scales and do these drivers interact? How has climate change affected the distribution, magnitude, and frequency of disturbance regimes such as fires? What time lags have occurred between biotic response and climate change? Are there consistent patterns in time and/or space of population expansion, population extinction, and migration dynamics in relation to environmental change? Answers to all the questions raised here all require considerations of the past environment and the rates, magnitude, and inherent variability of environmental change.

Reliable, robust, and unbiased high-resolution environmental reconstructions including climate are thus an integral part of applied palaeoecology (Sensu Birks 1996) and of ecological palaeoecology (MacDonald et al. 2008; Willis et al. 2010a) as many ecological and conservation questions asked of palaeoecological data require environmental reconstructions. Similarly the understanding of historical ‘ecological legacies’ (Flessa & Jackson 2005a, 2005b; Willis & Birks 2006) in present-day ecosystems requires records of past climate or land-use changes (Millar & Woolfenden 1999; Swetnam et al. 1999; Foster et al. 2003). For example, Heiri et al. (2006) elegantly illustrate the use of a chironomid-based quantitative climate reconstruction as a driver in a vegetation dynamics model to simulate tree-line fluctuations during the Holocene and to test hypotheses about the causes of tree-line changes.

This essay reviews the range of quantitative approaches available for inferring past climate from late-Quaternary palaeoecological records. Although we focus our discussion on climate reconstructions, many of the approaches considered are also used to reconstruct other environmental variables (e.g. lake-water pH and total phosphorus) from limnic organisms such as diatoms (Birks 1998, 2010). We make no attempt to provide a comprehensive review of the vast array of available palaeoclimatic reconstruction approaches. Instead we present a personal perspective on the strengths and weaknesses of the major approaches used to reconstruct past climate from biological proxies, with particular emphasis on pollen and chironomid assemblages, the two groups of fossil organisms that we have most practical experience of working with. We also discuss, where relevant, beetles, plant macrofossils, and other groups of fossils.

**BASIC PRINCIPLES AND ASSUMPTIONS**

**Introduction**

Since the pioneering days of Quaternary palaeoecology in the first half of the 20th century, scientists have used fossils preserved in lake and bog sediments and the composition and physical properties of these sediments as a basis for reconstructing aspects of the past local and regional environment. The early studies of Blytt (1881), Andersson (1909), Iversen (1944), von Post (1946), and others using plant macrofossils, animal remains, pollen assemblages, and peat stratigraphy laid the foundations for many of the current ideas about late-Quaternary climate changes (see Birks 2008; Birks & Seppä 2010 for historical reviews).

An important aim of many Quaternary palaeoecological studies today remains the reconstruction of features of the past environment, in particular climate, from fossil assemblages preserved in terrestrial or marine sediments to help address the types of question we raised in the Introduction. Although fossil assemblages are usually meticulously counted with individual fossil pollen, ostracods, chironomids, foraminifera, etc. being routinely identified and enumerated using considerable time and effort, the resulting environmental reconstructions are often qualitative and are presented as broad climate ranges which are interpreted as “arctic”,...
violated that relate to the numerical approach used or to the aches for inferring past climate change based on biostratigraphical data. In many cases these reconstructions have been validated by comparing them with independent climate records from the mid-Pleistocene (Coope et al. 1998; Birks & Ammann 2000, Birks and Seppä 2000; Heiri & Millet 2005; Peyron et al. 2006). 2005). For the pre-glacial and early-Holocene, reconstruction methods based on biostratigraphical data are among the few approaches which can provide quantitative reconstructions that approach the temporal and spatial scales needed to allow the reconstructions to be compared with results from Earth system and general circulation models (e.g. Renssen & Isarin 2001; Renssen et al. 2009).

As with all methods for climate reconstruction, approaches for inferring past climate change based on biostratigraphical data may fail when important assumptions are violated that relate to the numerical approach used or to the ecological principles forming the basis of the reconstruction. The quality of all quantitative reconstructions strongly depends on the quality of the data-sets used, on the temporal chronologies of the data-sets used, on the performance and robustness of the numerical approaches applied to reconstruct past climate, on the extent to which these approaches realistically quantify and model the relationship between the biostratigraphical proxies and their environment in the modern world and in the past, and on rigorous numerical, ecological, and palaeoenvironmental evaluations of the resulting reconstructions.

Here we provide a review of the three basic approaches most commonly used by palaeoecologists to infer past climate based on biostratigraphical data, namely the indicator-species approach; the assemblage or analogue approach; and the multivariate calibration-function (‘transfer function’) approach. Since the latter approach is the most widely used approach in the reconstruction of past climate based on late-Quaternary biostratigraphical data, we review and discuss it in more detail than the other two approaches.

We discuss the general principles, requirements, and assumptions of climate reconstructions based on these three approaches. We then discuss individual methods within these approaches and outline their strengths and weaknesses. We indicate how rigorous application of evaluation and validation techniques, estimation of realistic errors of prediction, and sound ecological reasoning can be used to detect and reduce some of the problems that can occur when using the general approach of reconstructing past climate from proxy biostratigraphical data. Our emphasis throughout is on the basic biological concepts, the assumptions, requirements, and data properties of the various approaches, and on their strengths and weaknesses. We also discuss how modern ecological and biogeographical studies on organism responses to future climate change involve the indicator-species approach, the assemblage approach, or the multivariate calibration-function approach. We outline how such predictive studies are facing many of the same problems that palaeoecologists are facing, namely the hidden assumptions and limitations of bioclimatic-envelope modelling, problems of spatial autocorrelation, and the robustness and applicability of multivariate calibration functions. We conclude by outlining new approaches to climate reconstruction involving forward modelling procedures and Bayesian approaches, and suggesting possible areas for future improvements in quantitative climate reconstructions based on biological proxy data.


Principles, Notation, and Terminology

There are three main approaches to the quantitative reconstruction of past climates from biostratigraphical data
These approaches involve a space-for-time substitution and require information about the modern climatic preferences and tolerances of the taxa found as fossils. These data are usually obtained by exploring the distribution and abundance of organisms in relation to environmental variables in the modern world as an analogue to their expected preferences.
distribution and abundance in relation to the environmental variable of interest in the past (so-called ‘space-for-time’ substitution) (Jackson & Williams 2004). However, information on the response of organisms to environmental change can also be obtained from laboratory experiments (e.g. von Grafenstein et al. 1999; Brodersen et al. 2008) or by comparing variations in biotic assemblages during the instrumental period with time-series of measured changes in the environmental parameter (so-called ‘calibration’ in time or ‘time-for-space’ substitution) (e.g. Barnekow et al. 2007; Kamenik et al. 2009). The principle assumption of all climatic and all other environmental reconstructions in Quaternary palaeoecology is methodological uniformitarianism (Scott 1963; Gould 1965; Rymer 1978; Birks & Birks 1980; Hunley 2001), namely that modern-day observations and relationships can be used as a model for past conditions and, more specifically, that organism-environment relationships have not changed with time, at least in the late-Quaternary (Jackson & Overpeck 2000; Jackson & Williams 2004), so-called niche conservatism (Wiens et al. 2005; Pearman et al. 2008a, 2008b; Bennett et al. 2010; Wiens et al. 2010).

The basic idea of all quantitative reconstructions and the notation we use throughout are summarised in Fig. (1). We have fossil biological data \( Y_f \) (e.g. pollen or chironomid assemblages) at different depths or times in one or more sediment sequences (so-called climate ‘proxy’ data) and we want to reconstruct the past environment \( X_f \) (e.g. mean July temperature) for the times at which the fossil assemblages have been studied. Irrespective of the approach used to estimate or infer \( X_f \), we need modern distributional and/or abundance data \( Y_m \) about all or some of the species in the fossil assemblage and associated modern environmental data \( X_m \) in order to relate the occurrence and/or abundance of \( Y_m \) to the modern environmental variable(s) \( X_m \) that we are wanting to reconstruct \( X_f \) from our fossil assemblages \( Y_f \). The most commonly used forms of modern biological data \( Y_m \) in the three main approaches are summarised in Table 1, along with how the contemporary relationships with the modern environment \( X_m \) are established prior to reconstruction of \( X_f \) from \( Y_f \).

Although \( X_f \) can be estimated or inferred in many different ways, in practice nearly all quantitative reconstructions involve two main stages (Fig. 2). First, the responses \( U_m \) of the modern taxa \( Y_m \) to contemporary climate \( X_m \) are established. This is essentially a regression problem (ter Braak & Prentice 1988) and involves modern distributional data or a modern ‘training set’ of assemblages (‘response’ variables) with associated climate data (‘predictor’ variables). Second, the estimated modern responses \( U_m \) of \( X_m \) in relation to \( Y_m \) are then used to infer past climate variables \( X_f \).
from the composition of the fossil assemblages. This is a
calibration problem (ter Braak & Prentice 1988). These two
stages are summarised in Fig. (2). Before application to a
fossil data-set, the robustness and reliability of the modern
responses must be assessed by some form of cross valida-
tion. This cross-validation normally provides the basis for
producing robust estimates of the prediction error associated
with a given approach to environmental reconstruction. This
validation step is also shown in Fig. (2).

The term ‘transfer function’ is commonly used to refer to
all of these reconstruction approaches (e.g. Guiot & de
Vernal 2007). In particular, the modern analogue technique
(see below under The Assemblage Approach) is frequently
regarded as a ‘transfer function’ method. We avoid the use of
the term ‘transfer function’ altogether because it has a clear
and very different usage in statistics (Everett 2003). In its
place we use the term ‘calibration function’ approach to refer
to reconstruction methods such as two-way weighted averag-
ing (WA) and weighted averaging partial least squares
regression and calibration (WA-PLS) where there are an
explicit underlying taxon-climate response model and global
estimation of taxon parameters (see below The Multivariate
Calibration-Function Approach). Other methods that fall into
this approach but that are not discussed in this essay include
principal components regression (Imbrie & Kipp 1971),
partial least squares regression and calibration (Martens &
Næs 1989), Gaussian logit regression and calibration (ter
Braak & van Dam 1989; Birks et al. 1990), multinomial logit
regression and calibration (ter Braak & van Dam 1989; ter
Braak et al. 1993; ter Braak 1995), and correspondence anal-
ysis regression (Roux 1979) – see Birks (1995) for a review
of these ‘calibration function’ methods and related model-
free environmental reconstruction techniques. ter Braak and
Prentice (1988) and ter Braak (1996) provide a clear account
of the distinction between regression and calibration. ter
Braak (1995, 1996) notes that calibration is a type of
multiple-species bioassay where species are used to infer
environmental values from species data.

Modern training sets ($Y_m$) (e.g. pollen, chironomids)
contain many taxa (e.g. 100-300) whereas there may be 50-
200 samples. Data are usually quantitative and commonly
expressed as percentages of the total sample count. They are
thus closed, multivariate compositional data with a constant-
sum constraint (ter Braak 1995). They often contain many
zero values (up to 75% of all elements in the data matrix can
be zero) for sites where taxa are absent or unrecorded. The
data are complex, showing noise, redundancy, and internal
correlations, and often contain what may, in a particular
model, be regarded as outliers. Taxon abundance is usually a
unimodal function of the environmental variables (ter Braak
1996).

Modern climate data ($X_m$) usually contain many fewer
variables (c. 1-15) than the matching biological data. Climate
data rarely contain zero or absent values. Quantitative
climate variables often follow a normal distribution and
commonly show linear relationships and high correlations
between variables (e.g. mean July temperature and growing-
day degrees). There is thus much data redundancy. The
reliability and quality of the modern climate data can be
problematical in some instances.

Basic Requirements

There are at least seven major requirements in a quanti-
tative climate reconstruction using any of the three main
approaches (Birks 1995). These requirements are a result of
the complex numerical and ecological properties of modern
biological and climate data such as non-linear species-
environment responses. These requirements are as follows
(from Birks 1995).

1. A biological system is required that produces
abundant identifiable fossils and that is responsive
and sensitive to the climate variable(s) of interest
today at the spatial and temporal scales of study.

2. A large high-quality data-set of modern biological
data ($Y_m$) (species occurrences and absences, surface-
samples from lakes containing modern assemblages of
sub-fossil pollen, chironomids, etc.) and associated
climate data ($X_m$) is available. This data-set should
be representative of the likely range of climate variables
in the past ($X_0$), be of consistent and detailed
taxonomy and nomenclature (Finkelstein et al. 2006),
be of comparable quality (data-extraction procedures,
spatial scale, count size, sampling methodology,
preparation procedures, counting techniques) and, in
the case of surface samples, be from the same type of
sedimentary environment as the fossil samples (e.g.
lakes) (Bjune et al. 2010) and hence have comparable
taphonomies (cf. Minkley & Whitlock 2000;
Whitmore et al. 2005; Gonzales et al. 2009a; Tonello et al.
2009; Fletcher et al. 2010; Goring et al. 2010).

3. The fossil data-sets ($Y_f$) used for reconstruction
purposes should be of comparable taxonomy and
nomenclature, quality, and sedimentary environment
as the modern data ($Y_m$).

4. Good independent chronological control is required
for the fossil data-sets to permit correlations and
comparisons and, if required, to allow an assessment
of the rates of biotic response in relation to climate
changes (Birks & Ammann 2000; Birks et al. 2000).

5. Robust numerical methods for the regression and
calibration steps are required that can adequately
model the complex, non-linear, and often unimodal
relationships between modern taxa and climate. The
numerical methods used are theoretically, statisti-
cally, and ecologically sound, are easy to understand,
per-form well with large and small data-sets and
taxon-poor or taxon-rich assemblages, are not too
demand-ing in terms of computing resources, and the
relevant computer programs and data-sets are
available to the research community.

6. Reliable and realistic numerical estimation of stand-
ard errors of prediction for the modern data-set as a
whole ($X_m$, $Y_m$) and for each reconstructed climate
value ($X_0$) is required. As the reliability of the recon-
structed climate values may vary from one fossil
sample to another depending on, for example,
composition or preservation, sample-specific standard
erors of prediction are needed.
7. Critical ecological, numerical, and palaeoclimatic evaluations of all reconstructions \((X_t)\) are needed, as all numerical regression and calibration procedures are designed to produce a result. It is, however, essential to evaluate if the reconstruction is ecologically meaningful, and numerically and palaeoclimatologically reliable, and to validate it by comparison with other independent records.

**Basic Assumptions**

There are at least six major assumptions in all climate reconstructions from palaeoecological data (Imbrie & Kipp 1971; Birks et al. 1990; Birks 1995, 2003). Originally it was thought that there were only five key assumptions (Birks 1995) but the work of Telford and Birks (2005; 2009) has highlighted a sixth major assumption. These assumptions apply, in varying degrees, to all the three major approaches to climate reconstruction.

1. The \(m\) taxa in the training set \((Y_m)\) are systematically related to the climate \((X_m)\) in which they live.
2. The climate variable(s) \((X_t)\) to be reconstructed is, or is linearly, or at least monotonically, related to an ecologically important determinant in the system of interest and that it is on a continuous quantitative scale. Presence/absence (1/0) of a particular climate mode cannot be reconstructed using the methods discussed here.
3. The \(m\) taxa in the training set \((Y_m)\) are the same biological entities as in the fossil data \((Y_f)\) and their ecological responses to \(X_m\) and \(X_f\) have not changed over the time represented by the fossil assemblages. Thus the contemporary spatial patterns of taxon abundance \((Y_m)\) in relation to \(X_m\) can be used to reconstruct changes in \(X_f\) through time from \(Y_f\) (‘space-for-time’ substitution).
4. The mathematical methods used adequately model the species responses in \(Y_m\) to \(X_m\) and produce calibration functions \((U_m)\) with sufficient predictive power to allow accurate and unbiased reconstructions of \(X_f\).
5. Other environmental variables than the one(s) of interest \((X_t)\) have had negligible influence on \(Y_f\) during the time window of interest, the joint distribution of these variables of interest in the past was the same as today, or their effect on \(Y_f\) did not lead to past changes in assemblage states resembling shifts indicative in the modern environment of changes in the variable of interest.
6. In model validation and in the estimation of prediction errors by some form of cross-validation, the test data are statistically independent of the training set (Telford & Birks 2005; 2009).

We now consider the three major approaches to climate reconstruction, starting with the oldest and most-used approach, the indicator-species approach.

**THE INDICATOR-SPECIES APPROACH**

**Basic Principles and One or a Few Indicator Species**

Fossil occurrences of a species with known modern environmental preferences and tolerances provide a basis for inferring the past environment (Birks 1981). Assuming methodological uniformitarianism (Rymer 1978) and niche conservatism (Wiens & Graham 2005; Pearman et al. 2008a; Wiens et al. 2010), the past environment is reconstructed to have been the modern environmental, Grinnellian (Soberón 2007) or gamma-niche (Morin & Lechowicz 2008) of the species found as a fossil, namely “the range of values of environmental factors that are necessary and sufficient to allow a species to carry out its life history” (James et al. 1984). In reality we can only delimit from observational data the realised Grinnellian (cf. Soberón & Peterson 2005) and within it the realised regeneration niche (Grubb 1977) if data about reproduction and regeneration are available. Colwell and Rangel (2009) clarify the relationship between the Grinnellian (an environmental feature) and the Hutchinsonian niche (a species property) and its biotope (physical setting). The indicator-species approach requires information (Table 1) about what environmental factors may influence the distribution and regeneration today of the species concerned. (Species abundances are almost always not considered in the indicator-species approach in palaeoecology (but see Fauquette et al. 1998, 1999)).

The commonest means of obtaining such environmental information is to compare present-day distributions of species with selected climate variables of potential eco-physiological significance (Dahl 1998), such as the mean temperature of the coldest month, maximum summer temperature, or some measure of overall growing-season warmth such as respiration sums. If the geographical trend of an eco-climate variable covaries with the present geographical distribution of the species of interest, a cause-and-effect relationship is often assumed (Birks 1981). For example, Conolly and Dahl (1970) related the modern distribution of *Salix herbacea* in the British Isles to the 23°C maximum summer temperature isotherm for the highest points where *S. herbacea* grows today. Macrofossil records show that this dwarf willow occurred widely in lowland Britain and Ireland during the late-glacial Younger Dryas stadial where today maximum summer temperatures are 26-27°C, suggesting there was a depression in maximum summer temperature of 3-4°C during the Younger Dryas (see Dahl 1998).

This correlative approach of comparing modern distributions with contemporary climate variables, pioneered by Andersson (1902, 1903, 1909), has proliferated in the last 10-15 years (Soberón 2007; Franklin 2010). Now called bioclimate-envelope modelling and involving a wide range of modelling methods (e.g. Guisan & Zimmermann 2000; Anderson et al. 2003; Thuiller et al. 2003; Araújo et al. 2005a, 2005b; Leathwick et al. 2005; Araújo & Guisan 2006; Elith et al. 2006; Phillips & Dudik 2008; Baselga & Araújo 2009; Elith & Leathwick 2009; Franklin 2010), it is widely used to predict impacts of future climate change on species distributions (e.g. Currie 2001; Shafer et al. 2001; Thuiller et al. 2005, 2006; Hamann & Wang 2006;
Heikkinnen et al. 2006; Rehfeldt et al. 2006; Levinsky et al. 2007; Huntley et al. 2008; Iveson et al. 2008; Jeschke & Strayer 2008; Thuiller et al. 2008; Lawler et al. 2009; Soberón & Nakamura 2009; Franklin 2010; Yates et al. 2010. There is currently much debate about the basic assumptions underlying this approach (e.g. Pearson & Dawson 2003; Hampe 2004; Pearson & Dawson 2004; Heikkinnen et al. 2006; Dormann 2007a; Beale et al. 2008; Jiménez-Valverde et al. 2008; Thuiller et al. 2008; Araújo et al. 2009; Aspinall et al. 2009; Beale et al. 2009; Duncan et al. 2009; Morin & Thuiller 2009; Peterson et al. 2009; Willis & Bhagwat 2009; Chapman 2010; Mouton et al. 2010; Real et al. 2010; Willis et al. 2010b), namely that present-day distributions are controlled by climate (Araújo & Luoto 2007; Beale et al. 2009; Blach-Overgaard et al. 2010; Chapman 2010), that the distributions are in equilibrium with climate today (Svenning & Skov 2004; Araújo & Pearson 2005; Svenning & Skov 2005, 2007; de Marco et al. 2008; Svenning et al. 2008; Normand et al. 2009), that the distributional data and the climate data are reliable (Rolland 2003; Kittrics & Leriche 2010) and, in the case of montane and alpine biota, that the modern climate data are from the same altitudes as where the species being modelled actually grow (Dahl 1951, 1998; Randin et al. 2006; Lundquist & Cayan 2007; Pape et al. 2009; Randin et al. 2009a; Scherrer & Körner 2010, 2011), and that the observed realised distributional area is the potential and fundamental distributional area (Colwell & Rangel 2009; Soberón & Nakamura 2009). Despite all the effort in recent years that has gone into identifying and understanding the major sources of uncertainty associated with the use of bioclimate envelopes to model and predict current and future species distributions and developing performance criteria for different models (e.g. Kadmon et al. 2003; Araújo et al. 2005b; Guisan & Thuiller 2005; Luoto et al. 2005; Thuiller et al. 2005; Araújo & Guisan 2006; Araújo & Rahbek 2006; Elith et al. 2006; Heikkinnen et al. 2006; Lawler et al. 2006; Araújo & Luoto 2007; Botkin et al. 2007; Heikkinnen et al. 2007; Luoto et al. 2007; Beale et al. 2008; Green et al. 2008; Luoto & Heikkinnen 2008; Araújo et al. 2009; Diniz-Filho et al. 2009; Elith & Leathwick 2009; Engler et al. 2009; Titou et al. 2009; Randin et al. 2009b; Franklin 2010; Hoffman et al. 2010; Mouton et al. 2010; Smulders et al. 2010), the key assumption remains, namely that climate is assumed to limit the observed distribution in bioclimate envelope models. The greatest uncertainty is whether this assumption holds for the species modelled today (Beale et al. 2008; Duncan et al. 2009; Chapman 2010), and hence in predictions for the future (Dormann 2007a) and in the use of such bioclimatic-envelope models as a basis for inferring past climate from fossil remains.

An additional critical question in all bioclimate-envelope models is what climate variables should be included in such models (Gavin & Hu 2005, 2006; Norris et al. 2006; Jackson et al. 2009). Temperature comprises a large set of ecophysiologicaly relevant variables (Dahl 1998). The simple variable, annual mean temperature, covaries spatially with many broad-scale biotic patterns at regional and global scales (Leith & Whittaker 1975). Seasonal or monthly means may provide additional explanatory power (in a statistical modelling sense) (Jackson et al. 2009). These climate means and integrated ecophysiological measures (e.g. respiration sum, growing-degree days) are widely used in bioclimatic-envelope modelling and perform well in predicting modern distributions. Of course, organisms have maximum and minimum temperature thresholds and their sensitivity may vary between individuals and populations (e.g. Pigott 1970, 1975; Carter & Prince 1981; Pigott 1982; Larcher 2003; Norris et al. 2006; Ibáñez et al. 2007, 2008; Cote et al. 2008; Jackson et al. 2009; Proctor 2009). As Jackson et al. (2009) discuss, a proximal temperature predictor of a tree-range limit might, in reality, consist of the probability that temperature falls below a threshold within a certain number of days after bud burst, the frequency of years in which summer temperatures persist below a certain threshold, or freezing resistance (e.g. Sakai 1971; Sakai & Weiser 1973; Bigler et al. 2007; Morin et al. 2007; Morin & Thuiller 2009). The potential number and variety of such proximal variables and hence niche dimensions may be enormous and be beyond the current limits of empirical, correlative procedures (Jackson et al. 2009). Such high dimensionality is usually ignored by assuming a strong covariance between a simple and easy-to-obtain climate variable (e.g. mean annual temperature) and ecologically critical variables (e.g. respiration sum) (Dahl 1998). The apparent success of bioclimate-envelope modelling comes from this strong spatial covariance between easily measured variables and the poorly understood and largely unknown ecologically critical variables (Jackson et al. 2009). From a palaeoecological viewpoint, a critical question is whether this spatial covariance remains constant through late-Quaternary time (assumption 5 above). Jackson et al. (2009) argue that although the strength and direction (negative or positive) of this climatic covariance may be conserved through time, the covariance structure (slope, intercept, dispersion) may change as atmospheric circulation patterns respond to different forcing factors, feedbacks, and changing atmospheric composition (Jackson & Overpeck 2000; Williams & Jackson 2007; Porch 2010). Such inconstancy will clearly reduce the predictive power and reliability of bioclimate-envelope models when applied to past and future climate states with different covariance structures than today’s climate (Jackson et al. 2009; Porch 2010).

As not all possible climate states are realised today (Jackson & Overpeck 2000; Jackson & Williams 2004; Williams & Jackson 2007), this implies that in contemporary data an ‘apparent’ threshold value for some climate parameter (e.g. summer temperature) may not actually be ecologically relevant even though it is consistently correlated with ‘real’ threshold values of a climate variable of critical physiological importance today. For example, the apparent threshold in summer temperature may, in reality, be related to a real threshold in winter or spring temperature. As a result, the indicator-species approach to reconstruction may fail under climate conditions in the past (or predicted conditions in the future) simply because these climate states with different climate parameters and covariance structures are not realised today. A palaeoecological example is from the middle Weichselian (marine isotope stage 3a) (Helmens et al. 2007) in northern Finland where a disagreement is found between air temperatures inferred from aquatic organisms (chironomids using the calibration-function approach and aquatic plants and other invertebrates using the indicator-species approach) and temperatures inferred by
calibration functions from fossil pollen assemblages. One hypothesis to explain these discrepancies is that cold winter temperatures influenced the terrestrial vegetation but not the aquatic organisms, which in lakes are effectively isolated from sub-zero temperatures by winter ice-cover. This hypothesis implies that whereas both aquatic organisms and pollen assemblages co-vary strongly with summer, winter, and mean annual temperature in the modern environment, they were affected to a different extent by summer and winter temperature in the past in a ‘summer-warm’ tundra or forest-tundra landscape representing a non-analogue climate state. Although the problem of non-analogue climates arises in all climate reconstruction procedures, we suspect that the indicator-species approach and the assemblage approach (see below) are the most susceptible to biases resulting from non-analogue climates.

The robustness of bioclimate-envelope modelling results can be greatly enhanced by explicitly incorporating mechanistic links between the functional traits of organisms and their environments into species distribution models (e.g. Kearney & Porter 2004, 2009; Kearney 2006; Colwell & Rangel 2009; Buckley et al. 2010). Physiological and biophysical principles can be used to link distributional data to the physiological responses and constraints of species to provide a mechanistic view of the fundamental niche which can then be mapped and compared with the realised niche today. Such mechanistic niche modelling (Kearney 2006) has considerable potential in predicting or reconstructing responses in novel or non-equilibrium conditions (Colwell & Rangel 2009).

In some instances it may be more realistic to consider species distributions in relation to two or more climate variables (e.g. Hintikka 1963; Gavin & Hu 2005, 2006). This bivariate or even multivariate (Gavin & Hu 2005, 2006) approach was pioneered by Samuelsson (1916) for the northern limit of Corylus avellana in Scandinavia and developed by Iversen (1944) in his classic work on Viscum album, Ilex aquifolium, and Hedera helix in Denmark (see Fægri (1950) for a discussion of the importance of this bivariate approach). Samuelsson (1916) found that at the northern limit of Corylus, lower summer temperature could be compensated for by a longer growing season and thus that the presence of fossil Corylus nuts did not give a direct, single palaeotemperature value (Andersson 1902, 1903, 1909) but a series of such values, each corresponding to a given growing-season duration (Fægri 1950). On the basis of detailed field observations, Iversen (1944) delimited the ‘thermal limits’ or bioclimatic-enclosures within which Viscum, Ilex, and Hedera flowered and produced seed (the Grinnellian and regeneration niches within Denmark). Iversen showed that Ilex aquifolium is intolerant of cold winters but tolerant of cold summers. Hedera helix is intolerant of winters with mean temperatures colder than -1.5°C but requires warmer summers than Ilex. Viscum album is tolerant of cold winters but requires warmer summers than either Ilex or Hedera. These shrubs are ideal ‘indicator species’ in palaeoecology because their pollen is readily identifiable to species level, it is not blown great distances so interpretation problems arising from far-distance transport do not arise, and their fruits (nuts and berries) are rapidly dispersed by birds. Their distributions, at least at the scale studied by Iversen (1944), are likely to be in equilibrium with climate. The validity of this assumption has been elegantly shown by Walther et al. (2005) who showed that the northern limit of Ilex has shifted northwards in the last 50 years, presumably in response to warmer winters in recent decades. From fossil pollen occurrences, Iversen (1944) applied his modern climate envelopes to infer that mid-Holocene summers were 2-3°C warmer and winters were 1-2°C warmer than today in Denmark.

### Many Indicator Species

This general bioclimate-envelope approach has been extended to several taxa simultaneously to identify areas of climate overlap based on pollen (e.g. Grichuk 1969; Grichuk et al. 1984; Markgraf et al. 1986; Kershaw & Nix 1988; McKenzie & Busby 1992), plant macrofossils (e.g. Sinka & Atkinson 1989; Mosbrugger & Utescher 1997; Sharpe 2002), chironomids (e.g. Dimitriadis & Cranston 2001), molluscs (e.g. Moine et al. 2002), ostracods (e.g. Horne 2007; Horne & Mezquita 2008), and beetles (e.g. Atkinson et al. 1987; Elias 1994, 1997; Elias et al. 1999; Elias 2001; Porch 2010), the so-called mutual climatic range (MCR) approach. The assumptions are identical to other bioclimate-envelope methods discussed above. Although the mutual climatic range method is simple in principle, problems arise when, as a result of non-analogue climate states, taxa co-occur in fossil assemblages that do not have overlapping climate ranges today. In such circumstances, a possible solution is to find the least dissimilar combination(s) of taxa (Guilot & de Vernal 2007). The reconstructed values are ranges for each of the climate variables considered. In general, these ranges are narrower for species-rich assemblages. However, in very species-poor assemblages, the presence of a taxon with an extremely narrow range of occurrence today may strongly bias the reconstructed climate ranges. Various attempts have been made to narrow the climate ranges reconstructed by MCR. One attempt uses a sine model and maximum likelihood envelopes to obtain more reliable modern climate data for beetles in a topographically and climatically diverse landscape such as New Zealand (Marra et al. 2004; 2006). A second attempt at narrowing MCR ranges involves an ingenious probabilistic approach (Klotz & Pros 1999; Pros et al. 2000; Klotz et al. 2003; 2004). Instead of simply calculating environmental envelopes with an equal reconstructed probability of all climatic states contained within the envelope, this method estimates mutual climate probability spheres for fossil samples. A large number of MCRs are calculated based on the entire set of possible pollen assemblages that can be expected to occur in the modern environment based on present-day plant distributional data and modern climate data on a 0.5° x 0.5° grid (New et al. 1999). MCRs for the variable of interest calculated for the gridded synthetic pollen assemblages are compared to the observed values of the variable of interest. Probability distribution patterns within the different MCRs calculated based on the synthetic assemblages can be established and analysed statistically. The synthetic florals show that only a part of the estimated MCR is actually represented by measured values of the variable of interest in the modern environment. This restricted envelope is then used to correct MCRs calculated for fossil assemblages, assuming that MCRs inferred for fossil assemblages can be corrected based on the probability distribution pattern observed for similar
envelopes in the modern environment. These narrower ranges are considered to represent the probability interval for the climate variable of interest. For graphical display, only the mean values of the upper and lower limits of the probability intervals are shown (e.g. Feurdean et al. 2008a, 2008b). This approach illustrates how the MCR technique that relies entirely on total geographical ranges exaggerates the climate ranges, whereas the synthetic assemblage approach produces narrower, more likely climate ranges based on the probability distribution of the climate states within the MCRs calculated for the synthetic assemblages.

Kühl (2003) and Kühl et al. (2002) have combined the Iversen (1944), Grichuk (1969), MCR, and co-existence approaches (Atkinson et al. 1987; Mosbrugger & Utescher 1997) to provide a potentially more rigorous approach to climate reconstruction based on presence/absence data (e.g. plant macrofossils). Kühl’s approach involves probability density functions (the so-called pdf-method) (Table 1). It combines modern plant distributional data for individual taxa with gridded climate data and summarises the modern climate-taxon relationships as conditional probability density functions (climate|taxon present) rather than as ranges or thresholds. A normal distribution is used to estimate the pdfs robustly. As the joint distribution of climate variables within Europe is not uniform, and as this distribution may have changed with time, a weighting of the modern climate variables is included to account for this non-uniform distribution and to make the estimated pdfs independent of the climate distributions today (Kühl et al. 2002). By assuming statistical independence, a joint pdf is calculated for a fossil assemblage as a product of the pdfs of the individual taxa in the assemblage. Each taxon is weighted by the dispersion of the modern climate range, so ‘narrow’ indicators receive ‘high’ weight. The product of the pdf’s is the most likely past climate and its uncertainty. The reconstructed climate is based on the complete distribution and climate data of all the taxa included and because it is a multiplicative technique, no single taxon is decisive (Kühl & Litt 2003). The pdf approach has been used to reconstruct Holocene (Litt et al. 2009; Kühl et al. 2010) and last interglacial and early Weichselian climate from pollen assemblages (expressed as presences and absences) (Kühl 2003; Kühl & Litt 2003; Kaspar et al. 2005). The pdf climate reconstructions have been compared, in many cases, with climate reconstructions based on quantitative pollen assemblage data using a modern analogue technique (see The Assemblage Approach below). These comparisons suggest that the pdf method generally underestimates past climate variability but may provide robust estimates of long-term climate trends rather than of climate variability of small amplitude (Litt et al. 2009; Kühl et al. 2010). This is not surprising as the bioclimatic envelopes of many central European trees and shrubs are very broad so that presence/absence data can only provide palaeoclimatic information when the site in question is near the range margins of some of the ‘key’ indicator taxa (e.g. Hedera, Ilex, Viscum, Taxus). The pdf method has been extended by Neumann et al. (2006) as a Bayesian indicator taxa model and used by Kühl et al. (2007, 2010) and Kühl and Gobet (2010). This extension combines the conditional pdfs with the prior probability density of climate to estimate Bayesian posterior probability density functions (Robertson et al. 1999). Two-dimensional normal distributions are used as parametric functions to describe the conditional pdfs of July and January temperature, thereby allowing the influence of these two variables to be considered together and hence for both variables to be reconstructed simultaneously (Kühl & Gobet 2010).

**Strengths and Weaknesses**

There are many assumptions behind the various indicator-species-based approaches to reconstruct climate from fossil assemblages, just as there are in modern bioclimatological approaches (see the conditional pdfs of climate and taxa). Perhaps the greatest limitation is that the indicator-species approaches are based on presence/absence data of taxa even where relative abundances of the taxa are often available, especially for pollen, chironomids, and ostracods. The indicator-species approach, relying on presence/absence data only, is very sensitive to count size, as the probability of finding a single pollen grain of a critical indicator taxon (e.g. Hedera helix) will increase as more and more pollen are counted. In some situations, when there are assemblages that no longer exist together today, abundances cannot be used in the assemblage of calibration-function approaches. For example, Pliocene fossil pollen assemblages from southern Europe contain not only Mediterranean taxa but also taxa that occur in China and North America today. In such instances, an indicator-taxa approach is the only choice. Fauquette et al. (1998, 1999) improved the basic MCR approach by using taxon abundances (as abundance classes of absent, present, strongly present, abundant) to refine the climate range identified by the presence of a given pollen taxon. For example, Quercus deciduous-type pollen is considered to be present at 5% with an annual temperature range between -20 and 30°C. Once its percentage passes a defined threshold, the taxon is considered to be abundant and the climate range is reduced. Quercus deciduous-type is considered abundant over 20% and the annual temperature range changes to between 5 and 23°C. This approach warrants further use as it is a considerable improvement over the use of presence/absence pollen data only in MCR and related techniques such as the probability density function methods of Kühl et al. (2002).

MCR approaches assume that a taxon has an equal probability of occurrence anywhere within its climate range (Huppert & Solow 2004; Horne & Mezquita 2008). This assumption is unlikely to be valid for ecological or biogeographical reasons (Christiansen & Fenchel 1977; ter Braak & Prentice 1988; Hengeveld 1990, but see Sagarin et al. 2006) for a contrasting analysis) and has been shown not to be true in many empirical studies (e.g. Horne & Mezquita 2008), in particular where response surfaces have been constructed to illustrate the probability of occurrence of a taxon at particular points in climate space (e.g. Huntley et al. 1995; Thompson et al. 1999a, 1999b, 2000; Shafer et al. 2001; Thompson et al. 2001; Bray et al. 2006). Given such response surfaces and/or the frequency of species occurrences in relation to selected climate variables, robust numerical methods of non-linear regression and calibration using maximum likelihood estimation exist for estimating not climatic ranges but the most likely value of the climate
variable of interest and its statistical uncertainty (e.g. ter Braak & Barendregt 1986; ter Braak & Looman 1986; ter Braak & Prentice 1988; Huppert & Solow 2004).

A major problem in the indicator-species approach is how to test the reliability of these methods (Mouton et al. 2010). Model validation ideally requires an independent test-set but when the two sets of variables (Figs. 1 and 2) being considered (geographical distributions of taxa and broad-scale climatic variables) show strong spatial auto-correlation (Beale et al. 2010; de Knegt et al. 2010), it is impossible to test a MCR model with an independent test-set (Telford & Birks 2005; 2009) because the geographical position of any test-set used will fall within the geographical range of the primary biological data used in the model (Araújo et al. 2005a). To address this issue in an MCR approach applied to beetle data, Bray et al. (2006) proposed “to avoid circular reasoning in these experiments (to evaluate the accuracy and sensitivity of the MCR method), care was taken to use only samples of modern beetles that have not previously been used in the construction of the primary MCR database”. However, this seems to be impossible to implement as the beetle data source they quote for the MCR database are broad-scale distribution maps and atlases containing the areas with the sites used to evaluate the MCR method. Porch (2010) uses leave-one-out cross-validation (jack-knifing) to evaluate beetle-based climate-envelope models in Australia where the modern beetle data are based on collections and museum specimens from 5500 separate locations. However, problems of spatial autocorrelations (Telford & Birks 2005; 2009) will arise nevertheless with data of these types, as discussed in the next section on The Assemblage Approach. Comparison of reconstructions with palaeoclimate records developed from other, independent climate proxies therefore seems the only way of evaluating MCR-based inferences whereas methods for producing reliable and robust estimates of prediction errors are presently not available for the standard MCR approach.

Despite its antiquity in palaeoecology, the indicator-species approach remains a potentially useful tool in reconstructing past climates from fossil assemblages of, for example, plant macrofossils, molluscs, and beetles where taxon abundances in the sediments are not necessarily a direct reflection of the former abundance of the taxon in the past. It is potentially valuable when the fossil assemblages appear to have no modern analogues, for example in the early or middle Pleistocene or the Pliocene, when no reliable modern assemblages are available because of intense human impact in, for example, central Europe or the Mediterranean basin, or when there are no data-sets of modern assemblages available at all (e.g. Porch et al. 2009). In the latter case, modern distribution data from a range of sources can be relatively easily incorporated into species-climate envelopes even when the biological sampling techniques are very different to standard palaeoecological approaches (e.g. Dimitriadis & Cranston 2001). It is important to remember, however, that data quality as well as data quantity determine the reliability of any bioclimate-envelope model (Mateo et al. 2010), as they do in all ecological or biogeographical studies.

Given the increasing availability of modern distributional data of taxa in the form of atlases and on-line data-bases (Graham et al. 2004), of fossil pollen records in data-bases (Gajewski 2008), of gridded climate data (New et al. 1999), of robust non-linear numerical methods for regression modelling and calibration reconstructions (Araújo & New 2007; Thuiller et al. 2009), and of suitable software (e.g. Guo & Liu 2010; Tarroso & Rebelo 2010; Warren et al. 2010), what are the limiting factors in a detailed and rigorous application of the indicator-species approach in palaeoecology?

The basic assumptions of bioclimate-envelope modelling (Dormann 2007a) are as relevant in predicting modern and future distributions as they are in reconstructing past climates. The modern distributional data used in such modelling should include not only presences but also absences (Phillips & Dudik 2008; Phillips et al. 2009; Soberón & Nakamura 2009; Ward et al. 2009; Lobo et al. 2010, but see Phillips & Elith (2010) for using presence data only) if probabilities of occurrence are to be estimated (cf. Argáez et al. 2005). Transformation of abundance data (e.g. pollen percentages) into ordinal classes reflecting absence, presence, and abundance (Fauquette et al. 1998, 1999) should be used more frequently. The appropriateness of the modern climate data used is very critical (Daly 2006; Ashcroft et al. 2008, 2009; Fridley 2009; Randin et al. 2009a; Kitiricos & Leriche 2010; Roubicek et al. 2010; Tabor & Williams 2010). In species-climate modelling it is assumed that modern climate data used are the actual climate values where the species occurs in its known localities. Climate stations tend to be at low altitudes whereas cold-tolerant species tend to occur at high altitudes, especially in the southern parts of their range (Lundquist & Cayan 2007; Pape et al. 2009). Unless the climate data are adjusted for the altitude of the localities where the species occurs, there will be a bias towards higher temperatures in climate reconstructions based on, for example, macrofossil or coleopteran assemblages of alpine and montane species. Although the interpolation algorithms and statistical models for modern climate estimation are sophisticated and high-resolution digital elevation models can be used to incorporate adiabatic lapse rates and regional climate (Randin et al. 2006), they still predict meteorological (2 m above ground surface) air conditions rather than actual life conditions for alpine plants and coleopterans (Scherrer & Körner 2010, 2011). It is questionable whether such gridded or interpolated climate data reflect the actual alpine environment where the majority of organisms live in microhabitats strongly decoupled from atmospheric conditions and interacting with micro-topography at a very fine spatial scales (Lookingbill & Urban 2003; Scherrer & Körner 2010, 2011). Spatial heterogeneity in climate is a very important environmental feature and is of critical importance in the reliability and usefulness of bioclimate-envelope models that use mesoscale climate data (Ashcroft et al. 2009; Ackerly et al. 2010; Bennie et al. 2010). When the biological distribution data are derived from distribution maps and atlases, the altitudes at which the species grow are often unknown so the climate data from lowland climate stations used in MCR are likely to be ecologically unrealistic. Another critical point is that as new data-analytical techniques are rapidly being developed, existing taxon-climate data-sets should be made available to researchers developing new modelling procedures. As Huppert and Solow (2004) report in their work on developing new numerical techniques
to reconstruct climate from fossil beetle assemblages, “despite repeated attempts, we have been unable to acquire data to permit a direct comparison of the results of our method with the results of the MCR method. We recognize the value of such a comparison and we regret the unavailability of such data”. As many indicator-species approaches, particularly the MCR method, place major emphasis on the range limits of species rather than the probability of occurrence within their range, understanding the dynamics of range limits in relation to climate is critical (Gaston 2009; Pigot et al. 2010). Recently, Keith et al. (2008), Anderson et al. (2009), Buckley et al. (2010), and Huntley et al. (2010) have shown the importance and feasibility of moving from simple bioclimatic-envelope models to models that incorporate dynamic climate change and metapopulation dynamics (see also Jackson et al. 2009 and Midgley et al. 2010). Palaeoecologists using bioclimate-envelope approaches to reconstruct past climate from fossil assemblages could profitably test the robustness of their correlative methods by applying appropriate statistical tests to establish if the distribution of the taxa used in climate reconstructions show statistical relationships with climate, along the lines of Beale et al. (2008, 2009) and Chapman (2010). A final and currently insoluble problem concerns reconstructions of past climatic variables under conditions with novel or non-analogue climates (Jackson & Williams 2004; Williams & Jackson 2007). Here the covariance structure between the climate variable being reconstructed such as mean July temperature and an eco-physiologically relevant variable such as respiration sum may not be the same as it is today (Jackson et al. 2009). Climate reconstructions under such conditions remain a major challenge (Morin & Lechowicz 2008; Gonzales et al. 2009b; Porch 2010). Predicting biotic responses in a future world with non-analogue climate (MacDonald 2010) is equally challenging.

THE ASSEMBLAGE APPROACH

Basic Principles

In contrast to the indicator-species approach, the assemblage approach considers the fossil assemblage as a whole and the relative abundances of all the different fossil taxa (Birks & Birks 1980). It has been widely used in an intuitive, non-quantitative way for many decades. For example, fossil pollen assemblages can be interpreted, using a range of criteria, as reflecting tundra, pine forest, or deciduous forest. Past environmental inferences for the fossil assemblages are then based on the present-day environment in which these vegetation types occur today. In the 1960s the interpretation of fossil pollen assemblages in terms of past vegetation types was put on a firmer basis through systematically studying modern pollen assemblages from known vegetation types (Wright 1967) and then by comparing modern and fossil pollen assemblages in a qualitative modern-analogue matching procedure (e.g. McAndrews 1966; Wright et al. 1967; Birks 1973a, 1973b). More recently, the assemblage approach has developed a more quantitative basis, the so-called modern analogue technique (MAT) and the related response-surface approach (Table 1).

The basic idea of MAT is to compare numerically, using a dissimilarity measure (e.g. squared chord distance) (Overpeck et al. 1985; Prell 1985; Simpson 2007, 2011) a fossil assemblage with modern assemblages. Having found the modern sample(s) that is (are) most similar to the fossil assemblage, the past climate for the fossil sample is inferred to be equivalent to the state of the climate variable(s) of interest for the analogous modern sample(s). The procedure is repeated for all fossil samples and a simultaneous reconstruction of one or several climate variables can be made on the basis of the modern analogues. The climate reconstruction(s) can be based on the modern sample that most closely resembles the fossil assemblage or, more reliably, it can be based on the mean or the weighted mean of, say, the 10 or 25 most similar modern samples, with weights being the inverse of the dissimilarities so that modern samples with the lowest dissimilarity (= highest similarity) have the greatest weight in the climate reconstruction. Williams and Shuman (2008) found for a large North American data-set of modern pollen assemblages that strong weighting by the inverse of the squared chord distance dissimilarity reduced the predictive ability of their MAT model, whereas there were little differences if an unweighted average or an average weighted by the inverse of the chord distance was used.

A critical question is to discover how many analogues to include in a reconstruction. An estimate of how many analogues to include in the reconstruction must be derived by numerical cross-validation. Procedures involving receiver operating characteristic (ROC) curves (Gavin et al. 2003; Wahl 2004) are not appropriate here as the analogues being sought are not 1/0 vegetation types (as in analogue matching (Simpson 2011) with the ROC approach) but the closest multivariate assemblage. Leave-one-out estimates of the climate variable(s) of interest based on the modern assemblage data-set are obtained for 1, 2, …k modern samples when the inferred or predicted value for the one sample left out is determined from the modern training data-set (excluding the single test sample). The procedure is repeated, leaving out another sample to form a test sample, until all samples have been excluded once. The predicted and observed values for the excluded samples based on 1, 2, … k analogues are differenced to calculate the prediction residuals. The root mean square error of prediction (RMSEP) and associated model statistics such as the mean bias, the maximum bias, and the coefficient of determination (r²) between predicted and observed values (Birks 1995; Barrows et al. 2000; Barrows & Juggins 2005) are then calculated (Simpson 2007, 2011). The value of k that gives the lowest RMSEP is then used in climate reconstructions from fossil assemblages and this RMSEP is sometimes assumed to be the prediction error for all the palaeoenvironmental inferences. With improving computing resources, it is now possible to derive the value of k for models with the lowest RMSEP as assessed by the more computer-intensive procedure of bootstrapping (Birks et al. 1990) the modern samples and to generate bootstrap-derived sample-specific errors for each fossil sample using many (usually 1000) bootstrap cycles (Simpson 2011). An alternative measure of reconstruction uncertainty suggested by ter Braak (1995) is the standard error of the estimates calculated as the weighted sample variance among the k analogues where the weights are the inverse of the dissimilarities (Simpson 2011). This measure has several attractive features (ter Braak 1995):
1. it is independent of the magnitude of dissimilarity to the \( k \) most similar analogues

2. if the magnitude of the standard error is large relative to the values computed for the modern samples, this indicates that no close modern analogues exist for the fossil assemblage and the climate estimate cannot be trusted

3. the fossil assemblage may be similar to several modern analogues that are very dissimilar in terms of their modern climate, thereby resulting in a high standard error. As a consequence of this multiple analogue situation, the assemblages are not responsive to the climate variable of interest, at least in the region of the climate gradient represented by the fossil sample.

As ter Braak (1995) notes, it can be considered an advantage of MAT that it highlights such problems. MAT is more commonly known in the data-analytical literature as \( k \)-nearest neighbours (ter Braak 1995).Analogue matching (Simpson 2011) is a method in classification (assignment) or discrimination. MAT is also one of several approaches to inverse regression involving non-parametric smoothers (ter Braak 1995). However, it does not fit a global model. Instead it fits a local model to small subsets of the training data for each fossil sample. To be effective MAT therefore requires a good coverage of samples in local space which implies a well-populated network of samples across the climate gradient(s) of interest (Juggins & Birks 2011).

As in all other reconstruction procedures, it is essential that the fossil data-sets used for climate reconstruction are from the same sedimentary environment as the modern training set. The most striking violation of this basic requirement is provided by the recent study of Fletcher et al. (2010) where they use a 3350-sample data-set of terrestrial modern pollen assemblages from a variety of continental sedimentary environments in a MAT-based climate reconstruction for a marine core from the Alboran Sea, despite the well-known differences in taphonomy of terrestrial and marine pollen assemblages. The authors deleted \( Pinus \) from the modern and fossil samples because of its over-representation in marine assemblages. Clearly the resulting climatic reconstructions may be heavily biased by taphonomic differences between marine and terrestrial pollen assemblages and by deletion of the most abundant pollen taxon (see also Dormoy et al. 2009).

In terms of the underlying mathematical properties of MAT and the revised MAT approach of Waelbroeck et al. (1998) that combines MAT with the response-surface method of Bartlein et al. (1986) (the so-called revised analogue method (RAM)), they are inverse reconstruction procedures (ter Braak 1995). They have no assumed underlying linear or unimodal species-environment model, they use full dimensionality (all taxa), and estimate smooth non-parametric local functions rather than parametric global functions, resulting in their inability to extrapolate beyond the range of the modern training set. Although extremely different in their numerical computations and algorithms, artificial neural networks (ANN) have identical mathematical properties when applied to palaeoenvironmental reconstructions. Malmgren and Nordlund (1997), Malmgren et al. (2001), Burrows et al. (2005), and Kucera et al. (2005) describe the use of ANN in marine sea-surface temperature reconstructions; Peyron et al. (1998, 2000, 2005), Tarasov et al. (1999a, 1999b), and Guiot et al. (1996) provide examples of their use with terrestrial pollen data; and Raia et al. (2001; 2003; 2004) discuss ANN applications in palaeolimnology. Telford and Birks (2005) show that in cross-validation tests with a truly independent test-set, MAT and ANN perform poorly as both involve estimating smooth local functions. In practice, ANN appears, in some ways, to be a computationally demanding way of implementing simple MAT! There are several disadvantages to ANN. First, it is difficult to interpret network coefficients in any ecologically meaningful way as ANN is essentially a ‘black box’ tool. Second, artificial neural networks are very flexible and with large numbers of taxa in training sets, they are very prone to overfitting. Telford et al. (2004) and Telford and Birks (2005) show the importance of using, in addition to the training set and an independent test-set, a separate optimisation data-set to optimise the networks based on the training set or to select the optimal number of analogues in MAT and RAM.

There are many examples of the use of MAT for reconstructing Holocene climates from pollen data (e.g. Bartlein & Whitlock 1993; Cheddadi et al. 1998a; Kerwin et al. 2004; Nakagawa et al. 2002; Sawada et al. 2004; Peyron et al. 2005; Ortu et al. 2006, 2008, 2010; Tarasov et al. 2007; Feurdean et al. 2008a, 2008b; Bordon et al. 2009; Kühlt al. 2010). MAT has been extended by Guiot (1990), Guiot et al. (1989; 1992), and Cheddadi et al. (1998b) to reconstruct several climatic variables from pollen assemblages for the last glacial-interglacial cycle using so-called ‘palaeobio-climatic operators’ as weights to emphasise preferentially the climatic signal within fossil pollen data (see below).

A realistic assessment of the ability of MAT, RAM, and ANN (and other calibration-function based reconstruction procedures) to reconstruct modern climate can be made not by simple leave-one-out cross-validation but by the more powerful \( n \)-fold leave-out cross-validation or split-sampling of the modern data-sets \( (X_m, Y_m) \) (Barrows & Juggins 2005). This involves splitting the data into \( n \) (usually 5 or 10) random subsets containing 20% or 10% of the modern data points, respectively. Each subset is removed from the data-set in turn and the remaining modern samples are used to generate reconstruction models that are then applied to the omitted samples. The process is repeated for each subset to give a leave-out climate estimate for each modern sample. This data-splitting procedure is repeated 5 or 10 times, each with random partitions of the modern data to provide a more reliable estimate of the model performance than is provided by simple leave-one-out cross-validation (Barrows & Juggins 2005).

**Response Surfaces**

Before discussing the limitations and inherent problems of MAT (and ANN), we will outline the so-called response-surface approach (Table 1) because, in reality, it is a form of MAT using smoothed modern pollen data rather than the individual pollen assemblages. Response surfaces are three-dimensional graphical representations of the occurrence and/or abundance of individual taxa in modern climate space.
(Huntley 1993). The $x$ and $y$ axes represent climate variables (e.g. mean July temperature, mean January temperature) and the $z$ axis represents the occurrence or relative abundance of the taxon of interest. Such modern taxon-climate response surfaces have been constructed to summarise patterns of modern taxon abundances along major climate gradients. The surfaces have been fitted by multiple regression (e.g. Bartlein et al. 1986), locally weighted regression (e.g. Huntley et al. 1989; Prentice et al. 1991; Bartlein & Whitlock 1993), or generalised additive models (e.g. Smilauer & Birks 1995). Palaeoenvironmental reconstructions (e.g. Webb et al. 1987; 1993a; 1993b; Allen et al. 1995; Watts et al. 1996a; 1996b; Bartlein et al. 1998; Webb et al. 1998; Allen et al. 2000, 2002; Kerwin et al. 2004) are made by ‘stacking’ modern surfaces to produce synthetic modern assemblages for a series of grid nodes, usually 20 x 20 nodes in modern climate space. These synthetic assemblages are then compared to fossil assemblages using a dissimilarity measure, usually the squared chord distance as in MAT. Climate values for the 10 grid nodes with synthetic pollen spectra most similar to the fossil assemblage are then used to infer the past climate. The final inferred value is a mean of the climate variable weighted by the inverse of the squared chord distance (Prentice et al. 1991). Climate reconstructions are thus done by MAT but the modern data consist of fitted or smoothed pollen values in relation to modern climate and not the original pollen values. ter Braak (1995) calls this a ‘smooth response-surface approach via local weighted averaging’. The fitted response-surface values naturally smooth the data to varying degrees depending on the extent of smoothing and procedure used (ter Braak 1995). Much inherent local site-scale variability that is assumed to be unrelated to broad-scale climate patterns is thus removed (Bartlein & Whitlock 1993).

MAT and response surfaces including RAM are widely used with quantitative terrestrial pollen data and with marine fossil assemblages (e.g. Barrows & Juggins 2005; Kucera et al. 2005; Guiot & de Vernal 2007). Thompson et al. (2008) present an ingenious and rigorous use and validation of MAT with qualitative presence/absence data of plant macro-fossils. They applied MAT with four different similarity coefficients to a continental-scale set of modern plant distribution presence/absence data and associated bioclimatic data for North America. For each of 32,211 grid points, they calculated the similarity between the floristic data in the grid point of interest and all other points on the grid (excluding nearby points within 50 km of the grid point of interest to minimise the effects of spatial autocorrelation). The climate of the points with most similar florars was used to estimate the climate at the grid point of interest. They showed the accuracy of the climate estimates is strongly linked to the number of taxa in the target assemblage and like all MAT (and ANN) procedures, it is constrained to produce estimates within the range of observed values. They then applied their MAT procedures to a Last Glacial Maximum plant macro-fossil assemblage from a packrat midden in southern Nevada (Thompson et al. 1999c) to derive estimates of moisture conditions and growing season warmth, and compared the MAT estimates with results from a mutual climate range method (Thompson et al. 1999c). They found that the MAT methods produced more plausible reconstructions of temperature-related variables than moisture-related variables.

Weaknesses

MAT, ANN, and response surfaces suffer from a number of problems (Brewer et al. 2007) including assemblages containing taxa that respond to different environmental variables, the estimation of realistic errors of prediction, fossil assemblages that have no modern analogues or have multiple modern analogues, and assessing model performance realistically because of inherent spatial autocorrelation that all methods using local-estimation procedures such as MAT and ANN are particularly susceptible to. They, like the multivariate calibration-function approach discussed in the next section, are data-demanding techniques in terms of data quality and data quantity. It is particularly important that all the modern and fossil assemblages are from the same sedimentary environment to minimise variation due to taphonomy, basin size, relevant source areas, etc (cf. Fletcher et al. 2010). A further limitation with MAT and related methods is that because they do not assume any response model or have any underlying statistical model or basis, it is not possible to develop model evaluation or diagnostic procedures analogous to regression diagnostics in statistical modelling, nor to have any clear principles of model selection and testing. Unlike methods with a statistical basis and assumed response model, MAT, ANN, etc, have no clear testable assumptions and are thus, in many ways, a ‘black box’, particularly ANN and some variants of MAT. Without an underlying model or statistical basis, it is difficult to develop ‘artificial’ simulated data with realistic assumptions for numerical evaluation experiments (e.g. ter Braak 1995).

In order to deal with the problems of taxa responding to different environmental variables, Guiot (1990) derives ‘palaeo-bioclimatic operators’ to weight preferentially the dissimilarity calculated between the modern and fossil pollen assemblages. An ordination (usually a principal components analysis) is made of all the modern samples, and the distribution of taxa are examined to identify the component axis that is most strongly related to the climatic variable of interest. The taxon scores on this axis are then used as weights. Other variants of these operators or weighting procedures are discussed by Birks (1995).

The error involved in reconstructing climatic values is usually derived from the dispersion of the climatic values of the selected analogues around the weighted average of the climatic value. This approach has the advantage of considering the higher and lower estimates separately, resulting in non-symmetric and possibly more realistic error estimates. However, the total error is underestimated (Brewer et al. 2007). Nakagawa et al. (2002) use a linear relationship calculated between observed and estimated climate values at modern pollen sites. The confidence intervals for this linear relation are then applied to derive probability distributions and/or confidence intervals for the estimates of past climate. This procedure needs a dense network of modern climate stations. Potentially the most reliable procedure for error estimation in MAT is bootstrapping (Simpson 2011) to derive sample-specific error estimates for past climate. However, the reliability of such bootstrap estimates in MAT in the presence of spatial autocorrelation has not yet been investigated.
A very significant problem for MAT and related methods including ANN, is situations where no good modern analogues can be found for a fossil assemblage (e.g. Ortu et al. 2006, 2010; Minckley et al. 2008). Such non-analogue situations can result from, for example, unique biotic interactions, vegetation dynamics, novel climates (low CO₂ concentrations, unique combinations of summer and winter irradiance), anthropogenic influence, and lack of modern samples (Jackson & Williams 2004). A critical question therefore is what is a ‘good analogue’ and what is a non-analogue. Definitions are difficult and involve total taxonomic composition, the relative abundance of the numerical dominants, the identification of specialists and generalists, and life-forms and functional types. These biological attributes are not easy to measure and even more difficult to summarise in a single dissimilarity or analogue measure (Juggins & Birks 2011).

Davis et al. (2003) (see also Davis & Brewer 2009) modified the MAT approach to help circumvent the non-analogue problem. They grouped the modern and fossil pollen taxa into plant functional types (PFTs) that are broad classes of plants defined by stature, life-form, phytology, physiology, leaf-form, and climatic tolerances (Duckworth et al. 2000). Analogue matching was carried out on the basis of the PFT abundances. As each PFT represents a set of ecologically similar taxa (Prentice et al. 1996), the assumption is made that a similar climate will always support a similar composition of PFTs, even if the actual species composition within a PFT may vary for non-climatic reasons (Brewer et al. 2007). This approach of grouping pollen taxa into PFTs has also been used by Peyron et al. (1998) and Tarasov et al. (1999a, 1999b) in their reconstructions of Europe and Eurasia during the Last Glacial Maximum (see also Peyron et al. 2000) and at 6000 BP, and, rather surprisingly, in reconstructions of late-Holocene climate by Kühl et al. (2010). Because of the large climatic amplitudes of many PFTs, this approach can lead to very large reconstruction errors, for example of 5-10°C for annual mean temperature.

An ingenious approach to trying to cope with the non-analogue problem is to construct so-called expanded response-surfaces (Gonzales et al. 2009b). The method assumes that pollen taxon abundances follow a symmetrical unimodal distribution along climatic gradients, that taxa with truncated distributions in modern climate space occupy a subset of their fundamental or potential niche, and thus the truncated distributions can simply be expanded by mirroring around the distributional mode to recover the portion of the potential niche not realised today in modern climate space (Gonzales et al. 2009b). This approach should usefully be compared with conventional and more rigorous statistical modelling of taxon responses in relation to climate by generalised linear (ter Braak & Looman 1987) or generalised additive modelling (Yee & Mitchell 1991), both of which allow some degree of extrapolation.

A further problem in the general MAT approach is the existence of multiple analogues (Huntley 1996, 2001). These arise when the fossil assemblage is similar to several modern samples that differ widely in their modern climate. For example, modern assemblages dominated by Pinus pollen can be derived from northern, central, or Mediterranean Europe, all of which have very different climates today (ter Braak et al. 1996; Birks 1998). Clearly in these circumstances, the MAT approach will provide unreliable and ambiguous reconstructions. To help circumvent this problem, information from a second climate proxy has been used to constrain the climatic reconstruction. Cheddadi et al. (1997) reconstructed past climate from pollen data using MAT constrained by palaeolake-level data. The constraint consists of restricting the set of modern pollen samples considered as analogues for the fossil samples to those locations where the implied change in annual precipitation minus evapotranspiration (P-E) is consistent with the regional change in moisture balance as indicated by the palaeolake-level data. This constraint led to an improvement in the spatial coherency of the reconstructed palaeoclimate anomalies, particularly (and not surprisingly) for P-E (Brewer et al. 2007). Other proxies used as constraints have included biome reconstructions derived from assemblages of plant macrofossils or fossil pollen (e.g. Magny et al. 2001, 2003; Ortu et al., 2006, 2010), beetle-based climate reconstructions, and sedimentary parameters (see Birks 1995 for a review). The use of certain proxies as a constraint has the disadvantage that these proxies can no longer be used to verify independently the reconstruction results (Brewer et al. 2007). However, if the climate response of the proxy is well understood, the use of a constraint may provide a more consistent set of results than those from an unconstrained MAT (e.g. Magny et al. 2001, 2003; Muller et al. 2003; Bordon et al. 2009). The need of using such constraints raises questions about the suitability and robustness of MAT as a climate-reconstruction procedure when applied to pollen data, especially when the constraints applied are themselves derived from the pollen data (e.g. biomes).

Spatial Autocorrelation

The problem of spatial autocorrelation (Legendre 1993) in modern assemblage and associated environmental datasets and its influence on the performance of environmental reconstruction techniques, both the assemblage approach and the multivariate calibration-function approach (see next section) has, until recently (Telford & Birks 2005; 2009), been ignored. Cross-validation (leave-one-out, split-sampling into a training or calibration data-set and a test-set, and bootstrapping) assumes statistical independence of samples, an assumption that is violated in the presence of spatial autocorrelation (Legendre 1993), leading to over-optimistic estimates of RMSEP and other model performance statistics.

Telford and Birks (2005), using an extensive modern foraminiferal assemblage data-set from the Atlantic showed that MAT (and ANN – see also Telford et al. (2004)) utilises spatial structure in the assemblage data that is uncorrelated with the environmental variable being modelled and thus improves the apparent predictive-model abilities of MAT and ANN. This residual structure is likely to be related to spatial structures in environmental variables other than the one being reconstructed (see Telford 2006). When a spatially independent test-set (e.g. South Atlantic) is used to assess the MAT and ANN model performances when the calibration data-set is from the North Atlantic, MAT and ANN perform no better than standard calibration-function methods such as two-way weighted averaging (see The Multivariate Calibration-Function Approach), suggesting that previously
reported MAT and ANN model performance statistics in the palaeoceanographic literature are over-optimistic (Telford et al. 2004). These findings highlight that spatial autocorrelation is a problem in the assemblage approach to environmental reconstruction when the environmental variable(s) of interest is spatially smooth and where reconstruction methods such as MAT and ANN involve local non-parametric estimation of functions rather than global parametric estimation as in two-way weighted averaging.

The extent to which spatial autocorrelation affects other environmental variables and other proxies has been addressed by Telford and Birks (2009). In modern data-sets with strong spatial autocorrelation (e.g. pollen and July sunshine, planktonic foraminifera and summer sea-surface temperature, benthic foraminifera and salinity), MAT generally outperforms other reconstruction techniques, whereas MAT underperforms with data-sets with weak spatial autocorrelation (e.g. diatoms and lake-water pH). The most likely explanation for this behaviour is that MAT finds a fit between the species assemblages and the environment that is local rather than global, and as a result MAT is not robust to the presence of spatial autocorrelation. In light of these results, Telford and Birks (2009) recommend that MAT not be used with modern data-sets where strong spatial autocorrelation is present despite its widespread use in marine studies (Guio & de Vernal 2007) and terrestrial pollen-analytical studies (Williams & Shuman 2008).

Telford and Birks (2009) present two simple means for evaluating the influence of spatial autocorrelation on the performance of environmental-inference models. The first is simply to delete samples at random and derive modern performance statistics (RMSEP, etc.) for different sized modern data-sets. Samples are also deleted that are geographically close to the test sample and performance statistics for both types of deletion are calculated and compared. If strong spatial autocorrelation is present, deleting geographically close samples will preferentially delete the most similar samples. Because of spatial autocorrelation these close samples will bias inferences and lead to seemingly ‘good’ performance of the reconstruction model. Thus their deletion should drastically decrease model performance. In contrast, random deletion should have much less impact on model performance. The second method involves $h$-block cross-validation and provides a means of evaluating a reconstruction model in the presence of spatial autocorrelation. In time-series analysis, $h$-block cross-validation involves deleting an observation from a model set along with $h$ observations on either side to minimise the effects of temporal autocorrelation (Borman et al. 1994). The idea has been extended to spatial autocorrelation (Telford & Birks 2009) by defining radius $h$ based on the range of a geostatistical variogram of the model residuals from the basic reconstruction model. RMSEP and related model statistics are calculated for $h$-block cross-validation and compared with the same statistics based on simple leave-one-out cross-validation. Telford and Birks (2009) showed a consistent increase (up to 230%) in RMSEP in $h$-block cross-validation using MAT with modern assemblage data-sets with high spatial autocorrelation.

Despite this work, some investigators claim that spatial autocorrelation does not bias MAT models (e.g. Guio & de Vernal 2007; Fréchette et al. 2008; Bonnet et al. 2010). The basis for this claim is generally to select at random a test-set (e.g. 10% or 20% of the modern data) and to estimate RMSEP for this test-set. In this procedure, the test-set samples are not spatially and hence not statistically independent and so cannot be used to test correctly for the influence of spatial autocorrelation. To do this appropriately, the test-set must be spatially independent from the calibration data-set (e.g. Telford & Birks 2005). However, using spatially independent test-sets is rarely possible, so the two procedures of Telford and Birks (2009) outlined above should be used to test for the influence of spatial autocorrelation on the performance of MAT and ANN when applied to spatially structured assemblage data-sets.

Biogeographers and ecologists are also beginning to wrestle with the very real problems of spatial autocorrelation in the numerical analysis of modern species distribution data (e.g. Lichstein et al. 2002; Araújo et al. 2005; Betts et al. 2006; Rangel et al. 2006; Dormann et al. 2007; Dormann 2007a, 2007b, 2007c; Beale et al. 2010). As in palaeoecology, there is currently a lively debate about the need or otherwise to account for the effects of spatial autocorrelation (e.g. Lennon 2000; Betts et al. 2006, 2009; Beale et al. 2007, 2010; Hawkins et al. 2007; Bini et al. 2009; Dormann 2009; de Knept et al. 2010) in bioclimate-envelope modelling and other forms of species distribution modelling.

Despite the long tradition in biogeography of species-climate modelling and analysis, this has almost exclusively involved individual species responses (e.g. Elith & Leathwick 2009; Franklin 2010). Recently, biogeographers (Baselga & Araújo 2009, 2010) are considering species assemblages in relation to climate variables to predict assemblage dynamics under future climates using the recently developed technique of canonical quadratic ordination (Yee 2004, 2006). Other predictions of future assemblage change include Hamann and Wang (2006) and Rehfeldt et al. (2006).

As in the indicator-species approach, there are increasingly close research parallels between the palaeoecological community on the one hand, and the ecological and biogeo graphical communities using the assemblage approach on the other. Both research communities should be aware of current trends within both research communities as there is likely to be much of relevance to each research community.

THE MULTIVARIATE CALIBRATION-FUNCTION APPROACH

The third approach to palaeoclimate reconstruction is the multivariate approach involving calibration functions. This approach involves underlying statistical models with global estimation of parametric functions for all the taxa present. This allows, to some degree, some extrapolation (ter Braak et al. 1993; ter Braak 1995) and helps to overcome some of the problems inherent in the assemblage approach.

The basic idea of quantitative climate reconstructions involving multivariate calibration functions (Table 1) is summarised in Figs. (1 and 2). As with the indicator-species and assemblage approaches, it assumes that there is one or more climate variable(s) ($X_i$) to be reconstructed from fossil
biotic assemblages \((Y_i)\) consisting of \(m\) taxa in \(n\) samples. To estimate or reconstruct \(X_t\), we need to model numerically the responses of the same \(m\) taxa today in relation to modern climate variable(s) \((X_m)\). This requires a modern ‘training set’ or ‘calibration set’ of \(m\) taxa at \(f\) sites or modern samples \((Y_m)\) studied as assemblages preserved in modern surface sediments (e.g. surface (0-1 cm) lake muds) with associated modern climate variables \((X_m)\) for the same \(f\) modern sites or samples. The modern relationships between \(Y_m\) and \(X_m\) are modelled numerically by some form of regression analysis and the resulting calibration function is then used to transform the fossil data \((X_i)\) into quantitative estimates of the past climate variable(s) \((Y_i)\).

Since Imbrie and Kipp (1971) revolutionised Quaternary palaeoclimatology by presenting, for the first time, a numerical procedure (principal components regression) for quantitatively reconstructing past environments (in their case sea-surface summer and winter temperatures and salinity) from fossil foraminiferal assemblages, several numerical techniques have been developed for deriving multivariate calibration functions (see Birks 1995; ter Braak 1995; Birks 1998; Guiot & de Vernal 2007; Juggins & Birks 2011 for reviews).

Basic Considerations

There are four basic considerations when deriving multivariate calibration functions (ter Braak 1995). First, there is the choice between classical and inverse regression approaches. The classical approach is of the general form:

\[
Y_m = f(X_m) + \text{error}
\]

The function \(f(\cdot)\) is estimated by linear or non-linear multivariate regression from the modern training set \((X_m, Y_m)\). The estimate of \(f(\cdot)\) is then ‘inverted’ to infer the past climate \(X_f\) from \(Y_f\):

\[
X_f = f^{-1}(Y_f)
\]

‘Inversion’ involves finding the past climate variable that maximises the likelihood of observing the fossil assemblages in that climate. If the function \(f(\cdot)\) is non-linear, which it almost always is, non-linear optimisation procedures are required and these can raise programming problems (Birks 2001).

Alternatively there is the simpler but ecologically slightly curious inverse approach of:

\[
X_m = q(Y_m) + \text{error}
\]

where the difficult inversion step is avoided by estimating directly the function \(q(\cdot)\) from the training set by inverse regression of \(X_m\) on \(Y_m\), in contrast to the classical approach where \(Y_m\) is regressed on \(X_m\). The inferred past climate \((X_i)\), given a fossil assemblage of \(Y_i\), is simply:

\[
X_i = q(Y_i)
\]

Statisticians have debated the relative merits of the classical and inverse approaches (ter Braak 1995). In practice, inverse models nearly always perform as well as classical methods. Inverse models appear to perform best if the fossil assemblages are similar in composition to samples in the central part of the modern training data, whereas classical methods may be better at the extremes and under some extrapolation as in non-analogue situations (Birks 1998).

Second, there is the question of an assumed species-response model. Some climate reconstruction procedures (e.g. MAT, ANN – see above) have no underlying assumed species response model. Multivariate calibration-function approaches assume either linear or unimodal species-environment responses (Birks 1995). It is a general law of nature that organism-environment relationships are non-linear and taxon abundance is usually a unimodal function of the environmental variable (ter Braak 1996). Each taxon grows best or is most competitive at a particular optimal value of that variable and cannot survive or is less competitive where the value of that variable is too low or too high (ter Braak 1996). Thus all taxa tend to occur over a characteristic but limited environmental range and within this range to be most abundant at or near their environmental optima (see Whittaker (1956, 1967) and Odum (1971) for further discussions of the unimodal species response model in ecology). Although species responses may be more complex than implied by the unimodal model, this model is nevertheless useful in developing numerical descriptive techniques for data showing mostly unimodal responses, just as linear models are useful in developing numerical descriptive techniques for data that are only approximately linear (ter Braak & Prentice 1988). Modern pollen data collected over a continental or sub-continental scale covering broad climate gradients (e.g. Williams et al. 2006) may show complex multimodal responses (Birks & Telford 2006). An additional problem associated with such data-sets includes the existence of multiple analogues, as discussed under The Assemblage Approach.

Third, there is the question of model dimensionality. Should all taxa be considered individually (full dimensionality) or should some axes or numerical combinations of taxa (e.g. principal components, correspondence analysis axes, partial least squares (PLS) components, weighted averaging PLS components) (reduced dimensionality) be used?

Fourth, there is the estimation procedure to consider. Should a global estimation procedure be used that estimates parametric functions such as taxa optima across the complete modern training set and thus allows some extrapolation, or should a local estimation procedure be adopted that estimates non-parametric local functions that do not allow any extrapolation?

The two multivariate calibration-function techniques that we will discuss here (two-way weighted averaging (WA) regression and calibration and weighted averaging partial least squares (WA-PLS) regression and calibration) both assume a unimodal organism-environmental response model, involve global parametric estimation, and are inverse regression procedures. They differ in using full dimensionality (WA) and reduced dimensionality (WA-PLS).

Our experience with a wide range of data-sets from many different environments suggest that there are good reasons for favouring methods with an assumed taxon response model and global parametric estimation. These include:

1. It is possible to test if a taxon has a statistically significant relationship to a particular climate variable by some form of linear or non-linear regression ana-
lysis (e.g. Lotter et al. 1997, 1998; Seppä et al. 2004; Tonello et al. 2009; Herzschuh & Birks 2010).

2. It is possible to generate ‘artificial’ simulated data under realistic ecological assumptions and with known numerical properties for comparative experiments on model performance (e.g. ter Braak & Juggins 1993; ter Braak et al. 1993; ter Braak 1995).

3. Models with assumed response models and involving global estimation procedures have clear and testable assumptions and are less of a ‘black box’ than, for example, artificial neural networks (Telford et al. 2004; Telford & Birks 2005).

4. It is possible to develop model evaluation or diagnostic procedures analogous to regression diagnostics in statistical modelling (e.g. Birks et al. 1990; Birks 1995; 1998).

5. As such methods have an underlying statistical basis, it is possible to adopt the well-established principles of statistical model selection and testing (e.g. minimal adequate model, maximum numbers of degrees of freedom, principle of parsimony) in calibration-function methodology, thereby minimising ‘ad hoc’ aspects of selecting, for example, taxon weighting functions in modern analogue procedures (Birks 1995; 1998).

6. It appears from recent work that methods involving the estimation of global parametric functions are more robust to problems of spatial autocorrelation (Telford & Birks 2005; 2009) than methods that involve local non-parametric estimation.

It is more difficult to present reasons for favouring classical or inverse approaches, as discussed above. The main reason for favouring methods that use full dimensionality is, as we will discuss later, that they are easier to fit and there is less danger of ‘overfitting’, which can easily occur in methods that can involve many PLS components unless the user is aware of the dangers of overfitting in statistical modelling and of the need to develop a ‘minimal adequate model’ (Birks 1998).

Weighted Averaging and Weighted Averaging Partial Least Squares – Strengths and Weaknesses

The basic idea behind two-way weighted averaging (WA) (ter Braak & van Dam 1989; Birks et al. 1990; ter Braak 1996) is that if a taxon shows a unimodal relationship with a particular climate variable, its abundance will tend to be highest at sites with values of x close to the taxon’s environmental optimum or niche peak. A simple and ecologically realistic estimate of the taxon’s optimum for x is thus the average of all the x values for sites at which the taxon occurs, weighted by the taxon’s relative abundance. The estimated optimum is the abundance-weighted average of x (WA regression). Taxon absences have no weight and are thus disregarded. An estimate of a site’s value for climate variable x is the weighted average of the optima for x for all the taxa present (WA calibration). The underlying theory of WA and the conditions under which it approximates the theoretically more rigorous Gaussian logit regression and calibration are discussed by ter Braak and Barendregt (1986), ter Braak and Looman (1986), and ter Braak (1996). WA has gained considerable popularity in many branches of Quaternary palaeoecology in the last two decades for several reasons (Birks 1998).

1. It combines ecological realism (unimodal taxon responses and the species-packing model) with mathematical and computational simplicity, sound underlying ecological and statistical theory, and good empirical power.

2. It does not assume linear taxon-environment responses, it is relatively insensitive to outliers, and, perhaps surprisingly, it is not hindered by the high inherent correlations between taxa whose abundances are expressed as ‘closed’ percentages or by the large numbers of taxa in training sets (Ym) (Birks 1994).

3. Because of its computational simplicity, it is possible to use computer-intensive boot-strapping to derive sample-specific root mean square errors of prediction (RMSEP) for all estimates of the past climate (Xf) (Birks et al. 1990).

4. WA performs well in ‘non-analogue’ situations (Hutson 1977; ter Braak et al. 1993). In such situations, environmental reconstructions are based on the WA of the optima of the taxa in common between the modern (Ym) and the fossil (Yf) assemblages. As long as we have reliable estimates of the optima for the fossil taxa with high numerical importance, WA inferences are often relatively robust. This is why WA resembles more a multivariate indicator-species approach in which the indicative values of individual taxa are weighted by their abundances than a modern analogue procedure.

5. Because WA estimates global parameters for all taxa across the full sampled climate gradient (Xm), it only models the variance in Ym that is correlated with Xm. It is therefore relatively robust to any spatial structure in the modern data, unlike the modern analogue technique and artificial neural networks (see above).

6. Many studies have shown that WA consistently performs well with noisy, taxon-rich compositional data with many taxa absent from many samples and extending over a relatively long climate gradient.

7. WA is relatively robust to violations of the underlying assumptions of a unimodal species-climate response (ter Braak & Verdonschot 1995; ter Braak 1996)

WA does, however, have three important potential weaknesses (ter Braak & Juggins 1993).

1. WA is sensitive to the distribution of samples within the modern training set along the climate gradient of interest (ter Braak & Looman 1986). With large datasets (>400 samples), WA has been shown to be surprisingly robust to this distributional requirement (Ginn et al. 2007).

2. WA ignores residual correlations in the modern biological data, namely correlations that remain in the
biological data after fitting the climate variable of interest. These residual correlations result from environmental variables not considered directly in WA.

3. WA suffers from ‘edge effects’ that lead to non-linear distortions at the gradient lengths. This problem is particularly acute for training sets with a long single dominant gradient and high compositional turnover. It leads to an overestimation of optima at the low end of the gradient and an underestimation at the high end. This in turn leads to biases in the inferred values (ter Braak & Juggins 1993).

The incorporation of partial least squares (PLS) regression (Martens & Næs 1989) into WA to create WA-PLS (ter Braak & Juggins 1993) helps to overcome, in part at least, the second weakness of WA by utilising residual correlations to improve the estimates of taxon climate parameters and the third weakness, namely the ‘edge-effect’ problem.

ter Braak and Juggins (1993), ter Braak et al. (1993), ter Braak (1995), and Birks (1995; 1998) describe the mathematical basis of WA-PLS and this is not repeated here. The main advantage of WA-PLS is that it often, but not always, produces calibration-function models with lower RMSEP and bias than simple two-way WA. There are two possible reasons for this improved performance.

1. WA-PLS reduces the ‘edge-effect’ problem. Due to the ‘edge effect’ in WA, there is not only a bias in the inferred values of the climate variable but also in the model residuals at the ends of the gradients. WA-PLS implicitly involves a weighted inverse deshrinking regression that pulls the inferred values towards the training-set mean. WA-PLS utilises both patterns in the residuals to update the calibration function, thereby reducing errors, and patterns in the systematic bias to reduce, to some extent, the ‘edge-effect’ problem.

2. In real life, there are often additional environmental variables that may influence the biological assemblages. WA ignores any structure resulting from these variables and assumes that environmental variables other than the one of interest have negligible influence, or that their joint distribution with the climate variable of interest in the past is the same as today (assumption 5 above). WA-PLS uses this additional structure to try to improve estimates of the taxon parameters in the final calibration function. For optimal performance, the joint distribution of these environmental variables in the past should be the same as in the modern data (ter Braak & Juggins 1993).

The main disadvantage of WA-PLS compared to WA is that great care is needed in model selection. As more components are added, the WA-PLS model appears to fit the modern data better and better as the model error decreases and becomes 0 when the number of components fitted equals the number of samples. Such a model, the so-called full model, has zero predictive power as it has no degrees of freedom. An independent test-set is needed to evaluate different WA-PLS models based on 1, 2, ..., $n$ components where $n$ is usually 4-10, and thus to find the optimal model with the lowest prediction error and bias for the test-set. In practice, there are usually no independent test-sets and WA-PLS model evaluation has to be based on cross-validation to derive approximate estimates of model performance. The final WA-PLS model to use in climate reconstruction is selected on the basis of low RMSEP, low bias, and a small number of ‘useful’ components (‘minimal adequate model’) (Birks 1998). In some cases, the number of ‘useful’ components (defined by Birks (1998) as giving $>5\%$ reduction in the RMSEP of the one-component WA-PLS model) does not guard against selecting an overfitted model. A simple solution to avoid overfitting is to use van der Voet’s (1994) randomisation t-test to test the equality of predictions from two transfer-function models (see Racca et al. (2001) and Velle et al. (2011) for applications of this test). Sample-specific prediction errors for past climate variables can be estimated by Monte Carlo simulation or by bootstrapping (Birks et al. 1990; Birks 1995, 1998).

A further problem with WA-PLS is that as it exploits residual structure in the data, which is often related to the effects of environmental variables other than the one of interest. WA-PLS can, in theory, be more susceptible to biases related to different covariations of environmental variables in the past than occur in the modern training set. It is not uncommon to find discrepancies between reconstructions based on WA-PLS when two or three components are used, even though the ‘optimal’ model (based on model performance statistics) suggest a two- or three-component model is appropriate. It is also important that the residual structure used by WA-PLS is ecologically useful. We have worked with several pollen and chironomid data-sets for which additional WA-PLS components improved the performance statistics of the modern training set but when these additional components are applied to fossil stratigraphic data, the components simply increase the noise in the structure without showing more climatically-relevant structure or strengthening the signal relative to the noise in the reconstruction.

Examples of situations in which WA-PLS may lead to misleading results are training sets in which the relationship between climate and modern proxy-data is affected by non-climatic processes acting to different extents along the observed environmental gradients. For example, it is very likely that the strong relationship observed between chironomid assemblages and summer temperature is mediated and reinforced to a significant extent by climate effects on water chemistry parameters (e.g. nutrient and oxygen concentrations) (Brodersen & Quinlan 2006; Velle et al. 2010; Verbruggen et al. 2010). If, in modern training sets, these water chemistry parameters are affected in parts of the gradient by processes unrelated to climate, such as human activity or acidification, it is possible that WA-PLS will correct for any resulting offset in inferred values within a developed chironomid-based calibration function for temperature. However, this would result in a correction of an offset that is unrelated to climatic effects on chironomid assemblages and could potentially lead to a bias in the reconstructions obtained from fossil assemblages unaffected by confounding factors important in the modern training set. Other examples of potentially problematic situations for
WA-PLS might include training sets in which the relationship between an environmental parameter and assemblage data is driven by different seasonal components of the parameter of interest in different parts of the observed environmental gradient (e.g., winter temperature versus summer temperature as a dominant parameter affecting plant assemblages in different climatic conditions) or training sets in which the environmental gradient of interest covers major transitions in bedrock type which might influence species distributions (e.g., calcareous versus non-calcareous bedrock).

In a series of numerical experiments using a 191- and 310-sample modern pollen-climate data set from Norway, northern Sweden, and Svalbard, Bjune et al. (2010) showed that WA-PLS model performance statistics were only slightly improved by increasing the size of the training set. However, an important result was that down-core reconstructions of mean July temperature showed much less sample-to-sample variation ("noise") when the larger training set was used. This emphasizes the importance of considering not only modern model statistics but also the resulting climate reconstructions.

Our general experience is that all model performance statistics are only a rough guide to model selection. The problem is that all these performance statistics are based on predicting temperature from modern assemblages with known climate. The statistics do not indicate how reliable the models are when they are applied to fossil assemblages where the past climate is not known. Some careful and critical two-way interaction is needed between assessing modern model performance statistics and the resulting down-core reconstruction (see Velle et al. 2010).

Like WA, WA-PLS performs surprisingly well and considerably better than modern analogue procedures when none of the fossil assemblages are similar to the modern assemblages (ter Braak et al. 1993; ter Braak 1995). For very strong extrapolation beyond the modern training set, WA often performs better than WA-PLS. Like WA, WA-PLS is a weighted multivariate indicator-species approach but where all taxa are used in the reconstruction and estimates of the relevant taxon parameters are derived from the modern training data rather than from modern autocorrelation or biogeographical data. Telford and Birks (2005) show that, unlike WA, WA-PLS can produce biased results and overly optimistic prediction errors in the presence of strong spatial autocorrelation. This occurs because, besides reducing the predictive error by reducing the ‘edge-effects’ inherent in WA, WA-PLS may acquire residual variation in certain parts of the environmental gradient that can be spatially autocorrelated to the climate variable of interest.

One approach to eliminate the problem of model selection and model overfitting in WA-PLS and to reduce the ‘edge-effects’ of WA is to use a monotonic smoothing spline (Wold 1992; ter Braak & Juggins 1993; Telford et al. in prep) rather than the conventional linear inverse or classical deshrinking regression in WA (Birks et al. 1990; Birks 1995). Comparisons using several diatom-environment data sets (Telford et al. in prep) indicate that a simple WA model with a monotonic spline often has the best predictive power, and produces the simplest model (‘minimal adequate model’) in terms of number of parameters to estimate and to fit.

Modern Ecological Applications of Multivariate Calibration Functions

In the previous sections, we have seen how palaeo-ecologists, ecologists, and biogeographers are independently considering the same or related problems in the indicator-species approach and the assemblage approach. Is there a similar parallelism in the multivariate calibration-function approach? The answer is yes.

Plant ecologists have long been using modern plant assemblages as a basis for assessing modern environmental conditions, so-called bio-indication, by means of ecological indicator values (e.g., Ellenberg 1948; Ellenberg et al. 1992). Ordinal environmental indicator values (‘optima’) for the central European flora (Ellenberg et al. 1992) and the western European flora (Hill et al. 2000; 2004; 2007) have been estimated on the basis of field, laboratory, and phytosociological studies for light, moisture, soil reaction, nitrogen, temperature, and salt tolerance. Given a modern assemblage, the environmental value of the sites is inferred to be the average of the species indicator values (if presence/absence data only are available) or the abundance-weighted average of the indicator values if quantitative abundance data are available. Similar index-based approaches have been developed and are widely used for biomonitoring of freshwater ecosystems. Examples include the Benthic Quality Index (Wiederholm 1980) based on abundance-weighted averages of indicator values for selected chironomid species or abundance-weighted indices reflecting past and present water quality based on diatom assemblages (e.g., Renberg & Hellberg 1982). Diekmann (2003) provides a thorough review of species indicator values as a tool in applied ecology, and additional excellent examples of their use include Dzvonko (2001), Hawkes et al. (1997), Hill and Carey (1997), and Holttand et al. (2010). The underlying mathematical basis for the use of indicator values is outlined by ter Braak and Barendregt (1986) and ter Braak and Gremmen (1987).

Recently, Brady et al. (2010) have used exactly the same multivariate calibration-function approach in palaeoclimatology of WA-PLS to develop modern climate-plant calibration functions based on 107 forest plots in Oregon and Washington. Their aim is to revisit and record the plots in the future and to use their modern calibration function to infer what climatic changes there have been. Such an approach could be of great value in remote arctic or alpine areas where there are very few meteorological stations. However, developing a modern calibration function in such areas is not possible without reliable climate data. It will be interesting to see, under conditions of future climate change, how robust and how useful the approach of Brady et al. (2010) will be.

We now turn to topics common to all approaches – presentation and interpretation, evaluation and validation, comparisons, and general limitations of climate reconstructions. In addition we discuss future developments and challenges.
PRESENTATION AND INTERPRETATION OF CLIMATE RECONSTRUCTIONS

In palaeoclimatology, it is common to present reconstructions or model hindcasts as climate ‘anomalies’ or ‘deviations’ from present-day values (e.g. $\Delta = -1.5^\circ\text{C}, \Delta = 2.1^\circ\text{C}$). There are several options in the presentation of climate reconstructions based on biological assemblages using the three main approaches described above:

1. as the inferred or reconstructed value in °C, mm of precipitation, etc (e.g. Seppä & Birks 2001)
2. as deviations (Δ) from the observed present-day value at the study site
3. as deviations (Δ) from the inferred present-day value at the study site (Heikkilä & Seppä 2010)
4. as deviations (Δ) from the mean of all reconstructed values for the last 100, 200, or 250 years (e.g. Heikkilä & Seppä 2003; Seppä & Poska 2004), or
5. as deviations (Δ) (possibly standardised to unit variance, so-called ‘z-scores’) from the mean of all reconstructed values for the sequence under study (Osborn & Briffa 2006).

Despite the considerable advances in techniques for reconstructing past climate from fossil assemblages, much work is needed on how to present optimally reconstructed climate temporal-series and how to detect consistent trends and patterns within and between such temporal-series (Birks & Seppä 2004). The simple threshold-count approach of Osborn and Briffa (2006) is a promising and robust procedure for comparing different climatic temporal-series after standardisation.

Expression of reconstructions as deviations from the modern inferred values may have the advantage that the deviations accurately reflect past changes in temperature even when absolute inferences are consistently too high or too low. This may be the case if the local thermal regime in a region or ecosystem is not adequately reflected by or in equilibrium with the thermal variable that is reconstructed. Examples are reconstructions of past air temperature based on lacustrine proxy-indicators (e.g. chironomids, diatoms, cladocerans) from lakes which receive considerable amounts of cool water via tributaries, pollen-based reconstructions from landscapes affected by higher or lower than expected insolation (e.g. south- or north-facing slopes) or, for WA and WA-based methods, reconstructions which infer values close to the edges of the examined temperature gradient and are therefore potentially affected by ‘edge effects’.

Despite considerable advances in multivariate calibration-function methodology and in developing organism-climate training sets, our abilities to interpret and compare time-series of palaeoclimate reconstructions have hardly developed beyond visual comparison of time-series. Willis et al. (2007) illustrate a statistically rigorous way of comparing two or more palaeoecological biological and environmental time-series using auto-regressive procedures.

Although it is possible, thanks to improved computing power and efficient programming, to derive sample-specific errors of prediction for climate reconstructions based on WA or WA-PLS using computer-intensive bootstrapping procedures, an unresolved problem is how to interpret such errors. All stratigraphical data and resulting reconstructions exhibit strong temporal autocorrelation and thus adjacent samples and their reconstructed values of Xt are not independent of each other statistically. Related to this problem is our limited ability to compare rigorously temporal series of environmental reconstructions, again because of the statistical problems created by temporal autocorrelation (Clarke 1989).

All biostratigraphical data and hence all climate reconstructions which are, in reality, a transformation (admittedly in many cases a complex, non-linear transformation) of the original stratigraphical data are rather ‘noisy’ due, in part, to the inherent sample-to-sample variation in the biostratigraphical data. Non-parametric regression such as locally weighted regression smoothers (LOESS) provide useful graphical tools for highlighting ‘signal’ or major patterns in temporal series of reconstructed climate variables (Birks 1998). LOESS (Cleveland 1993) models the relationship between a response or dependent variable (e.g. pollen-inferred July temperature) and a predictor or independent variable (e.g. age) when no single functional a priori form, such as a linear or quadratic model, is appropriate. LOESS provides a robust graphical summary that helps assess the relationship and detects major trends within ‘noisy’ data such as climate reconstructions. LOESS can also be used to produce a ‘consensus’ reconstruction based on several reconstructions (e.g. different transfer-function models, different data-sets, different records, different proxies) (Birks 1998). More sophisticated smoothers such as SiZer (significance of zero crossing of the derivative) (Chaudhuri & Marron 1999; Holmström & Erästö 2002) and the related BSiZer (Erästö & Holmström 2005) have considerable potential in palaeoclimatology because they can assess which features seen in a range of smoothed data are statistically significant and thus may be environmentally significant (see Korhola et al. 2000; Erästö & Holmström 2005, 2006; Weckström et al. 2006 for palaeoecological applications). Given the random walk simulations of pollen data presented by Blaauw et al. (2010), there is an increasing need to use techniques such as SiZer or BSiZer to distinguish signal from random red noise in stratigraphical time-series.

EVALUATION AND VALIDATION OF CLIMATE RECONSTRUCTIONS

Evaluation and validation of palaeoecological climate reconstructions receive surprisingly little attention. They are extremely important, as all reconstruction procedures will provide results irrespective of which method or approach is used. The critical question is how reliable are these results?

There are two general approaches – numerical evaluation using reconstruction diagnostic statistics and validation using historical data and instrumental records or independent palaeoclimatic data. In terms of numerical evaluation there are four useful numerical criteria (Birks 1998; Birks 2003; Juggins & Birks 2011). These are only applicable to the assemblage and the calibration-function approaches.

1. Sample-specific RMSEP for individual fossil samples (Birks et al. 1990).
2. ‘Goodness-of-fit’ statistics assessed by fitting fossil samples ‘passively’ onto the first axis of an ordination of the modern training data constrained by the climate variable being reconstructed and evaluating how well individual fossil samples fit onto this constrained axis in terms of their squared residual distance (Birks et al. 1990).

3. Analogue measures for each individual fossil sample in comparison with the modern training set (Simpson 2007, 2011). A reconstructed climate variable is likely to be more reliable if the fossil sample has modern analogues within the training set (ter Braak 1995).

4. The percentages of the total fossil assemblage $Y_t$ that consist of taxa that (a) are not represented at all in the training set $Y_m$ or (b) are poorly represented (e.g. only present at low abundance, only present in a few samples) in the training set. Parameters summarising the ecology of these taxa (e.g. WA optima) are more likely to be poorly estimated and have large standard errors associated with them in cross-validation (Birks 1998).

Bigler et al. (2002), Heiri et al. (2007) Engels et al. (2008, 2010), and Lotter et al. (2011) illustrate the use of these numerical evaluation criteria in studies on climate change using a range of proxies. These numerical criteria are, however, only a guide to the possible reliability of the reconstructions. Even samples with poor evaluation statistics (e.g. no close analogues, a poor fit with the climate variable of interest) may yield accurate reconstructed values, whereas samples with favourable evaluation statistics may be biased, for example if the basic assumptions behind the numerical method used are violated or if the biological system of interest is strongly influenced by environmental or biotic variables unrelated to climate. Examples of palaeoecological reconstructions yielding results in agreement with independent climate records even in instances where evaluation statistics indicate a poor fit with temperature and no close or good analogues include Heiri et al. (2003, 2007) and Ilyashuk et al. (2010). Not surprisingly the likelihood of encountering non-analogue situations increases with the age of the fossil assemblages (e.g. Birks et al. 1990, Heiri et al. 2003; Heiri & Millet 2005) and during periods of major climatic change such as the late-glacial period (e.g. Heiri & Millet 2005; Heiri et al. 2007). In these instances palaeoecological reconstructions of past climate must be carefully evaluated using other, independent climate records and checked for their palaeoecological and palaeoclimatological plausibility.

It is important to note that although numerical evaluation criteria can help in identifying non-analogue situations, their interpretation is often problematic. Numerical evaluation should therefore be seen not as an end in itself but as a source of information to supplement an interpretation based on an understanding of the ecological processes underlying the observed changes (Juggins & Birks 2011). Korhola et al. (2002) provide an elegant example of the use of both numerical and ecological criteria to help to evaluate a chironomid-based climate reconstruction in northern Fennoscandia.

What is required for all these reconstruction approaches is rigorous validation through comparisons with independent palaeoclimate evidence such as stable isotopes analysed in ice-core or tree-ring records, geomorphological evidence (e.g. glacier fluctuations, occurrence of permafrost), or other biological proxies (i.e. a multi-proxy study, Birks & Birks 2006). Work in Norway (S.J. Brooks and H.J.B. Birks, unpublished) in which pollen-based and chironomid-based calibration functions are applied to reconstruct mean July air temperature in the Holocene shows that the pollen-based and chironomid-based reconstructions can sometimes give very different results for the same stratigraphical sequence, with the chironomid-based reconstruction tending to give consistently lower temperature values than the pollen-based climate reconstruction. The critical question is thus, which reconstruction is the more reliable? Additional means of independent validation are needed to help decide which reconstruction should be accepted. One approach is to use plant macrofossil evidence as proof of local presence of, for example, tree Betula or Pinus sylvestris. On the basis of modern ecological observations (the indicator-species approach), their local presence can set lower limits (e.g. mean July temperature of 11°C or more) for the climate at the times when their macrofossils occur. Another approach is to use the probability density function approach of Kühl et al. (2002) for taxa that occur as macrofossils. A novel and as yet untried approach is to divide the fossil pollen assemblages into the numerically abundant and frequent taxa that comprise 75-90% of the assemblage and to use these to reconstruct the past climate using calibration functions and to use the excluded rare and numerically low taxa as ‘indicator’ taxa for validation purposes in a similar way to the use of plant macrofossils outlined above.

An important question related to the comparisons of chironomid-based and pollen-based climate reconstructions is why should chironomid-based temperatures be lower than the pollen-based temperatures? There are several possible reasons that relate to some of the basic assumptions and limitations of calibration functions.

1. Pollen-climate calibration functions are based on an indirect relationship (Birks & Seppä 2004). Modern pollen is a function, admittedly a complex and non-linear function, of modern vegetation. Modern vegetation is a function of modern climate, at least at a broad scale such as Fennoscandia. There is thus an indirect link between modern pollen and modern climate. An assumption of modern pollen-climate calibration functions is that the bulk of the pollen assemblage comes from the relevant pollen source area of the site and is thus indirectly related to the modern climate at the site. Long-distance dispersed ‘extra-regional’ pollen can be blown into sites from areas at lower altitudes (e.g. Ortu et al. 2006, 2010) or further south. This is a major and well-known problem in pollen analysis of sites in northern, alpine, and arctic areas. Plant macrofossils are a valuable guide to local species presence (Birks & Birks 2000). However, the absence of macrofossils does not mean that the species was absent locally. The net result of far-distance pollen on pollen-based climate reconstructions is that the resulting climatic estimates may be higher than the actual values. This effect is well
2. All empirical calibration functions are, by necessity, based on estimates of the parameters (e.g. optimum) of the realised Grinnellian niche or the regeneration niche today (e.g. Smart et al. 2010). In the past, the realised niches of taxa may have been different for a variety of ecological, environmental, and historical reasons (Jackson & Overpeck 2000; Jackson & Williams 2004) and thus assumption 3 of calibration functions and other climate reconstruction approaches, namely that the ecological responses of taxa today have not changed over the time represented by the fossil assemblages, may not be valid. Examples suggesting changes in realised niches are provided by comparative studies of reconstructed and simulated Holocene range shifts of *Picea abies* and *Fagus sylvatica*, two common tree species in northern and central Europe. Comparisons of their reconstructed Holocene spread patterns with their modelled range shifts show distinct divergences and thus highlight the difficulties in explaining the species’ Holocene range history on the basis of their modern realised climatic niches (Gieseeke et al. 2007; Miller et al. 2008).

3. An important bias in many modern pollen-climate training sets may result from the fact that much of the Earth’s land surface is covered by vegetation that is modified or even produced by human activity, especially in the last few hundred years. In northern Europe, the effects of human impact would generally decrease the percentage of *Quercus, Ulmus*, and *Tilia*, all of which are associated with high temperatures, and increase the percentages of non-arboreal pollen such as *Poaceae, Ericaceae, Juniperus*, and *Artemisia*, all of which (in the absence of human activity) are associated with low temperatures (Seppä et al. 2004). Holocene climate reconstructions may therefore be difficult to evaluate, especially when there is independent evidence for human activity in the study area and where there is extra-regional far-distance pollen. Climate reconstructions based on late-glacial pollen assemblages with high values of *Artemisia*, *Poaceae*, and other non-arboreal pollen types have a high chance of giving misleading temperature values, because much of the pollen may be extra-regional. St Jacques et al. (2008) develop a pollen-climate calibration set for Minnesota based on 133 pollen assemblages that pre-date European settlement, as well as a set based on modern pollen assemblages. Their study shows serious biases in climate reconstructions based on modern assemblages and less bias when the pre-European assemblages are used.

4. Although calibration functions for the same climate parameter can be developed for several groups of proxy-indicators, this does not guarantee that these organism groups are necessarily responding to the same aspect of present and past climate. For example, seasonal temperatures and precipitation are strongly intercorrelated in many available training data-sets. Similarly, a parameter such as summer air temperature will usually be correlated with other thermal parameters representing summer climate such as growing degree days, growing season length (Jackson et al. 2009), and, in the case of lake-living indicator groups such as chironomids, cladocerans, or diatoms, water temperature. In chironomid-July air temperature calibration functions, we are assuming that chironomid distribution and abundances today are a function of air temperature, whereas ecologically they are probably in part, or even to a large extent, a function of water temperature. Although there is a monotonic relationship today between air and water temperature (Livingstone & Lotter 1998), this relationship may not have been the same in the past due, for example, to changes in winter precipitation, leading to more and longer lasting snow presence at high elevation or high latitude sites, or due to changes in insolation and cloud abundance which may have affected the thermal regime of lakes. Lower chironomid-based estimates of mean July air temperature compared to pollen-inferred values may thus be a result of the chironomid-July air temperature calibration function being based on an indirect rather than a direct ecological relationship. Similarly, relationships between seasonal temperatures or thermal parameters may have been different in the past than they are at present. Lotter et al. (2011) discuss different hypotheses for explaining the offset between chironomid- and pollen-based July air temperature inferences from the sediments of Gerzensee, a small lake on the Swiss Plateau. Both proxies perform well in reconstructing temperatures in the modern environment and produce similar reconstructions during the earliest part of the late-glacial period but diverge in the latter part of the late-glacial interstadial between ca. 13,000 and 13,800 calibrated 14C years BP. One possible reason for this divergence is that vegetation and chironomid assemblages were responding to different aspects of late-glacial climate which are strongly correlated today but were not necessarily correlated in the late-glacial. Lotter et al. (2011) discuss that late-glacial vegetation may have been strongly affected by climatological parameters such as seasonality, winter temperature, or hydrological changes which are expected to have had a lower impact on chironomid distribution and survival.

A general observation from many multi-proxy studies is that while the different climate reconstructions usually agree in terms of highlighting the major trends and change-points, there can be substantial disagreement in the absolute values of the reconstructions between proxies (Birks et al. 2000). This is, in some ways, inevitable as different biological proxies have different sensitivity to the climate variable of interest and to any confounding variables. In this way, a partial validation of the basic proxy records follows from an attempt to quantify, understand, and explain the biases inherent in each proxy (Birks & Birks 2006; Juggins & Birks 2011).

Table 2 summarises some of the major problems that can arise in climate reconstructions from biological assemblage
Some Problems that can Arise in Climate Reconstructions from Biological Assemblage Data, the Detection of these Problems, and Potential Solutions

<table>
<thead>
<tr>
<th>Problem</th>
<th>Detection</th>
<th>Potential Solution</th>
</tr>
</thead>
<tbody>
<tr>
<td>High amount of noise in reconstruction</td>
<td>Visual examination of time series; calculation of measures of dispersion for time series</td>
<td>Smoothing using locally weighted regression; use simpler model to reduce overfitting</td>
</tr>
<tr>
<td>Systematic bias</td>
<td>Comparison with other quantitative reconstructions</td>
<td>Express reconstructed values as differences from mean or modern reconstructed values; use WA with classical deshrinking</td>
</tr>
<tr>
<td>Non-analogue situations</td>
<td>Reconstruction diagnostic statistics and evaluation methods</td>
<td>None; try WA or WA-PLS</td>
</tr>
<tr>
<td>Quality and availability of instrumental data</td>
<td>Numerical analysis of climate data</td>
<td>Use gridded data and robust interpolation procedures; assess errors associated with interpolation</td>
</tr>
<tr>
<td>Variable other than the one of interest driving the biotic changes</td>
<td>Comparison with independent physical, chemical, or biological proxies</td>
<td>None</td>
</tr>
<tr>
<td>Poor model performance statistics</td>
<td>High RMSEP, bias, etc</td>
<td>Careful numerical and ecological examination of data</td>
</tr>
<tr>
<td>Large sample-specific errors of reconstruction</td>
<td>Large error bars</td>
<td>Examine reconstruction diagnostics and test for non-analogue assemblages</td>
</tr>
</tbody>
</table>

Some Errors that can Arise (and have Arisen) in Developing Modern Organism-Environment Calibration Data-Sets and Possible Solutions

<table>
<thead>
<tr>
<th>Errors</th>
<th>Possible Solutions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Modern data from different sedimentary environments with contrasting taphonomies</td>
<td>Data screening</td>
</tr>
<tr>
<td>Not all samples are modern samples</td>
<td>Data screening and examination of meta-data</td>
</tr>
<tr>
<td>In very large data-sets, same samples may be duplicated by accident</td>
<td>Data screening</td>
</tr>
<tr>
<td>Inconsistent taxonomy or low taxonomic resolution</td>
<td>Analytical quality control and recounting</td>
</tr>
<tr>
<td>Inconsistent and/or poor environmental data</td>
<td>Data screening, new data</td>
</tr>
<tr>
<td>Model overfitting solely to minimise RMSEP</td>
<td>Van der Voet (1994) randomisation test, more rigorous cross-validation</td>
</tr>
<tr>
<td>Ignoring spatial autocorrelation in assessing model performance</td>
<td>Telford &amp; Birks (2009) deletion and h-block methods</td>
</tr>
<tr>
<td>No estimates of sample-specific errors of reconstruction</td>
<td>Bootstrapping</td>
</tr>
<tr>
<td>Model performance not based on cross-validation. Apparent statistics only</td>
<td>Use cross-validation (leave-one-out, split sampling, n-fold cross-validation)</td>
</tr>
<tr>
<td>No numerical evaluation of reconstruction</td>
<td>Apply reconstruction diagnostic measures</td>
</tr>
<tr>
<td>No validation of reconstruction using independent records</td>
<td>Not always possible but literature or internet searches can be useful</td>
</tr>
<tr>
<td>Reconstructing 2 or more variables that may, in reality, not be reconstructable</td>
<td>Careful use of partial constrained ordinations, consider not only marginal effects but also conditional effects (Juggins &amp; Birks 2011), simulations and randomisation tests</td>
</tr>
</tbody>
</table>

COMPARISON OF CLIMATE RECONSTRUCTIONS USING DIFFERENT METHODS

The three general approaches (Table 1) and their numerical methods discussed above are all different mathematically and ecologically and they model (implicitly or explicitly) species-climate responses in different ways. These methods should be viewed as complementary and not competitive (Racca et al. 2001), especially when there is no clear ‘winner’ in terms of modern model performance statistics (Juggins & Birks 2011). In these cases, it is useful to compare reconstructions based on a range of techniques. If down-core biological changes are primarily driven by changes in the reconstructed climate variable, one would
expect reconstructions from different models to follow similar trajectories, even if they differ in their absolute values (Birks & Ammann 2000). If different methods produce widely different reconstructions, this suggests that fluctuations in the dominant taxa are not primarily related to changes in the reconstructed variable and the reconstruction must be treated with caution (Juggins & Birks 2011). Similarity in reconstructions based on different methods but the same proxy data does not imply rigorous validation but indicates that the reconstructions are free from method-specific bias (Juggins & Birks 2011). See Walker et al. (1997), Lotter et al. (2000), Birks (2003), and Köster et al. (2004) for examples of such comparisons. When different reconstruction methods produce consistent rather than conflicting reconstructions, these can be combined into a single consensus reconstruction (e.g. Bartlein & Whitlock 1993; Racca et al. 2001; Birks 2003; Barrows & Juggins 2005).

Kucera et al. (2005) present a conceptual model for assessing the reliability of palaeoclimate reconstructions based on a scatter-plot of dissimilarity d, against model divergence Δ, represented by the standard deviation of the different estimates for each fossil sample. Samples with low d and Δ have convergent estimates and good analogues and are considered reliable. Samples with low d but high Δ also have good analogues but suffer from method-specific bias. Although one is faced with the problem of defining critical values of d and Δ, this simple method provides a tool that focuses attention on the interpretation of the differences between reconstructions based on different methods (Juggins & Birks 2011). This approach warrants wider use in palaeoecology.

NEW APPROACHES TO CLIMATE RECONSTRUCTION

The most successful and widely used approaches to reconstruct past climate changes based on fossil pollen and chironomid assemblage data strongly rely on empirical, relationships between assemblages and climatic parameters observed in the modern environment. However, empirical relationships and reconstruction models are not necessarily based on detailed ecological understanding of the mechanisms leading to a relation between fossil and subfossil assemblages and climate variables of interest. Furthermore, they do not usually include an explicit modelling of cause-and-effect relationships between environmental variables and taxon presence and abundance. Forward modelling of proxy responses to environmental change includes the establishment of a model describing the state (e.g. presence, abundance) of the proxy-indicator of interest considering a certain climate state (Haslett & Challenor 2010). Climatic reconstruction is then achieved by inverting the model and assessing the likelihood of different climatic conditions given a certain state (e.g. assemblage composition) of the proxy-indicator (e.g. Guiot et al. 2000, 2009). For example, Guiot et al. (2000) used a mechanistic model of vegetation expressed as a function of climate. By inverting the model under the constraint that the model output ‘fits’ the pollen data, Guiot et al. (2000) reconstructed past climate under various environmental conditions such as lowered atmospheric CO₂ concentrations. In contrast to the indicator-spe-

cies, assemblage, or multivariate calibration-function approaches described above, this forward modelling approach has a number of advantages. First, as in the Bayesian approaches briefly discussed below it allows the modelling of different sources of variability, whereas the assemblage approach and the multivariate calibration-function approach typically only provide a summary estimate of the reconstruction error. Second, since ecological processes are modelled explicitly, changes in species or assemblage response to changing environments over time can be explicitly included as well. An example includes the study of Wu et al. (2007a, 2007b), who used an inversion procedure based on a vegetation model to assess and take into account the effects of different atmospheric carbon dioxide concentrations on plant distribution when developing pollen-based climate reconstructions. Third, multiple proxies and/or multiple sites can be used simultaneously to produce climate reconstructions. The procedure then looks for the most likely climate state considering all the available models and the available proxy data. Fourth, such models are potentially very flexible. If taxa respond to different environmental parameters in different parts of the environmental or geographical gradients examined, this can be taken into account in the modelling approach. Fifth, observations under all environmental conditions are not needed, thereby enabling climate reconstructions for non-analogue conditions. The main disadvantages of this approach are that much more information is needed about the biological system of interest than for the indicator-species, assemblage, or multivariate calibration-function approaches, that many more assumptions are made about the proxy at hand, about the reliability of the applied models, and about the quality of the available proxy data, and that these modelling approaches are very demanding in respect to computing time. Such approaches based on forward modelling have been increasingly used in recent years using Bayesian statistics (e.g. Guio et al. 1999, 2008, 2009; Haslett et al. 2006; Hatté et al. 2009; Haslett & Challenor 2010) and it is expected that their importance and relevance will continue to increase with increasing computational resources and our understanding about the relationships between climate parameters and proxy responses.

GENERAL LIMITATIONS OF CLIMATE RECONSTRUCTIONS

The major strengths and weaknesses of the four most commonly used climate reconstruction techniques within the indicator-species approach, of the three most commonly used techniques within the assemblage approach, and of the two most commonly used calibration-function techniques are summarised in Table 4.

The key requirement in all climate-reconstruction methods is the need for high quality, internal consistency of the modern and fossil data-sets. Such data-sets require a detailed and consistent biological taxonomy and, for modern data-sets, reliable and representative climate data. The generation of modern training sets with detailed and consistent taxonomy in the multivariate calibration-function and assemblages approaches ideally requires that all the biological analyses are done by the same analyst who should be skilled in the relevant taxonomy. Many training sets covering broad geographical areas and climate gradients have, by necessity,
Patterns of climate variability are used, given the limited availability and quality of modern climate data in some geographical areas, and the complex topography of those areas makes it difficult to see how to improve the modern climatic data available. Particular problems arise in deriving reliable site-specific modern climate data for organisms. Even less attention is given to the quality and representation of methodology, quantitative analytical quality control, and agreed taxonomic and nomenclatural conventions are essential. Such harmonisation between data-sets and analysts is time-consuming and unattractive and as a result it is under-funded or even bypassed as national, continental, global data-bases rapidly develop. Even less attention is given to the quality and representativeness of the modern climate data used. Particular problems arise in deriving reliable site-specific modern climate data in mountainous and high-latitude areas, and standardised procedures of interpolation, lapse-corrections, etc., must be used throughout. Many interpolated modern climate values do not have reported uncertainties or, if reported, are ignored in developing modern organism-climate reconstruction models. In some situations it is difficult to see how to improve the modern climatic data used, given the limited availability and quality of modern climate data in some geographical areas and the complex patterns of climate variability over small areas, especially those with complex topography.

An important requirement in training-set development is that the modern data should be representative of the likely range of past climate variables. Besides having consistent taxonomy and nomenclature and being of comparable quality, the modern biological data should be from the same sedimentary environment as the fossil data-sets used for reconstruction purposes. Recent developments in modelling pollen-source areas (e.g. Prentice 1985; Sugita 1994; Jackson & Lyford 1999) have shown very clearly that moss polsters, small lakes, and large lakes all have very different relevant pollen-source areas (e.g. Zhao & Herzschuh 2009). Pollen spectra from soils, peat bogs, sediments from small enclosed lakes, and sediments from large lakes will also have different taphonomies. Similarly, it can be expected that the relationship of assemblages of lake-dwelling organisms (e.g. diatoms, cladocerans, chironomids) with temperature will be different in shallow, small lake basins compared with deeper, stratified lakes. It is essential to eliminate, when developing modern training sets to use.

Table 4. Strengths and Weaknesses of the Climate Reconstruction Techniques Discussed in this Essay

<table>
<thead>
<tr>
<th>Approach and Method</th>
<th>Strengths</th>
<th>Weaknesses</th>
</tr>
</thead>
<tbody>
<tr>
<td>Indicator-species approach</td>
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<tr>
<td><strong>Bio-climate modelling</strong> (e.g. Iversen 1944; Conolly &amp; Dahl 1970)</td>
<td>Simple, given distributional and climate data. Good for macrofossils</td>
<td>Presence/ absence data only</td>
</tr>
<tr>
<td><strong>Probability density functions</strong> (Kühl et al. 2002)</td>
<td>Probability of occurrence within climate space considered; estimates of uncertainty possible. Good for macrofossils and beetles</td>
<td>Presence/ absence data only</td>
</tr>
<tr>
<td><strong>Mutual climate range method</strong> (Atkinson et al. 1987)</td>
<td>Simple, given reliable distributional and climate data</td>
<td></td>
</tr>
<tr>
<td><strong>Modified mutual climate range method</strong> (Klotz et al. 2003; 2004)</td>
<td>Simple but elegant way of reducing estimated climate ranges; estimates of uncertainty possible</td>
<td>Presence/ absence data only</td>
</tr>
<tr>
<td>Assemblage approach</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Modern analogue technique</strong> (Overpeck et al. 1985; Simpson 2007, 2011)</td>
<td>Simple; classical; no assumed response model; deals with quantitative data; ecological plausible</td>
<td>Very sensitive to spatial autocorrelation; local fitting; data demanding; problems of finding appropriate numbers of analogues</td>
</tr>
<tr>
<td><strong>Response surfaces</strong> (Prentice et al. 1991; Bartlein &amp; Whitlock 1993)</td>
<td>Classical; no assumed response model; deals with quantitative data</td>
<td>Difficult to derived unbiased estimates of model performance; local fitting</td>
</tr>
<tr>
<td><strong>Artificial neural networks</strong> (e.g. Malmgren et al. 2001; Kucera et al. 2005)</td>
<td>No assumed response model; deals with quantitative data</td>
<td>Easy to overfit; very sensitive to spatial autocorrelation; ‘black box’; impossible to interpret</td>
</tr>
<tr>
<td>Multivariate calibration-function approach</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Weighted averaging (WA)</strong> (ter Braak &amp; van Dam 1989; Birks et al. 1990)</td>
<td>Assumed unimodal response model; ecologically plausible; simple and robust; can extrapolate; robust to autocorrelation; easy to compute prediction errors; global parameter estimation as optima; quantitative data</td>
<td>Edge effects; inverse; ignores other environmental gradients; sensitive to sample distribution in modern data</td>
</tr>
<tr>
<td><strong>Weighted averaging partial least squares (WA-PLS)</strong> (ter Braak &amp; Juggins 1993)</td>
<td>Assumed unimodal response model; can extrapolate; relatively robust to spatial autocorrelation; global parameter estimation; quantitative data</td>
<td>Edge effects; overfitting easy; inverse; reduced dimensionality; species coefficients not readily interpretable</td>
</tr>
</tbody>
</table>
with fossil data-sets, these sources of variation as far as possible (Zhao et al. 2009). Fossil pollen spectra from small lakes can only be reliably compared, whether in the analogue approach or the calibration-function approach, with modern pollen spectra from similar types of lakes. Climate reconstructions from fossil assemblages clearly require modern calibration functions estimated from modern assemblages from the same sedimentary environment as the fossil assemblages. However, Goring et al.’s (2010) work in British Columbia suggests that model error declines when samples from different depositional environments are combined for some pollen-based reconstruction models and climate variables.

The other important set of limitations of the multivariate calibration-function approach and the assemblage approach relate to two of the basic assumptions of climate reconstruction (see above), namely that the climate variable to be reconstructed is, or is linearly, or at least monotonically, related to an ecologically important determinant in the system of interest (assumption 2) and other variables than the climate variable of interest have negligible influence or their joint distribution with the climate variable of interest in the past is the same as today (assumption 5). These two assumptions are critical but are not often challenged (Juggins & Birks 2011). Assumption 2 raises the fundamental question of what climate variable can (or cannot) be reconstructed using a particular training set. For example, Fréchette et al. (2008) use the same pollen training set to reconstruct July temperature, January temperature, July sunshine, and annual precipitation. Muller et al. (2003) use MAT on the same modern pollen data-set in eastern Canada to reconstruct annual precipitation, mean annual temperature, evaporation:potential evaporation, mean January and July temperatures, run-off, and growing degree-days above 0°C and above 5°C. See also Magny et al. (2001, 2003) for reconstructions of seven climate variables from one data-set. de Vernal et al. (2001; 2005) use the same dinoflagellate cyst assemblages to reconstruct summer and winter sea-surface temperatures, the number of months of ice cover, and summer sea-surface salinity (see Telford 2006 for a critique).

The choice of climate variable to be reconstructed is usually done in one of two ways. First, it may be defined a priori by the initial project aims and the training-set designed specifically to sample this climate gradient (e.g. Brooks & Birks 2001; Bjune et al. 2010). Second, the climate variable may be selected post hoc after it appears to be an important biological determinant during a numerical analysis of the training set (e.g. Luoto 2010). In both cases, assumption 2, namely that the climate variable explains, in a statistical sense, a significant portion of the variation in the modern biological data can be tested using constrained ordination methods and associated Monte Carlo permutation tests (Birks 1995; 1998) with the climate variable of interest as the single constraining predictor variable (ter Braak 1987; ter Braak & Juggins 1993). The relative strength or importance of a climate variable of interest can be estimated by comparing the eigenvalue of the first axis of a detrended canonical correspondence analysis using the single variable of interest as the sole constraining variable with that of the first unconstrained axis (e.g. Lotter et al. 1997). As ter Braak (1987) notes, for a reconstruction to be useful, the first constrained eigenvalue should be large compared to the other eigenvalues because only then is the variable to be reconstructed determining the modern biological assemblages. Climate variables are inherently inter-related (Jackson et al. 2009) and assumption 2 is often qualified by the additional requirement that the variable of interest explains a significant and independent portion of the variation in the biological data. This is tested implicitly if variables are stepwise forward-selected in a constrained ordination (ter Braak & Verdonschot 1995) or explicitly using partial constrained ordination (ter Braak & Prentice 1988).

There are two important consequences from this. The first is that assumption 2 only requires a correlation between climate and biology, not a causal relationship. For some species there may be experimental evidence that suggests causal effects or demonstrates the physiological basis for the underlying response (e.g. Pigott 1982; Jackson et al. 2009). For other taxa there may be observational data that strongly suggest a direct effect (e.g. Brodersen et al. 2004, 2008). Where this is not the case, it should be recognised that the model may still have good predictive ability – but it does require an additional assumption that the relationship between the climate variable and the underlying causal ecological gradient has not changed through time. The second consequence is that reconstruction models developed for climate variables selected post hoc have an inherently weaker basis than those selected a priori in a hypothesis-testing approach. This is because of the circularity in cross-validating a model that has already been found to be significant. Models developed for variables selected using an automated step-wise procedure are especially problematic (Juggins & Birks 2011).

The problem of confounding effects (Table 5) of correlated climate and other environmental variables pervades almost all quantitative reconstructions, starting with Imbrie and Kipp (1971) and their reconstructions of summer and winter sea-surface temperatures and annual salinity. In almost all ecological systems, the composition of sedimentary assemblages is a complex function of multiple climate, edaphic, land-used, and historical factors. The first part of assumption 5, that environmental variables other than the climate variable of interest have negligible influence is therefore almost never met. The second part of this assumption, that the joint distribution of additional variables with the climate variable of interest does not change with time, is also violated in many cases (Jackson et al. 2009; Juggins & Birks 2011).

Telford and Birks (2005; 2009) discuss in detail assumption 6, namely the statistical independence of test data-sets, and, as reviewed above in connection with The Assemble Approach, provide ways of testing and allowing for lack of independence as a result of spatial autocorrelation. Two-way WA is relatively robust to spatial structure in the training set, probably because it estimates global parameters. WA-PLS appears to be less robust to spatial structure (Telford & Birks 2005; 2009) but it is not as sensitive as assemblage-approach methods such as MAT and ANN.

This discussion of the general limitations highlights the need to understand better the limitations of quantitative climate reconstructions, particularly when the critical assumptions are violated and to be aware of the ecological, statistical, and palaeocological assumptions, strengths, and
Weaknesses of our data (Tables 2-5) (Velle et al. 2010; Juggins & Birks 2011).

Assessing and interpreting uncertainties in climate reconstructions is a largely unexplored but critical topic in the reconstruction of past climate from biostratigraphical data. Whilst it is relatively easy, given modern computing power and appropriate software, to derive sample-specific errors of reconstruction for the climate variable of interest by bootstrapping (Birks et al. 1990), these errors are solely errors of the reconstruction model itself. It is much more difficult to estimate the inherent errors associated with the modern biological ($Y_m$) or environmental ($X_m$) data or in the fossil biological data ($Y_i$). The errors in the biological data are due to counting procedures, number of fossils counted, and laboratory techniques (Maher et al. 2011) and they can generally be estimated. What is much more difficult (and for some sources of error, possibly impossible) is to estimate the errors in the environmental data ($X_m$) due to, for example, interpolation procedures, selection of climate period, local topography, and between-year variation. Moreover, none of the reconstruction methods discussed above can analyse variation in the modern environmental data. Goring et al. (2010) explicitly examine model error in pollen data from different sedimentary environments.

One possibility for assessing the influence of a particular error component on the overall error of a transfer function is to quantify the variability of inferred temperatures associated with a particular error source, assume independence between the overall model error and the error source of interest, and estimate the magnitude of the model error if this error source could be eliminated. For example, Heiri et al. (2003) obtained replicate samples from five lakes in Norway, assessed the variability of chironomid-inferred temperatures for the individual lakes and estimated that this kind of variability is responsible for approximately 6-15% of the overall error of the applied calibration function. Heiri et al. (2003) concluded that the quantified error component, related to uncertainties associated with estimating the chironomid assemblage of a lake based on a single sediment sample and a limited number of analysed fossils, was too small to warrant more labour-intensive sediment sampling and enumeration schemes.

Environmental reconstructions developed in a Bayesian framework provide the opportunity of explicitly estimating and modelling different error components (see the discussions on New Approaches to Climate Reconstruction above and on Challenges and Future Developments below). A Bayesian framework offers a means of handling in a coherent, logical, and explicit manner the many sources of uncertainty in data and models and this must be considered to be one of the most relevant advantages of this approach compared with more conventional methods for producing climate reconstructions from palaeoecological data. The challenge is, of course, to implement this Bayesian approach in theory and in practice and to model realistically the different error components, given the limited data available for estimating different sources of variability associated with using biological proxies for inferring past climatic conditions. It is an enormous challenge but its successful implementation will be a major contribution to quantitative palaeoecology in the future (e.g. Brewer et al. 2008).

**CHALLENGES AND FUTURE DEVELOPMENTS**

The major challenges and likely future developments in the reconstruction of climate from fossil assemblages fall into two major groups – numerical and ecological.
The most obvious numerical challenge and future development is to incorporate reconstruction methods into a Bayesian framework. All the reconstruction methods discussed above under the three main approaches have different statistical and ecological bases and assumptions but they all have one thing in common (with the exception of the Kühl et al. (2002) probability density function method): they are all so-called frequentist methods and they make the assumption that the model parameters (WA optima or WA-PLS coefficients, etc) are fixed and can be estimated from observations (the observed data in the training set) distributed randomly about the fitted values (Holden et al. 2008). Conversely, a Bayesian approach does not rely on an explicit model of the relationships between species and climate but assumes that the model is unknown and is to be estimated from the measured data which are fixed. Specifically, the Bayesian approach uses measured information to modify some prior belief about the environmental values (Robertson et al. 1999). This additional information is derived from a training set and expressed as a conditional probability density function, which is combined with the prior probability density function to give a posterior density function using Bayes theorem (Juggins & Birks 2011).

Bayesian approaches have been applied to reconstruct past climate in several palaeoecological studies. Toivonen et al. (2001) present a Bayesian model with a conditional probability density function based on a unimodal species-environment response model. Vasko et al. (2000) and Korhola et al. (2002) extend this to include the more realistic multimonial Gaussian response model and apply it to chronomrid-based temperature reconstructions. Haslett et al. (2006) develop further these ideas to more generalised modelling of pollen-climate response surfaces, and Holden et al. (2008) present a computationally efficient approach based on probability weighting of species response curves. Haslett & Challenor (2010) present a very readable review of the current ‘state-of-the-art’ of palaeoclimatic reconstructions within a Bayesian framework.

Although the prediction errors for Bayesian models are generally of a similar magnitude to those for non-Bayesian approaches, they have the major advantage that they provide a coherent and explicit handling of uncertainty (Juggins & Birks 2011). Bayesian models offer an elegant solution for modelling multiple sources of evidence and their associated uncertainties within a single coherent framework and are thus a priority for future work (Haslett & Challenor 2010). However, the lack of available computer software and the huge computational burden of some Bayesian reconstruction models (days to weeks for a single reconstruction) currently prevents their more widespread use (Juggins & Birks 2011). Hopefully this situation will change in the future.

Despite continuing development and refinement of reconstruction methods (e.g. Vasko et al. 2000; Toivonen et al. 2001; Korhola et al. 2002; Gersdon et al. 2005; Erästö & Holmström 2006; Haslett et al. 2006; Holden et al. 2008; Hübener et al. 2008; Goring et al. 2009; Velle et al. 2011), we are probably close to the resolution of current data and methods. Decomposition of the variance in model RMSEP shows that the largest part (75% or more) is due to the fact that at a given environmental value today, there is still site-to-site variation in modern assemblages (Birks et al. 1990). No amount of mathematical analysis or modelling is going to minimise nature’s inherent variation. We need to pay more attention to the assumptions of the reconstruction approaches and to improve our abilities to interpret and compare temporal series of climate reconstructions. There is an urgent need to develop robust approaches for comparing temporal series and to be able to interpret sample-specific errors of reconstruction in a rigorous manner.

A second future numerical development may be the stronger integration of quantitative climate reconstructions with palaeoclimate models and dynamic vegetation models. In addition to using reconstructions for the validation of palaeoclimate model outputs (e.g. Braconnot et al. 2007a, 2007b; Renssen et al. 2009), the integration of modelling can provide improvements for quantitative climate reconstructions under environmental conditions that are strongly non-analogous with the present. An example of such a situation is the climate reconstructions from the last glacial period when the atmospheric CO₂ content was 180 ppm, thus nearly 50% lower than at present. Under such conditions, low CO₂ can influence processes of carbon and water uptake by plants and influence their distribution patterns, thus complicating the use of modern climate-vegetation patterns for climate reconstruction. Inverse vegetation modelling has been suggested as a method that can account for the inconstancy of the vegetation-climate relationship under non-analogous environmental conditions, such as during the last glacial period (Guiot et al. 2000). In this approach, several most likely climate scenarios are estimated for the time period in question, the vegetation model is run with each scenario and the simulated vegetation types are compared with the fossil pollen data to estimate the most coherent simulations. The past climate is obtained by inverting the climate input from the vegetation model (Guiot et al. 1999, 2000, 2009; Garreta et al. 2010). Wu et al. (2007a) used an inverse modelling approach with modern and glacial CO₂ concentrations to investigate the impact of changing CO₂ concentration on the reconstruction results from Africa and Eurasia. Wu et al. (2007b) used inverse vegetation modelling to suggest that the lowering of the altitudinal treelines in tropical Africa during the last glacial maximum was mostly caused by drying but amplified by decreased CO₂ concentration. Garreta et al. (2010) improved the method by replacing the static equilibrium model with a dynamic vegetation model LPJ-GUESS. They argue that the use of a dynamic vegetation model helps to bypass the assumption of equilibrium between vegetation and climate change and that the temporal link of the dynamic vegetation model allows a better exploitation of information from fossil pollen records (Garreta et al. 2010). On the downside, the approach of inverse modelling incorporates additional sources of error and uncertainty associated with the dynamic vegetation models, including the species parameterisation used in the model, and are likely to lead to large error estimates in the reconstructions of last glacial climate.

The other major set of challenges is ecological. Since the pioneering work on quantitative environmental reconstructions from biological assemblages (e.g. Imbrie & Kipp 1971; Webb & Bryson 1972; ter Braak & van Dam 1989; Birks et al. 1990), there have been many methodological developments in the numerical procedures for reconstructing past climates (e.g. MAT, response surfaces, WA-PLS) and in the
creation and application of training sets world-wide. Despite all these developments, surprisingly little work has been done relating to the assumptions and limitations of the reconstruction methods (but see Telford & Birks 2005; 2009).

The development of user-friendly software like C² (Juggins 2005) has given all palaeoecologists access to a wide range of reconstruction procedures. As a result, there is a shift from a single method and reconstruction model to a multi-model approach in response to the recognition that in many cases there is no single ‘best’ method or model (Juggins & Birks 2011). This shift has included an important move away from an obsession with models with the lowest RMSEP or, even worse, the highest \( r^2 \) (Birks 1995; 1998) to a more critical consideration of model uncertainty including bias. The use of multi-model reconstructions necessitates the recognition that model selection itself contributes to the overall uncertainty (Johnson & Omland 2004). Rigorous model selection has much to offer palaeoecologists. It offers a way of drawing inferences from a set of multiple competing hypotheses. It is based on likelihood theory, a robust framework that supports most modern statistical approaches (Johnson & Omland 2004). Its major advantages are as follows.

1. The investigator is not restricted to evaluating a single model where performance or significance is measured against some arbitrary threshold. Instead, competing models are compared to one another by evaluating the relative support in the observed data and by considering the model complexity (number of parameters, etc) for each model.

2. Models can be ranked and weighted, thereby providing a quantitative measure of relative support for each competing model.

3. When models have similar levels of support from the data, model averaging can be used to make robust parameter estimates and inferences (Johnson & Omland 2004).

There has also been a trend (Table 3) in recent years to reconstruct several environmental variables from a single training set (e.g. Luoto 2010). Given the very complex set of interacting environmental and biological factors on species distribution and abundance, the robustness of reconstruction methods to the effects of confounding variables (Table 5) becomes very critical, and is often ignored in studies where two or three environmental variables are reconstructed simultaneously from the same data-set. There are statistical tools to help misusing quantitative reconstruction methods to reconstruct variables of little or no quantifiable importance (ter Braak & Verdonscht 1995; Telford 2006; Juggins & Birks 2011), and greater use should be made of these and related statistical modelling techniques. The problem of the confounding effects of correlated environmental variables (Table 5) pervades all quantitative reconstructions (Juggins & Birks 2011), a point emphasised by Anderson (2000) in his discussion of the use of diatoms to reconstruct past climate and by Velle et al. (2010) in their discussion of the use of chironomids to reconstruct past climate.

Many of the early studies on quantitative environmental reconstructions involved strong environmental gradients such as sea-surface temperature, lake-water pH, salinity, or summer temperature. These studies stimulated development of new reconstruction techniques and of high-quality modern training-sets. Attempts at reconstructing weaker, secondary gradients are much more problematical and different methods may give very conflicting reconstructions (Juggins & Birks 2011). Although the problems of confounding variables have barely been addressed, these problems almost certainly mean that reconstructions for some variables based on some proxies are problematic at best (Juggins & Birks 2011). Future developments will hopefully see palaeoecologists being more critical of their inference models and the resulting reconstructions, and be alert to the invidious effects of confounding variables. Such developments will require not only a good understanding of the assumptions and limitations of the numerical methods being used but also a sound knowledge of the organisms and their ecology when used as palaeoenvironmental proxies and of the relevant environmental variables and their interactions.

CONCLUSIONS

Palaeoecology is the ecology of the past as we discussed in the Introduction. In practice, it has mainly been concerned with reconstruction of past biota, populations, communities, landscapes, environments, and ecosystems (Birks & Birks 1980). In such reconstructions, often all the available palaeoecological data, biotic and abiotic, have been used. The recent upsurge of interest and activity in multi-proxy studies (Birks & Birks 2006) where a range of biotic and abiotic proxies is studied on the same core or set of correlated cores allows palaeoecology to better understand the ecology of the past.

There are at least two major approaches to study the ecology of the past.

1. We study the responses of organisms in the past preserved in sediments to climate change but the palaeoclimate record is not based on the fossil group of interest but instead is based on independent palaeoclimate records such as stable isotopes and lake-level changes (Jackson & Booth 2002; Shuman et al. 2004), sea-level changes, diatoms, and geochemistry (e.g. Virah-Sawmy et al. 2009a; 2009b), calculated orbital solar irradiance and moisture values derived from stable isotopes (e.g. Willis et al. 2007), lake-level changes and fire severity (Shuman et al. 2009), tree-rings (Helama et al. 2009a, 2009b), or palaeolimnological proxies (e.g. Blass et al. 2007; Trachsel et al. 2010). This approach is very much in the scientific philosophy and methodology of using ‘the geological record as an ecological laboratory’ presented by Flessa and Jackson (2005a, 2005b).

2. In a multi-proxy study (e.g. Birks et al. 2000), one or more biological proxy can be used to provide an independent palaeoclimatic reconstruction using calibration functions (e.g. chironomids as a temperature proxy (Brooks & Birks 2000) or testate amoebae as a moisture proxy (Booth & Jackson 2003; Booth et al. 2004; Booth 2008, 2010). The responses in other proxies, e.g. pollen and, by inference, terrestrial...
vegetation, to the inferred climate changes are studied and questions of response times, lags, and rates of turnover can be studied and quantified (e.g. Birks & Birks 2008).

Both approaches give palaeoclimatic records that are independent of the group(s) of fossils of primary ecological interest and permit insights into the ecology of the past. They allow the late-Quaternary palaeoecological record to be used as a long-term ecological observatory or laboratory (Flessa & Jackson 2005a, 2005b) in which long-term ecological dynamics can be studied under a range of environmental conditions, not all of which exist on Earth today (e.g. lower CO₂ concentrations, low human impact) (e.g. Liu et al. 2010).

Related to palaeoecological reconstruction but with a greater ecological emphasis than palaeoclimatic inferences, are the recent studies that quantify the relationships between modern pollen assemblages and satellite remote-sensing data reflecting tree-cover or leaf-area index (LAI) (e.g. Williams 2002; Williams & Jackson 2003; Tarasov et al. 2007; Gonzales et al. 2008; Williams et al. 2008; Bezrukova et al. 2010: Herzschuh et al. 2010b). By using modern pollen data and Advanced Very High Resolution Radiometer (AVHRR) or Moderate Resolution Imaging Spectroradiometer (MODIS) remote-sensing data, it is possible to establish modern pollen–tree-cover or modern pollen–LAI relationships. Given fossil pollen data and with MAT- (Williams 2002; Tarasov et al. 2007; Gonzales et al. 2008; Williams et al. 2008; Bezrukova et al. 2010) or WA-PLS-based (Herzschuh et al. 2010b) models, reconstructions of past conifer-forest cover, deciduous-forest cover, vegetation cover, or LAI can be made. Using the same approach, net primary productivity can also be reconstructed which along with LAI is an important index of vegetation greenness (Williams 2002). Such reconstructions provide a valuable link between Earth system models and palaeoecological data.

By more closely integrating palaeoecology with ecology and climate and Earth system modelling (e.g. Brewer et al. 2007, 2009), and by changing the emphasis from reconstruction of past environments to the ecology of the past, palaeoecology can provide unique information about past systems such as variations in rates, states, composition, and resilience, responses to external boundary conditions and drivers including those with no modern counterparts, spatial and temporal scaling, and long-term perspectives that are much longer than those provided by ecological observations and long-term monitoring programmes. Palaeoecology can thus provide the ‘missing dimension’ in many aspects of ecology, conservation biology, and global science (Jackson 2006, 2007; Willis et al. 2010a).

Quantitative palaeoclimatic reconstructions based on the indicator-species approach, the assemblage approach, and/or the multivariate calibration-function approach will, we predict, continue to play an important role in future Quaternary palaeoecology. However, if the emphasis of Quaternary palaeoecology shifts from reconstructions of the past to the ecology of the past, climate reconstructions may cease to be ends in themselves but hopefully such reconstructions will become important means to new, challenging, and exciting ends in late-Quaternary palaeoecology.

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