

1        **Living systematic reviews: 3. Statistical methods for updating meta-analyses**

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22        **Keywords**

23        Living systematic review; Meta-analysis; Type I error; Type II error; Heterogeneity

24

25 **1 Table and 3 Figures**

26 **Table 1:** Key properties of the updating methods

27 **Figure 1:** Type I error rate as the number of studies or updates in a meta analysis increases.

28 **Figure 2:** Cumulative meta-analysis of the peptic ulcer data.

29 **Figure 3:** Applying the four sequential methods to the peptic ulcer meta-analysis

30 **ABSTRACT**

31 A living systematic review (LSR) should keep the review current as new research evidence emerges.  
32 Any meta-analyses included in the review will also need updating as new material is identified. If the  
33 aim of the review is solely to present the best current evidence standard meta-analysis may be  
34 sufficient, provided reviewers are aware that results may change at later updates. If the review is used  
35 in a decision-making context, more caution may be needed. When using standard meta-analysis  
36 methods, the chance of incorrectly concluding that any updated meta-analysis is statistically  
37 significant when there is no effect (the type I error) increases rapidly as more updates are performed.  
38 Inaccurate estimation of any heterogeneity across studies may also lead to inappropriate conclusions.  
39 This paper considers four methods to avoid some of these statistical problems when updating meta-  
40 analyses: two methods, that is, law of the iterated logarithm and the Shuster method control primarily  
41 for inflation of type I error and two other methods, that is, trial sequential analysis and sequential  
42 meta-analysis control for type I and II errors (failing to detect a genuine effect) and take account of  
43 heterogeneity. This paper compares the methods and considers how they could be applied to LSRs.

44 **Box “What is new?”**

- 45 – Living systematic reviews will require updating of any included meta-analyses at each review
- 46 update.
- 47 – If a living systematic review is used as part of a decision-making process, the frequent updating
- 48 of the meta-analysis could lead to inappropriate conclusions being drawn, due to an inflated
- 49 risk of falsely concluding statistical significance (type I error).
- 50 – Four statistical methods exist to avoid type I error inflation, and other statistical problems,
- 51 that arise in repeated meta-analyses.
- 52 – This paper gives an overview of these methods and how meta-analyses should be performed
- 53 in a living systematic review.

54

55 **Box 1 Living systematic reviews**

- 56 – A systematic review which is continually updated, incorporating relevant new evidence as it
- 57 becomes available
- 58 – An approach to review updating not a formal review methodology
- 59 – Can be applied to any type of review
- 60 – Uses standard systematic review methods
- 61 – Explicit and a priori commitment to a predetermined frequency of search and review updating

62

63 **Box 2 An example meta-analysis of peptic ulcer trials**

64 As an example of how the methods might be applied, we apply these methods to a meta-analysis of  
65 23 trials comparing endoscopic hemostasis to a control treatment for treatment of bleeding peptic  
66 ulcers<sup>23</sup>. This was originally used as an example to illustrate sequential meta-analysis<sup>19</sup> but is applied  
67 to all methods here.

68 A random-effects cumulative meta-analysis is shown in Fig. 2. This shows the results of the meta-  
69 analysis if it were updated once for every new trial, from the first-published trial at the top, to the last,

70 at the bottom. Each row of the forest plot representing the meta-analysis of all trials up to that point.  
71 It can be seen that a conventionally statistically significant result is achieved once only four trials have  
72 been included. We compare this to applying the four methods considered, assuming we wish to  
73 control for the standard type I error rate of 5%. For trial sequential analysis and sequential meta-  
74 analysis, we also assume we wish to have 90% power to detect a relative risk of 0.5 (which is that  
75 found from a meta-analysis of all the trials). In this example, we do not use the “approximate Bayes”  
76 heterogeneity estimation for sequential meta-analysis.

77 Fig. 3 shows the results for the four methods, respectively, (A) trial sequential analysis, (B) sequential  
78 meta-analysis, (C) Shuster, and (D) law of the iterated logarithm. In each case, the red dots and line  
79 show the progress of the updated meta-analyses after adding each trial, starting at the third trial, since  
80 a random-effects meta-analysis of two trials cannot reliably estimate heterogeneity. The black lines  
81 show the stopping boundaries for each method. Trial sequential analysis and sequential meta-analysis  
82 cross both the boundary for demonstrating treatment benefit and the maximum required sample size  
83 or information boundary after 10 trials for trial sequential analysis and 11 for sequential meta-analysis,  
84 although trial sequential analysis just touches the boundary after 6 and 9 trials. This shows that the  
85 required information or sample size has been reached after 10 or 11 trials, so had this analysis been  
86 run as a living systematic review, updating could reasonably have been stopped or slowed at that  
87 point. The law of the iterated logarithm and the Shuster methods take longer to find in favor of the  
88 treatment, requiring 16 or 17 trials to cross a boundary.

89 These analyses have been shown as if there were an update to the LSR after every new trial. If updates  
90 are less frequent, so multiple trials are added at each update, the analyses and their results are the  
91 same. It is currently conventional to display the results of trial sequential analysis and sequential meta-  
92 analysis methods as if an update had been performed for every trial, but this is not required. All  
93 analyses were performed in R, and the code is available from the authors on request. Code for trial  
94 sequential analysis is also available from the project website<sup>24</sup>.

95

96 **1 - BACKGROUND**

97 The key intention of a living systematic review (LSR, see Box 1), which differentiates it from a standard  
98 systematic review, is that it will be updated frequently, ideally as soon as any new relevant study is  
99 published or identified<sup>1-3</sup>. Over time the information available to be included may increase, requiring  
100 the review to be updated to ensure it is presenting the best available evidence. In many updates, this  
101 will require updating one or more of the meta-analyses included in the review.

102 There are two purposes for undertaking an LSR, which while subtly different have implications for the  
103 methods used to update meta-analyses. The first purpose is to present a summary of the evidence at  
104 the time of the most recent update. For this purpose, simply repeating each meta-analysis (whether  
105 fixed or random effects), adding the newly identified studies and presenting new forest plots and  
106 summary estimates, may be the most appropriate approach. All other components of the meta-  
107 analyses such as assessment of heterogeneity, subgroup analysis, and investigations of reporting bias  
108 will also have to be updated and repeated. Provided the meta-analysis methods used are appropriate,  
109 this approach will give the best estimate of the effect of interest at that point in time<sup>4</sup>. However, both  
110 the reviewers and readers should be aware that the results may change at later updates, and findings  
111 may be highly uncertain if there are few studies or participants included in the analysis.

112 Systematic reviews and meta-analyses are also used for clinical decision-making, guideline  
113 development, and reimbursement decisions. Typically, the level of credibility for the meta-analyses of  
114 many beneficial and harmful outcomes is considered before making recommendations for practice.  
115 An LSR in particular might be used to support the creation of “living guidelines”<sup>5</sup>, in which the best  
116 available evidence about the benefits and harms of an intervention is used to inform frequently  
117 updated recommendations about the use of the intervention. The effect estimate from the meta-  
118 analysis and its precision (or confidence interval) is one of the deciding factors in grading the existing  
119 evidence, and in this paper, we discuss the implications of continually or frequently updating meta-  
120 analyses for the statistical precision of the summary effects.

121 In a meta-analysis of clinical trials, we may wish to determine if an experimental treatment is superior,  
122 inferior, or equivalent to a control treatment. If the review presents assessments of statistical  
123 significance with a conventional 95% confidence interval or a P-value of 0.05, then updating of the  
124 meta-analyses may overestimate the number of meta-analyses considered statistically significant.  
125 While each individual analysis has only a 5% chance of finding a statistically significant result when, in  
126 fact, there is none (type I error), the chance of finding a false statistical significant result in any one  
127 meta-analysis increases as we repeat these analyses with each review update<sup>6</sup>.

128 As an example, consider a sequence of clinical trials of a new intervention compared to a control, with  
129 an updated meta-analysis conducted as soon as each new trial is published. Suppose that there is no  
130 true difference in effect between intervention groups on a particular outcome. In this circumstance,  
131 the type I error rate, of incorrectly getting a statistically significant result, rises rapidly with each new  
132 analysis, as shown in Fig. 1. Similarly, the confidence intervals that often accompany the summary  
133 effect will be too narrow if calculated using a conventional meta-analysis. Therefore, using  
134 assessments of statistical significance at any individual update of a meta-analysis carries a substantial  
135 risk of erroneously concluding that the new intervention is beneficial (or harmful). More formally,  
136 repeating a meta-analysis inflates the type I error.

137 In an LSR, we may also wish to determine when there is sufficient evidence such that we can be  
138 confident there is no meaningful effect to detect (such as no important difference in effect between  
139 new intervention and the control). This should be achieved so that a type II error is avoided, that is,  
140 the error of failing to detect a genuine effect and so that no future update will detect any evidence of  
141 a clinically meaningful effect. In a clinical trial, we might select an effect size to identify, such as a  
142 minimal clinically meaningful effect, a statistical power to detect that effect (e.g., 80% or 90%) and  
143 calculate the required sample size for the trial. We might conclude that the true effect size is less than  
144 the clinically meaningful effect if no statistically significant result is found once the specified sample  
145 size has been reached<sup>7</sup>. A similar approach can be taken with meta-analyses, including those in an LSR.  
146 However, previous analyses have found that few meta-analyses ever reach a sufficient sample size<sup>8</sup>.

147 When an LSR is used only to summarize the best evidence on a topic over time, using standard meta-  
148 analysis methods should be sufficient as the review is updated. However, if the LSR is being used to  
149 make decisions or readers will use it to do so, then we may wish to consider approaches to avoid  
150 inadvertent type I and II errors. This paper considers four methods that have been proposed to correct  
151 for these potential errors when updating a meta-analysis. While this paper focuses on LSRs, the same  
152 issues apply to all systematic reviews which may be updated. For example, Cochrane recommends  
153 that all Cochrane reviews be kept up to date, with revisions at least every 2 years if new trials have  
154 been published.

155

## 156 **2 - ANALYSIS METHODS FOR REPEATED META-ANALYSES**

157 Updating a meta-analysis has some similarities with interim analyses of clinical trials<sup>9-11</sup>. Interim  
158 analyses are often performed in trials so the trial can be stopped early if there is convincing evidence  
159 that the intervention is beneficial or harmful. Methods have been developed to avoid type I and II  
160 errors and produce robust conclusions for these trial sequential analyses. These methods have been  
161 adapted for the analysis of repeated meta-analyses and more recently for the updating of network  
162 meta-analysis.

163 Heterogeneity is also of particular concern in repeated meta-analyses. Heterogeneity should be  
164 considered in any meta-analysis, but it cannot be estimated accurately with few studies, and its  
165 estimation may vary substantially as a meta-analysis is updated. Incorrect estimation of heterogeneity  
166 may affect the conclusions drawn if the level of variability across studies is overestimated or  
167 underestimated. Heterogeneity also affects the required sample size, as greater heterogeneity  
168 reduces statistical certainty in the evidence and so increases the sample size required to detect a  
169 specified effect size.

170

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172

## 173 **2.1 -Trial sequential analysis**

174 Trial sequential analysis seeks to control the type I error by ensuring that the cumulative type I error  
175 rate across all updates remains at the desired level (usually 5%). To do this, the method uses the  
176 principle of alpha spending, that is, penalizing the type I error rate (alpha) at each analysis<sup>12-14</sup>. To  
177 avoid type II error, a maximum required sample size to detect some assumed effect size is also  
178 specified. This sample size is calculated in the same way as if the meta-analysis was a single clinical  
179 trial, by setting a desired type I error, an assumed effect size, and the desired statistical power to  
180 detect that effect.

181 In order to avoid inflated type I error prior to achieving the maximum sample size, alpha-spending  
182 boundaries are applied to the meta-analysis. In trial sequential analysis, the O'Brien-Fleming  
183 boundaries are applied to the sample size<sup>15</sup>. At each update of the meta-analysis, the Z score  
184 (estimated treatment effect divided by its standard error) is calculated. If this exceeds the upper alpha-  
185 spending boundary, then the result can be considered conclusive. For example, in a clinical trial, this  
186 would lead to a conclusion that the experimental intervention was superior to the control.  
187 Correspondingly, if the Z score were less than the lower alpha-spending boundary, the experimental  
188 intervention is worse than the control. If the maximum sample size is exceeded without crossing an  
189 alpha-spending boundary, we would conclude that any effect of the intervention is less than the  
190 specified effect. Additional stopping boundaries can be added to test for futility, so the updating  
191 process can be stopped if it is unlikely that a meaningful effect will be found.

192 Ideally, the assumed effect size would be the minimal clinically important effect size, as recommended  
193 by experts in the relevant field [16]. Alternatively, the effect size may be based on the trials currently  
194 in the meta-analysis. If this approach is used, it is recommended that only trials judged to be at low  
195 risk of bias be used to estimate the desired effect<sup>14</sup>. Heterogeneity across studies increases the sample  
196 size because it increases uncertainty in the effect estimates. It is therefore recommended that the  
197 sample size be adjusted for heterogeneity, using either some prespecified estimate of heterogeneity  
198 or the best current estimate of heterogeneity in the meta-analysis. In trial sequential analysis, the

199 heterogeneity adjustment is generally made using the  $D^2$  statistic, which is mathematically correct and  
200 produces a larger required sample size, although the more widely used  $I^2$  statistic may be used  
201 instead<sup>17</sup>.

202

## 203 **2.2 - Sequential meta-analysis**

204 Sequential meta-analysis, in a similar way to trial sequential analysis, uses methods adapted from  
205 sequential trial monitoring and applies them to a meta-analysis<sup>10</sup>. Sequential meta-analysis uses  
206 Whitehead's sequential trial boundaries approach to control type I error inflation and also type II error  
207 (failing to detect a genuine effect)<sup>18,19</sup>.

208 Sequential meta-analysis is based around calculating the cumulative Z score (the sum of the study  
209 effect estimates times their meta-analytic weights) and the cumulative statistical information V (the  
210 sum of the inverse of the study weights) at each update. A conclusive result is deemed to be achieved  
211 if the Z/V pair lies outside some prespecified boundary. For meta-analysis, a rectangular boundary is  
212 recommended, as this reduces the chance of crossing a boundary very early. Hence, if Z exceeds some  
213 boundary value  $Z_{MAX}$ , then there is evidence of a beneficial effect (as when crossing an alpha-spending  
214 boundary in trial sequential analysis). If V exceeds a boundary  $V_{MAX}$ , then the updating can be stopped  
215 as no conclusive result is ever likely to be found, as the maximum required statistical information or  
216 sample size has been reached. The  $Z_{MAX}$  and  $V_{MAX}$  values are calculated based on setting a desired type  
217 I error, an assumed effect size, and the desired statistical power to detect that effect.

218 Sequential meta-analysis implicitly adjusts for heterogeneity because as heterogeneity increases, the  
219 information contained in the meta-analysis decreases. This means the cumulative information V can  
220 decrease between updates as well as increase. Sequential meta-analysis can also control for  
221 misestimation of heterogeneity using an "approximate Bayesian" approach<sup>19</sup>. The DerSimoniane –  
222 Laird estimate of heterogeneity used at each update of the random-effects meta-analysis is replaced  
223 by a weighted average of the DerSimonianeLaird estimate and a prior estimate of heterogeneity. If

224 this prior estimate is suitably large, the method can control for underestimation of heterogeneity (and  
225 consequent overestimation of statistical information) early in the updating process.

226

### 227 **2.3 - The Shuster method**

228 The Shuster method is a newer alternative to the above two methods, designed by Shuster and Neu<sup>20</sup>.

229 This method also uses alpha-spending boundaries but with the more conservative Pocock boundaries

230 used in place of the O'Brien-Fleming boundaries used in trial sequential analysis<sup>20</sup>. The Pocock

231 boundaries were chosen as they are considered more robust to possible changes over time in the

232 effect size and to the fact that the required sample size is estimated rather than known.

233 Rather than a Z score, a modified t statistic is used. The result is only considered conclusive if the t

234 statistic crosses the Pocock alpha-spending boundary. The method controls only for type I error

235 inflation, so an assumed treatment effect and power are not required, and no sample size or statistical

236 information estimate is needed. This method requires prespecifying the number of meta-analysis

237 updates that will be performed. As this may not be known for an LSR, a reasonable guess will have to

238 be made.

239 The Shuster method makes no explicit adjustment for heterogeneity, but in a random-effects analysis,

240 the t statistic is a function of heterogeneity, decreasing as heterogeneity increases.

241

### 242 **2.4 - Law of the iterated logarithm**

243 Unlike the preceding methods, the law of the iterated logarithm approach is not based on sequential

244 trial analysis<sup>21,22</sup>. Instead, it seeks to adjust the usual Z statistic so that the desired type I error (e.g.,

245 5%) is maintained across all updates. To do this, the method utilizes the fact that a modified form of

246 the conventional Z statistic can be constructed to be bounded as the sample size N tends to infinity:

247 The law of the iterated logarithm approach therefore recommends replacing the standard Z statistic

248 at update k with a similar penalized statistic which is bounded as the statistical information (inverse

249 of the sum of the meta-analytic weights) increases:

250 The formulae also require a further penalty term  $\lambda$  in the denominator. For an appropriate choice of  
251  $\lambda$ , we can ensure that this penalized statistic is bounded by some suitable value, such as 1.96 for a  
252 conventional 95% confidence interval. Comparing this penalized statistic to 1.96 ensures that the  
253 standard 5% type I error is maintained across updates. The suggested values of  $\lambda$  are 2 for analyses of  
254 odds ratios, risk ratios, and mean differences and 1.5 for risk differences<sup>21</sup>. As with the Shuster  
255 method, the law of the iterated logarithm method only controls for type I error inflation, so does not  
256 require specification of sample size, an assumed effect estimate, or power. As with the Shuster  
257 method, no explicit adjustment for heterogeneity is made, other than the impact on the adjusted Z  
258 statistic from heterogeneity when using a random-effects analysis.

259 An application of the four methods to a meta-analysis of peptic ulcer trials is presented in Box 2.

260

### 261 **3 - METHODS FOR NETWORK META-ANALYSIS**

262 A multivariate extension of the alpha-spending boundaries method has been proposed for updating  
263 network meta-analysis under the assumption of consistency<sup>25</sup>. Despite the computational complexity  
264 in the presence of multiple interventions, the approach is essentially the same as in pairwise meta-  
265 analysis. Relative treatment effects between the compared treatments need to be set so as to satisfy  
266 the consistency assumptions. Then successively, monitoring boundaries for a predefined level of  
267 power are calculated so that overall, the type I error is at the nominal level. Comparison-specific  
268 treatment effects are updated after a study is added to the network as it contributes indirect evidence.  
269 In the method presented by Nikolakopoulou et al., informative priors are used for heterogeneity  
270 throughout.

271 Updating a network meta-analysis requires additional considerations. The addition of a trial examining  
272 a given comparison updates the treatment effects for all other treatment comparisons examined in  
273 the network. The assumption of consistency underlying this method needs to be reassessed after each  
274 update and the inflation of type I error needs to be controlled for in the inferences. In the early phases

275 of the network where few studies are included, estimation of inconsistency and heterogeneity will be  
276 problematic<sup>26</sup>.

277

#### 278 **4 - COMMENTARY ON THE METHODS**

279 The key properties of each method are outlined in Table 1. Most of the methods for handling repeated  
280 meta-analysis are based on an analogy between repeating meta-analysis and sequential analysis of a  
281 single clinical trial. While this analogy is generally reasonable, it has some limitations because meta-  
282 analyses are based on multiple studies and are not a single controlled trial. Heterogeneity between  
283 studies is an obvious key difference. In all methods, if a random-effects meta-analysis is used, the test  
284 score incorporates the extra uncertainty and decreases as heterogeneity increases. In sequential  
285 meta-analysis, the observed information decreases if the observed heterogeneity increases, and in  
286 trial sequential analysis, the required sample size is adjusted for heterogeneity, so will increase if  
287 heterogeneity increases. Neither law of the iterated logarithm nor the Shuster method makes any  
288 explicit adjustment for heterogeneity, other than its effect on the t statistic or adjusted Z statistic.  
289 Currently, only sequential meta-analysis accounts for poor estimation of heterogeneity, particularly  
290 when there are few studies, by using the approximate Bayesian adjustment. However, as this  
291 adjustment is essentially an alternative estimator for heterogeneity, it could, in principle, be used in  
292 any of the methods.

293 The methods have been described here as reaching a conclusion when some specified boundary is  
294 crossed (as seen in Fig. 3). It is also possible to represent the methods in a conventional forest plot, as  
295 with the cumulative plot in Fig. 2. This is achieved by adjusting the conventional 95% confidence  
296 intervals using the stopping boundaries so that the adjusted confidence interval excludes the null  
297 value only if a stopping boundary is crossed. Trial sequential analysis-adjusted confidence intervals  
298 can be generated, and the principle has been illustrated elsewhere for the sequential meta-analysis  
299 method<sup>19</sup> but can be similarly used for all four methods discussed here.

300 Although sequential meta-analysis and trial sequential analysis appear different on the surface, they  
301 are, in fact, based on the same underlying statistical theory of using O'Brien-Fleming alpha-spending  
302 boundaries to adjust the significance level required to judge that an effect is statistically significant.  
303 As such, the methods should, in principle, have similar properties, although results may differ in any  
304 particular meta-analysis<sup>27</sup>.

305 The primary difference between the methods is that sequential meta-analysis is based on the required  
306 statistical information to detect a desired effect, whereas trial sequential analysis generally uses the  
307 required sample size. Sample size depends on properties of the studies, such as the risk of an event in  
308 the control group. This may vary across studies and its estimate may change as the meta-analysis is  
309 updated, and so, the required sample size may not be constant across updates. Sample size should  
310 also be adjusted for heterogeneity. This could be done using the estimated heterogeneity at the  
311 current update, in which case sample size may vary substantially between updates. Alternatively,  
312 some prior estimate of expected heterogeneity could be used, but the sample size may be  
313 inappropriate if this estimate does not reflect the observed heterogeneity. Using required statistical  
314 information instead (as in sequential meta-analysis) has the advantage that it is independent of the  
315 properties of the trials, and of the heterogeneity, so, it does not vary across updates and can be  
316 calculated before trials are identified (e.g., in the protocol). Statistical information is, however, more  
317 difficult to interpret than sample size, and the total information may decrease between updates if the  
318 heterogeneity increases substantially. Although trial sequential analysis generally uses the sample size  
319 in its calculations, it is possible to use statistical information instead without any change to the  
320 underlying method.

321 As law of the iterated logarithm and the Shuster method control only for type I error inflation, they  
322 do not specify a required sample size or statistical information, nor a desired effect size or statistical  
323 power to detect it. This may make them simpler to implement as the stopping boundaries are not  
324 dependent on the properties of the studies included in the analysis or of external factors such as a  
325 clinically meaningful effect size. However, it does mean that these two methods have no stopping

326 conditions if there is no observable effect, so the methods cannot easily recommend that the updating  
327 of an LSR shall be stopped for futility. While trial sequential analysis and sequential meta-analysis do  
328 allow for stopping for futility, they require specification of a desired effect size, which may require  
329 specialist knowledge to determine and may be arbitrary or overestimate the true effect.

330 The methods could also be used to make judgments about when to update the LSR and its meta-  
331 analysis. Informally, if the current results are close to a stopping boundary, then an update might be  
332 needed soon, but if the results are a long way from a boundary, then it may be appropriate to wait  
333 longer. In the sequential meta-analysis and trial sequential analysis methods, it is possible to estimate  
334 how much statistical information or additional sample size might be needed before a boundary is  
335 crossed, and so, time future updates for when that level of information might become available from  
336 new trials. To our knowledge, these methods have not yet been used in this way so any use of these  
337 methods to plan future update should be cautious. Other methods for determining when and if a  
338 meta-analysis should be updated have been developed and could be used alongside the sequential  
339 methods considered here<sup>7,28,29</sup>.

340

## 341 **5 – CONCLUSIONS AND RECOMMENDATIONS**

342 The aim of an LSR is to provide the best available evidence to support decision-making by updating  
343 frequently, potentially as soon as a single relevant new study is identified. As with conventional  
344 approaches to updating, it is to be expected that the findings of the meta-analyses may change  
345 between updates and so reviewers should be suitably cautious when drawing conclusions from a  
346 meta-analysis in an LSR, particularly why n considering if a result is statistically significant.

347 The methods discussed in this paper should, in principle, increase the chance that conclusions drawn  
348 from a repeated meta-analysis are robust. The use of these methods in LSRs could therefore help  
349 prevent reviewers and readers from drawing inappropriate conclusions about the effectiveness of  
350 interventions. If these methods are used in an LSR, they should be clearly set out in the review  
351 protocol, including specification of desired type I error, assumed effect size, and the desired statistical

352 power. All the methods considered have been shown to avoid type I error inflation, as demonstrated  
353 in simulation studies for each method, and, to a somewhat lesser extent, in practical application in  
354 real meta-analyses. While this paper has focused on LSRs, the need to avoid errors of interpretation  
355 applies to all meta-analyses that are updated, even if less frequently than in an LSR. If a meta-analysis  
356 receives only one or two updates, however, the type I error inflation is modest, and there may be less  
357 need for these methods.

358 The frequent updating in LSRs may make them more resource intensive, expensive, and time-  
359 consuming to perform than a conventional review which might be updated infrequently or never.  
360 Given this, it is likely that in any LSR, decisions will have to be made about when to perform updates  
361 and if regular updating could be made less frequent or stopped. A possible benefit of the methods is  
362 that they could provide guidance as to when ceasing to update an LSR, or reducing update frequency,  
363 is statistically justifiable. The high risk of type I error means that conventional statistical significance is  
364 unsuitable for this<sup>30</sup>. When a stopping boundary is crossed in the methods considered here, however,  
365 the conclusions of the analysis are unlikely (up to the specified type I error) to change at future  
366 updates.

367 In an LSR, it would also be useful to know that updating could be stopped because no meaningful  
368 effect will ever be found. Reaching the maximum sample size or statistical information (without  
369 crossing any other boundary) in trial sequential analysis and sequential meta-analysis provides a  
370 possible means for making such a decision. It should be noted, however, that the properties of using  
371 these methods to decide on when and how to update an LSR has not yet been formally investigated.

372 Heterogeneity across studies in a meta-analysis will always be of concern, particularly when there are  
373 few studies so any estimation of heterogeneity is uncertain. This is a particular issue in LSRs as  
374 misestimation of heterogeneity will lead to incorrect confidence intervals and wrong judgments about  
375 the required sample size or amount of statistical information contained in the analysis. The  
376 approximate Bayes estimation of heterogeneity used in sequential metaanalysis may help to prevent  
377 such misestimation when there are few studies. However, any meta-analysis in an LSR which shows a

378 statistically significant result based on few studies, little information, or where there is evidence of  
379 substantial heterogeneity should be treated with caution, and further updates considered.

380 The methods described can correct for the statistical errors of type I and II errors, but they do not  
381 prevent other nonstatistical errors of analysis or interpretation. In particular, they do not correct for  
382 bias, and analysts should still consider the possibility of publication and selective reporting biases, as  
383 well as potential for bias due to including poor-quality studies.

384 This paper has only considered applying the methods to a single outcome, but most LSRs will meta-  
385 analyze multiple outcomes. Conclusions drawn from the LSR and decisions regarding stopping  
386 updating will, naturally, have to consider the findings across all outcomes and potentially on any  
387 subgroup analyses. The methods discussed here could potentially be used simultaneously on multiple  
388 outcomes, but the value of doing this is currently unclear. Similarly, all the methods are designed for  
389 the analyses of trials comparing interventions. How to avoid statistical errors when updating other  
390 types of review, such as in diagnostic test accuracy or prognostic testing, remains uncertain.

391 Some issues relating to the use of these methods remain uncertain and require further research. These  
392 include how the methods behave for different effect metrics (mean differences, relative risk, risk  
393 difference), their properties when data are sparse or highly heterogeneous, and how robust methods  
394 are when a boundary is crossed.

395 All the methods considered here are designed to achieve correct type I errors or P-values across  
396 repeated meta-analyses. Of course, making judgments about the value of an intervention based on  
397 the P-value alone is, rightly, widely criticized<sup>31</sup>. In any statistical analysis, it would be wrong to assume  
398 that an intervention is beneficial simply because a P-value of below 0.05 has been found. The same  
399 applies to sequential methods; when a boundary is crossed, the full evidence should be considered,  
400 including effect size, confidence intervals and heterogeneity, and the evidence from other outcomes  
401 or subgroups. The main purpose of these methods is, perhaps, not so much to demonstrate a  
402 beneficial effect as to avoid misinterpretation of conventional meta-analyses and confidence intervals

403 in LSRs where frequent updating means the risk of type I error is high and to guide the need for  
404 updating.

405

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410

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478 **TABLE**

479 **Table 1**

480 Key properties of the updating methods

	<b>Trial sequential analysis</b>	<b>Sequential meta-analysis</b>	<b>Shuster</b>	<b>Law of the iterated logarithm</b>
Corrects for type I error	Yes	Yes	Yes	Yes
Corrects for type II error	Yes	Yes	No	No
Assumed effect size and statistical power required	Yes	Yes	No	No
Need to specify number of updates	No	No	Yes	No
Adjusts information/sample size for heterogeneity	Yes	Yes	No	No
Adjusts for misestimation of heterogeneity	No	Optional	No	No

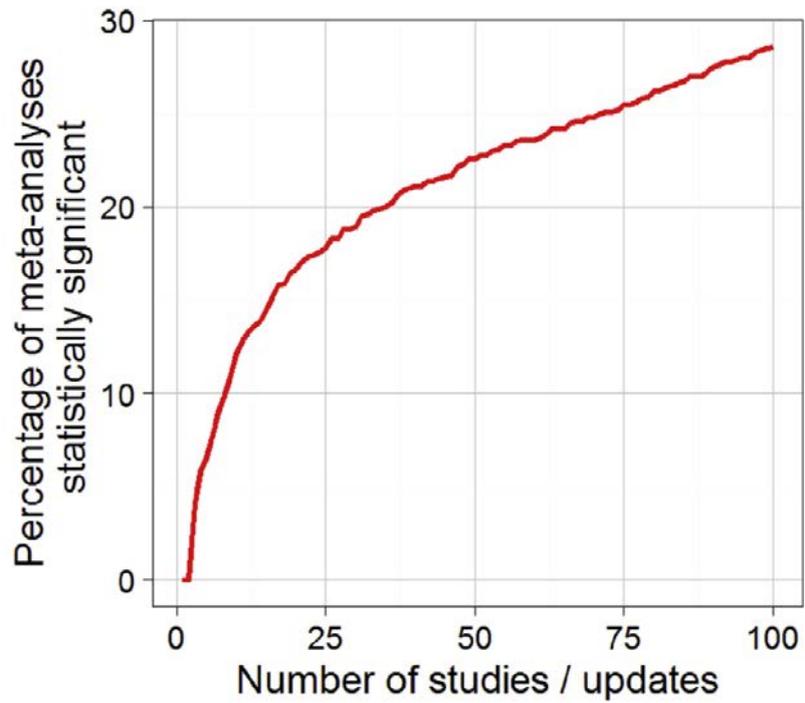
481

482

483 **FIGURES**

484 **Figure 1**

485 Type I error rate as the number of studies or updates in a meta-analysis increases.

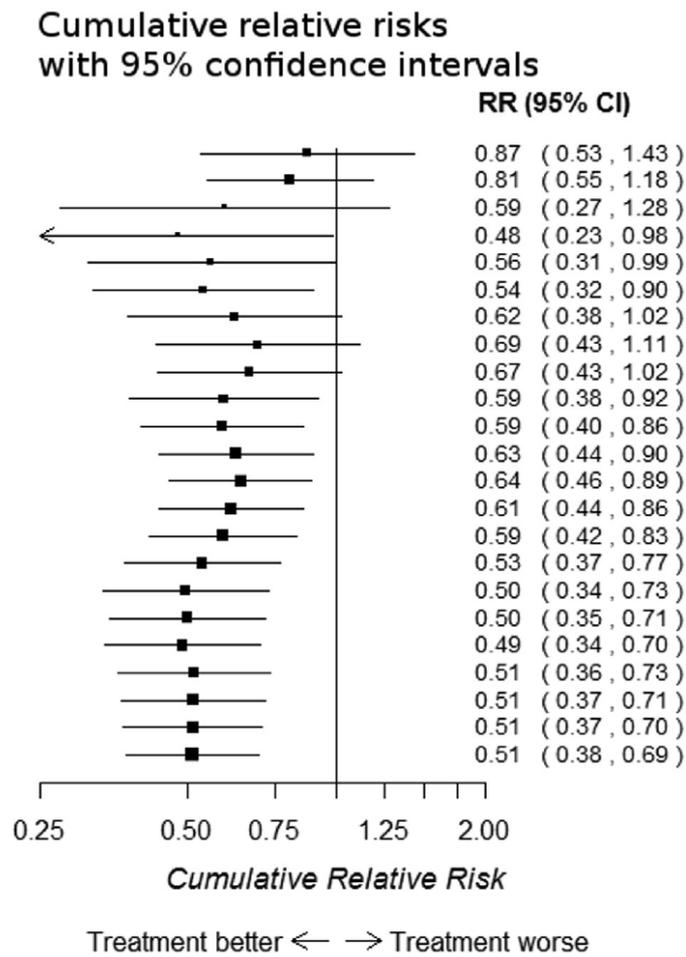


486

487

488 **Figure 2**

489 Cumulative meta-analysis of the peptic ulcer data. Each row of the forest plot representing the meta-  
 490 analysis of all trials up to that point, as if it were updated once for every new trial, from the first-  
 491 published trial at the top, to the last, at the bottom.



492

493

494 **Figure 3**

495 Applying the four sequential methods to the peptic ulcer meta-analysis. Results of updated meta-  
 496 analyses are shown for (A) trial sequential analysis, (B) sequential meta-analysis, (C) Shuster, and (D)  
 497 law of the iterated logarithm. The red dots and line show the progress of the updated meta-analyses  
 498 after adding each trial, starting at the third trial, since a random-effects meta-analysis of two trials  
 499 cannot reliably estimate heterogeneity. The black lines show the stopping boundaries for each  
 500 method. Trial sequential analysis plots the standard Z score against cumulative sample size. Sequential  
 501 meta-analysis plots the cumulative Z score (the sum of the study effect estimates times their meta-  
 502 analytic weights) against the cumulative statistical information (the sum of the inverse of the study  
 503 weights). Law of iterated logarithm plots the penalized Z score at each update or trial and the Shuster  
 504 method, the adjusted t statistic at each update or trial. (For interpretation of the references to color  
 505 in this figure legend, the reader is referred to the Web version of this article.)

