IUPAC-IUGS common definition and convention on the use of the year as a derived unit of time (IUPAC Recommendations 2011)*,**

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Abstract: The units of time (both absolute time and duration) most practical to use when dealing with very long times, for example, in nuclear chemistry and earth and planetary sciences, are multiples of the year, or annus (a). Its proposed definition in terms of the SI base unit for time, the second (s), for the epoch 2000.0 is $1 a = 3.1556925445 \times 10^7$ s. Adoption of this definition, and abandonment of the use of distinct units for time differences, will bring the earth and planetary sciences into compliance with quantity calculus for SI and non-SI units of time.

Keywords: annus; decay constants; geochronology; IUPAC Analytical Chemistry Division; IUPAC Inorganic Chemistry Division; SI units; units of time.

INTRODUCTION

The International Union of Pure and Applied Chemistry, IUPAC, and the International Union of Geological Sciences, IUGS, set up a task group in October 2006 with the goal of updating the recommendations on radioactive decay constants (and half-lives) for geochronological use, last formalized in 1976.

In the course of the initial assessment, it was noticed that use of units for time in the geological literature is inconsistent both internally and with respect to SI (*Le Système international d'unités*). A source of inconsistency is the perceived contrast between "absolute time", or "age", i.e., the time difference between "now" and an event in the past, and the time difference between two events in the past. This issue is addressed immediately, as it requires neither new experiments nor extensive literature evaluations but only judgment and adherence to SI rules.

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SI AND NON-SI UNITS FOR TIME

The SI unit of time, the second (s), is impractical for expressing very long time intervals both for earth scientists and nuclear physicists alike. In such cases, other units are accepted for use with the SI. For geological and astronomical applications and for use with long-lived radioactive nuclides the year, or annus (symbol, a), is used [1–4].

The definition of the year in terms of the SI base unit, the second, is no trivial matter, as the year is not commensurable with the day, and is not a constant. There are several possible definitions available for the year, such as Julian, Mayan, Gregorian [1], Tropical (or Solar) and Sidereal. It is desirable that the chosen definition be stable with respect to long-term mismatch, i.e., it should contain a term accounting for variations of the year over time. None of the existing definitions of the annus fully embodies this fundamental principle. Definitions of the annus that are based on an intermediate relationship via the day, such as the Julian and Gregorian year, bear an inherent, pre-programmed obsolescence because of the variability of Earth's orbital movement.

Prior to the introduction of the atomic standard to define the second in 1967 (and the subsequent refinement in 1997, see ref. [5]), the SI definition of the second derived in terms of a fraction of a tropical year, for the epoch 1900.0, was "the second is the fraction 1/31 556925.9747 of the tropical year for 1900 January 1 at 12 hours ephemeris time [6]".

In view of the necessity to define units for time in such a way that they can be considered as constant for practical purposes, it is here recommended to define the year directly on the basis of the SI unit, the second. The Task Group proposes the annus as a defined multiple of the second that minimizes time-dependent inaccuracy. The present recommendation effectively reverses the definition used by [6] in favor of a more precise and up-to-date definition of the second. Taking into account the non-relativistic estimate of astronomical decrease by 0.530 s per century [1], for the epoch 2000.0 the year amounts to 31 556 925.445 s.

The unit a can be supplemented with prefixes k ($\times 10^3$), M ($\times 10^6$), and G ($\times 10^9$), without a fullstop between the prefix and the unit, viz. ka, Ma, and Ga to designate thousand, million, and billion (USA usage) years, respectively. These derived units are already in widespread use in earth and planetary science literature, though as noted above they lack precise definition. The departure lies in the use of different units (e.g., m.y., from the American Engineering Society) for ages and time differences, such that the interval between 90 and 100 Ma, for example, is sometimes designated as 10 m.y. Instead, following quantity calculus [4], units must follow algebraic rules such as the distributive law: 100 Ma -90 Ma = (100 - 90) Ma = 10 Ma, and so on. Similarly, half-lives should be expressed in ka, Ma, or Ga, and decay constants and rates of geological processes in ka⁻¹, Ma⁻¹, or Ga⁻¹. The definition of the second, and of the year based on the second, is that of a duration, or time interval. All time measurements are performed with respect to some reference datum, and the semantic distinction between age and duration depends solely on the choice of datum. Therefore, both should have the same units, and specification of the reference datum should be embodied in the context rather than in a distinct unit. In other words, in order to express an age, or absolute time, the same unit must be used as for time duration, with the optional addition of qualifiers such as "ago" or "before present" if a disambiguation is required. In such cases, it is implicit that the reference datum is the time of measurement, or a conventional datum such as 1950.0 or 2000.0. Analogies on the use of absolute and relative SI units are useful; for example, it is rarely denied that the depth difference between 100 and 200 m below ground level in a borehole is 100 m.

It is therefore recommended that geoscientists no longer express time durations in distinct ad hoc units such as k.y., M.y., or G.y. The goal is achieving compliance with the international standard by expressing time durations as a, ka, Ma, Ga.

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