Exoplanet characterization by multi-observatory transit photometry with *TESS* and *CHEOPS*

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ABSTRACT

Space-based photometric surveys have discovered large numbers of planets transiting other stars, but these observe in a single band-pass and yield only the planet radius, orbital period and transit duration. Information on the masses, compositions and any atmospheres of these planets requires additional observations from the ground or space. The Transiting Exoplanet Survey Satellite (TESS) will yield thousands of planets around bright stars suitable for such follow-up. In the absence of spectroscopy or spectrophotometry from space, observations through the different passbands of multiple space telescopes provide some spectral information useful for identifying false-positive signals, distinguishing between reflected light and thermal emission from hot Jupiters, and detecting Rayleigh scattering by planetary atmospheres. We calculated the expected difference in transit depths measured by the TESS and Characterizing Exoplanet Satellite (CHEOPS) missions, which will be more sensitive to redder and bluer optical wavelengths, respectively. The difference due to companion or background stars is small (<3 per cent for main-sequence companions) and likely to be negligible and undetectable. For only a few 'hot' Jupiters, can combined photometry disambiguate between the reflected and thermal signals from planets. However, the Rayleigh scattering by hazy atmospheres with particles sizes near 0.04 μ m and at pressure altitudes above ~1 mbar can be detected for ~ 100 transiting planets, assuming every planet has such an atmosphere. Hazes with this characteristic particle size do not obscure observations at longer (near-infrared) wavelengths; CHEOPS follow-up of TESS-detected planets could thus identify candidates suitable for further study with the James Webb Space Telescope.

Key words: planets and satellites: atmospheres - planetary systems.

1 INTRODUCTION

Exoplanet research is moving beyond an era dominated by discovery and statistics and into one in which characterization of planets and their atmospheres takes a leading role. Pioneering surveys by ground-based telescopes using the Doppler radial velocity (RV) method (Udry, Fischer & Queloz 2007), and the *CoRoT* satellite using the transit photometry method (Deeg 2013) segued to the *Kepler* mission and its transit survey of almost 200 000 stars (Borucki et al. 2010). The yield of thousands of candidate or confirmed exoplanets has enabled statistical descriptions of the planet population down to Earth-size or smaller.

However, the information provided by a transiting exoplanet mission like *Kepler* and its successor *K2* is limited to the orbital period and radius of the planet, assuming the radius of the star is known.¹ This is true of any 'white light' measurement where only the signal integrated over the full wavelength range of the instrument response is recorded. To validate and characterize transit detections, additional data obtained from the ground or space are usually needed. Future space-based exoplanet surveys, such as the *Transiting Exoplanet Survey Satellite (TESS*; Ricker et al. 2014) and the *Planetary Transits and Oscillations (PLATO*; Rauer et al. 2014), will target brighter stars suitable for such follow-up over much of the sky. In addition to RV observations to measure planet mass, spectral (wavelength-dependent) information is valuable or crucial

¹ The transit duration provides limited information on the orbital elements and/or density of the star.

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in at least three other aspects: validation of the planet and confirmation of its host star, distinguishing between reflected and emitted light from the planet as observed during opposition and secondary eclipse, and detection of any atmosphere in transmitted light during a primary transit.

Validation of the transiting object as a planet and identification of the correct host star often requires other observations, sometimes at multiple wavelengths. To cover large areas of sky, transit surveys use large pixel sizes (21 arcsec for TESS), meaning a nonnegligible probability that background stars or stellar companions contribute to the flux in the photometric aperture of a target. The additional sources dilute the transit signal, meaning that the transiting object is actually larger than apparent. In addition, a fainter, blended star rather than the target star may be the source of the signal. Blended eclipsing binaries with a large contrast ratio or at much greater distances than the target star can produce 'false positives' that mimic some aspects of a planetary transit signal. These scenarios have motivated a variety of methods to identify false positives, including analysis of the transit photometry itself (Seager & Mallén-Ornelas 2003; Batalha et al. 2010; Bryson et al. 2013; Mullally et al. 2016), and high-resolution imaging of the host star to identify other blended sources in the transit survey (e.g. Everett et al. 2015). Another approach is to measure the transit depth at different wavelengths; if the host star has a different colour than other stars that contribute to the photometric flux then the transit depth will vary with wavelength (Tingley 2004; Colón, Ford & Morehead 2012; Tingley et al. 2014; Désert et al. 2015). For example, the transit will be deeper at longer wavelengths if the actual source of the signal is redder than the target star.

Additional observations are invariably required to obtain planet properties other than radius and orbital period; foremost among these are planet mass that can be measured by RV measurements or the method of transit timing variation (Agol et al. 2005; Holman & Murray 2005), and presence and composition of any atmosphere. Estimation of both mass and radius allows a planet to be placed on a mass-radius diagram and compared to interior models. These comparisons can, for example, identify planets that are almost exclusively rocky metal, with no or only a thin atmosphere, as well as planets with much lower densities that can be explained only by a thick envelope of hydrogen and helium, which are incondensible and have a low molecular weight. In intermediate regions of the mass-radius diagram the models are degenerate, that is, there are multiple possible bulk compositions, and mass and radius alone are not sufficient (Rogers & Seager 2010). In these cases, identification of an H-He envelope by independent means is valuable. Information on any atmosphere is also crucial to understanding the formation, chemistry, surface conditions and potential habitability of a planet.

One approach to detecting and characterizing the atmosphere of an exoplanet is by observations at multiple wavelengths when either the planet passes in front of the host star (primary transit) or when the star occults the planet (secondary eclipse; Seager 2008; Encrenaz et al. 2015). In the former case, variation in the absorption of the atmosphere due to atomic or molecular lines or scattering causes small changes in the apparent radius of the planet with wavelength. In the latter, the atmosphere manifests itself by reflection and emission, and hence changes in the secondary eclipse depth that are wavelength dependent.

The primary *TESS* mission will survey most of the sky and is expected to detect $\gtrsim 2000$ planets (Sullivan et al. 2015) around relatively bright stars suitable for such follow-up. These observations can be performed by ground-based telescopes, but variable

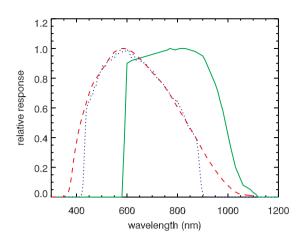


Figure 1. The predicted or established response functions of *TESS* (solid green), *Kepler* (dotted blue) and *CHEOPS* (dashed red), all normalized to unit maximum.

atmospheric absorption and the finite duration of continuous observations limit accuracy and completeness. Ground-based spectroscopy on a future generation of extremely large telescopes hold promise for exoplanet characterization, but the time available will greatly limit the task of screening thousands of planets. Highly accurate spectrophotometric observations can be performed above the atmosphere by the *Hubble Space Telescope (HST)* or the future *James Webb Space Telescope (JWST)*, but these are even more heavily competed for. What are needed are means to cheaply and rapidly screen most or all *TESS*-detected planets to identify those objects of particular interest, e.g. those most likely to have a detectable atmospheric signal.

At the time of writing, no space satellite other than HST offers spectroscopy or multipassband photometry from space. In the absence of such observations, limited spectral information can still be extracted if the passbands of two measurements are substantially different, that is, if one is redder or bluer than the other. In particular, the deep-depleted charge-coupled detectors (CCDs) to be used in the cameras of the TESS, have substantial response at $\lambda = 1 \,\mu\text{m}$ and beyond (Woods et al. 2016). This red response distinguishes them from the conventional CCDs used in other cameras, that is, that of the NASA Kepler satellite (Koch et al. 2010) and the upcoming Characterizing Exoplanet Satellite (CHEOPS; Fortier et al. 2014) and PLATO missions, which have declining sensitivity beyond $\lambda = 0.6 \,\mu\text{m}$ and virtually no response beyond 0.9–1 μ m. Fig. 1 shows the relative response functions of the Kepler, CHEOPS and TESS (that of PLATO is not yet available).

Placek, Knuth & Angerhausen (2016) demonstrated how the combination of photometry from *Kepler* and *TESS* can distinguish between the contributions of reflected light and thermal emission to the total signal from a 'hot' Jupiter-size planet on a close-in orbit. While *Kepler* photometry is more sensitive to bluer wavelengths and thus the reflected signal, *TESS* is more sensitive to redder wavelengths and the thermal emission from the hot day-side of the planet. By observing the depth of the secondary eclipse with both instruments, and making assumptions about the reflected and thermal spectra, the two signals can be separated, allowing both the geometric albedo and the day-side temperature to be independently estimated. The drawback of this strategy is that the primary *Kepler* mission observed only 0.28 per cent of the sky, and the successor

K2 mission is restricted to fields near the plane of the ecliptic, which *TESS* will not observe.²

In contrast, CHEOPS can point to most of the sky and is designed expressly for follow-up of known exoplanet systems, including those discovered by TESS. Lee et al. (2017) examine how the combination of TESS and CHEOPS photometry could be used to characterize the atmosphere of the hot Jupiter HD 189733b. In this work, we show how the combination of measurements by TESS and CHEOPS can contribute to characterization of transiting exoplanets and their atmospheres in the three ways described above. In Section 2, we describe some of the tools and data bases used in our calculations. In Section 3, we analyse the degree to which these measurements can identify the correct host star and identify false positives, that is, diluted eclipsing binaries. In Section 4, we investigate the contribution of TESS-CHEOPS measurements to distinguishing between the reflected and thermal emission from planets, that is, hot Jupiters. In Section 5, we use model planet atmospheres and empirical or realistic model spectra of stars to determine the magnitude of the TESS-CHEOPS signal produced by an atmosphere during a primary transit. We expand on the last aspect in Section 6, where we consider the detection of atmospheres with different compositions among the entire catalogue of simulated TESS planets constructed by Sullivan et al. (2015). We conclude in Section 7 with a discussion of systematic effects and future prospects for multicolour transit spectrophotometry both from space and ground.

2 METHODS

Stellar spectra. Two sets of spectra were used for these calculations. For K- and M-type dwarf stars ($T_{\rm eff} < 5400$ K), we used actual spectra obtained at visible and near-infrared wavelengths and flux-calibrated by Mann et al. (2015) and Gaidos et al. (in preparation). For the full range of spectral types, we used model spectra generated by the PHOENIX code in a spherical mode by Husser et al. (2013). The spectrum of the host star was interpolated from a grid with $T_{\rm eff}$, log g and [Fe/H]. In cases where the metallicity is not known, it was assumed to be solar.

Response functions and calculations. The response versus wavelength of *TESS* was taken from Ricker et al. (2014). The *CHEOPS* response function was calculated by multiplying the throughput of the optics by the detector quantum efficiency using data provided by the *CHEOPS* team (A. Fortier, personal communication). The *Kepler* high spectral resolution response function was constructed by J. van Kleeve and distributed by the NASA *Kepler* Guest Observer office.³

Planetary atmosphere transmission model. For the calculation of the transmission spectra (as a wavelength-dependent apparent planet radius R_p), we assumed a reference radius R_0 on top of which we place an isothermal atmosphere with a total pressure at R_0 of two bar. The pressure is high enough to guarantee that the atmosphere becomes opaque at all wavelengths. The planet is then divided into 200 annuli *p*. The integrated slant optical depth along each tangent height was calculated via

$$\tau_{\lambda}(p) = \int_{-\infty}^{\infty} \chi_{\lambda}(x(p)) \,\mathrm{d}x, \tag{1}$$

where χ_{λ} is the extinction coefficient, including contributions by absorption and scattering, and *x* the coordinate along the tangent.

The effective tangent height was then calculated via

$$h_{\lambda} = \int_0^\infty (1 - T_{\lambda}(p)) \,\mathrm{d}p, \qquad (2)$$

where

$$T_{\lambda}(p) = e^{-\tau_{\lambda}(p)} \tag{3}$$

is the transmission along a given tangent *p*. Finally, the wavelengthdependent transit radius is given by

$$R_{\lambda} = R_0 + h_{\lambda}. \tag{4}$$

Additionally, the transmission spectrum was normalized such that within a white-light filter from 0.5 to 1.05 μ m a given planetary radius is obtained.

The absorption coefficients for H_2O , CO_2 , CO, CH_4 , NH_3 , C_2H_2 and HCN were calculated with the HELIOS-K opacity calculator (Grimm & Heng 2015). For H_2O , CO_2 and CO we use the HITEMP2010 line lists (Rothman et al. 2010), whereas for the rest, HITRAN2012 (Rothman et al. 2013) was employed. In addition to these molecules, the lines of the alkali metals Na and K were also included, using the line data from Draine (2011). Collision-induced absorption continua description from HITRAN2010 (Rothman et al. 2010) was employed for H_2 - H_2 and H_2 -He collisions.

The molecular scattering cross-sections were derived via the usual Rayleigh scattering equation

$$\sigma_{\text{rayleigh}} = \frac{24 \,\pi^3 \nu^4}{n_{\text{ref}}^2} \left(\frac{n(\nu)^2 - 1}{n(\nu)^2 + 2}\right)^2 K(\nu),\tag{5}$$

where ν is the wavenumber, *n* the refractive index, n_{ref} a reference particle number density and *K* the King factor. The corresponding data for H₂ are adopted from Cox (2000), for H₂O from Wagner & Kretzschmar (2008), for CO, CH₄, CO₂ and He, respectively, from Murphy (1977), Sneep & Ubachs (2005) and Thalman et al. (2014). The atmospheric abundances of the molecules are calculated using an equilibrium gas-phase chemistry (Stock, Kitzmann & Patzer, in preparation). The chemistry model contains about 550 gas-phase species (including ions) and is based on the semi-analytic approach described in Gail & SedImayr (2014). The solar elemental abundances are taken from Asplund et al. (2009).

For the high-altitude condensates, we follow the approach of Howe & Burrows (2012) and assume a photochemical haze composed of tholin particles. The corresponding refractive index is adopted from Khare et al. (1984). Unless otherwise stated, all hazes are modelled with a monodisperse size distribution and a particle number density of 1000 cm^{-3} .

3 IDENTIFICATION OF HOST STAR IN MULTIPLE SYSTEMS AND FALSE POSITIVES

The large angular size of the pixels and photometric apertures of wide-field surveys such as *TESS* means that blends with stars other than the target star will be frequent, and many stars are unresolved multiples, thus it is often necessary to distinguish among multiple possible host stars for the transiting object. Moreover, a common 'false-positive' scenario in wide-field exoplanet surveys is a fainter background or companion eclipsing binary that contaminates the aperture (Brown 2003; Evans & Sackett 2010). If the colours of the stars that contribute flux to the total measured signal are different, then the transit depth will vary with wavelength and thus the passband because only one of the stars is obscured. The detection of a difference in transit depth between passbands thus can indicate

² An extended *TESS* mission could observe the ecliptic.

³ https://keplergo.arc.nasa.gov/kepler_response_hires1.txt

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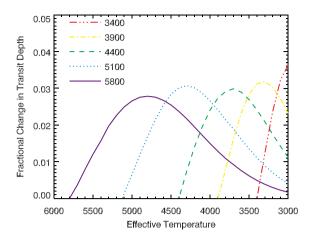


Figure 2. Fractional difference in *CHEOPS* and *TESS* transit depths due to the presence of an unresolved companion star as a function of the secondary star's T_{eff} , for several values of the primary star's T_{eff} .

a false positive and the *sign* of the difference can be used to tell which star is the host. The fractional change in the transit depth δ of a planet orbiting star '1' due a second star ('2') is

$$\Delta \delta = \int \frac{f_{1,A} f_{2,B} - f_{1,B} f_{2,A}}{\left(f_{1,A} + f_{2,A}\right) \left(f_{1,B} + f_{2,B}\right)} d\lambda, \tag{6}$$

where $f(\lambda)$ is the signal from source 1 or 2 in passband A or B.

Using equation (6) and the spectra described in Section 2, we calculated the fractional difference in *CHEOPS* and *TESS* transit depths produced by physical companion, for the case where the stars are unresolved and both on the main sequence, and the secondary is cooler and less luminous (Fig. 2). Since equation (6) is an antisymmetric function for $1 \Leftrightarrow 2$, the sign of the difference will depend on whether the planet orbits the first or second star. In all cases, the estimated difference is <3 per cent. The difference is small for nearly equal brightness binaries because the spectra are similar, whereas much cooler companions will have dissimilar spectra but contribute little to the overall flux. If the stars are resolved and the secondary contributes only part of its flux to the photometric aperture, the difference will be smaller.

We also considered the case of unrelated background stars. There are many possible configurations of candidate host stars and background sources, so to generate realistic scenarios, we used the synthetic catalogue of *TESS*-detected transiting planets and their host stars generated by Sullivan et al. (2015). We constructed a synthetic background star population covering one square degree to V = 30 using TRILEGAL v. 1.6 (Girardi 2016) with the default settings and 'typical' Galactic coordinates l = 90 and b = 30. There are negligible numbers of fainter (V > 30) stars for these settings. TRILEGAL outputs the fundamental parameters for each star plus the line-of-sight extinction A_V . The surface density of stars is 10.9 arcmin⁻², thus there is an average of 1.2 background star per 21 arcsec² *TESS* pixel.

We considered scenarios with a single background star per exoplanet host and simulated 10 such scenarios per host star, randomly drawing the background stars from the synthetic population. The spectra of the host star and background star were approximated by the PHOENIX spectrum with the closest values of T_{eff} , log gand [Fe/H], and reddened using the simulated A_V values converted to E(B-V) assuming a reddening ratio of 3.1 and the reddening curve of Cardelli, Clayton & Mathis (1989).

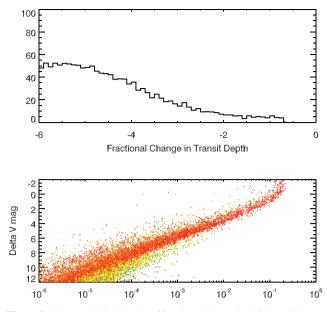


Figure 3. Top panel: distribution of fractional change in 1984 transit detections simulated by Sullivan et al. (2015) produced by a single star randomly selected from a background stellar population synthesized by TRILEGAL for l = 90, b = 30. Bottom panel: contrast ratio in the V band between host and background stars versus transit depth difference. Points are colour coded according to the T_{eff} of the host star, with red points representing cooler stars.

We calculated the fractional difference in transit depth using equation (6) and plot this versus the contrast ratio in magnitudes ΔV in Fig. 3. There is the expected correlation where brighter background stars tend to produce larger deviations in transit depth. However, in only a small fraction of instances (66, 3.4 per cent) is the difference appreciable (>1 per cent). In the vast majority of cases, the interloping background star can be clearly identified by ground-based seeing-limited observations (~1 arcsec resolution). For these cases, the spectrum of the background star can be estimated based on photometric colours and hence the sign and magnitude of the expected difference in transit depth can be calculated and compared with any observed difference.

4 DISAMBIGUATION OF REFLECTED AND EMITTED RADIATION

A sufficiently hot planet emits significant radiation at visible wavelengths (Heng & Demory 2013). Placek et al. (2016) demonstrated how combined observations by *Kepler/K2* and *TESS* during a secondary eclipse by the star can be used to separate the thermal emission and reflected light from a 'hot' Jupiter. The total signal from the planet, as measured by the eclipse depth, is equal to its reflected light plus the Wien tail of the thermal emission, and for bodies with equilibrium temperature $T_{eq} \gtrsim 2000$ K, the latter is significant. The thermal component is sensitive to detector sensitivity at the reddest wavelengths and thus is larger for *TESS* than *Kepler*. We performed a similar calculation, comparing the transit depths measured by *CHEOPS* and *TESS*, the former satellite having a response function similar to that of *Kepler* (Fig. 1).

Fig. 4 demonstrates the principle of this analysis with the hot Jupiter *Kepler*-43b. This system was selected because Angerhausen, DeLarme & Morse (2015) find a negative and obviously

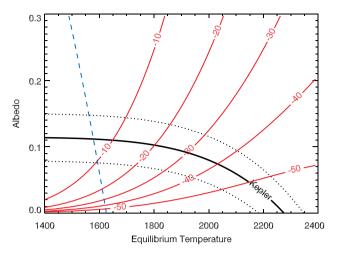


Figure 4. Possible albedo *a* versus equilibrium temperature T_{eq} for the hot Jupiter *Kepler*-43b, based on the *Kepler* secondary eclipse depth, assuming completely efficient heat redistribution (solid black line, with $\pm 1\sigma$ as dotted black lines). Theoretical predicted values are represented by the blue dashed line. The secondary eclipse depth measured by *Kepler* constraints the combination of T_{eq} and albedo *a* but there is degeneracy between the values. The red contours are the predicted per cent difference in secondary eclipse depth between *CHEOPS* and *TESS* observations, showing how a measurement can break the degeneracy.

non-physical albedo for the planet. The properties of the star were taken from Bonomo et al. (2015) and secondary eclipse parameters from Angerhausen et al. (2015). The calculation assumes blackbody thermal emission and efficient redistribution of heat around the planet. The constraint from the *Kepler*-measured secondary eclipse depth is plotted as the solid black contour in Fig. 4 with the dashed lines representing $\pm 1\sigma$. Contours of constant per cent difference between the predicted depth of the secondary eclipse in the *CHEOPS* versus the *TESS* band-passes are plotted as red lines. The dashed blue line is the theoretical value of T_{eq} assuming efficient heat redistribution. If heat redistribution is efficient, the difference between *CHEOPS* and *TESS* passband would indicate a higher day-side temperature and less-efficient heat transport to the night-side.

We calculated the CHEOPS-TESS difference in the secondary eclipse depth for the simulated planets in the Sullivan et al. (2015) catalogue, adopting a representative value of 0.1 for the albedo (Shporer & Hu 2015), blackbody emission and perfect redistribution of heat. Since the duration of the primary transit and secondary eclipse is equal for circular orbits, the photometric sensitivity to the two signals is equal and obtained by dividing the transit depth by the SNR estimated by Sullivan et al. (2015). Fig. 5 plots the expected CHEOPS-TESS difference versus the expected TESS sensitivity. The dotted line is a 5σ detection threshold, assuming that *TESS* observations limit the sensitivity.⁴ Only five planets out of nearly 2000, all hot Jupiters, are expected to have a detectable CHEOPS-TESS difference. This number will be larger if heat is not efficiently redistributed and the planets have hotter day-sides. In the Appendix, we also consider the potential for detection of differences in the relative phase in the peak of the light curve due to the non-uniform distribution of clouds on the day-side and transport of heat to the night-side.

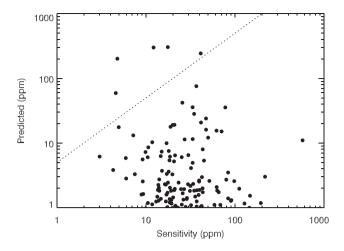


Figure 5. Predicted difference in secondary eclipse depth between *CHEOPS* and *TESS* in ppm versus the expected detection sensitivity of *TESS*, for the simulated catalogue of *TESS* detections by Sullivan et al. (2015). An albedo of 0.1, blackbody thermal emission and perfect redistribution of heat around each planet are assumed. The dotted line is a detection threshold of five times the sensitivity, and simulated planets above the line are expected to have detectable differences. Most *TESS* planets have predicted to exhibit differences of <1 ppm and are not shown.

5 TRANSMISSION SPECTRA OF PLANETS

It is possible to detect the atmosphere of a planet by comparing spectra obtained during and before/after a transit. The atmosphere manifests itself as a wavelength dependence in the transit depth and thus the apparent radius of the planet. The planet will appear larger at wavelengths where constituents in its atmosphere absorb or scatter some of the light of the host star. Atoms and molecules will absorb at discrete wavelengths, whereas the Rayleigh scattering by these and particles in hazes/clouds can produce a larger apparent radius at bluer wavelengths and a negative spectral slope. This wavelength dependence, integrated over the total response function of individual observatories, can produce differences in apparent transit depth. The magnitude of this effect depends on the scale height of the atmosphere and the spectrum of the host star, which effectively 'weights' different wavelengths.

We calculated the difference in transit depth between *CHEOPS* and *TESS* for the reference case of a GJ 1214b-like planet $(R_p = 2.6 \text{ R}_{\oplus}, M_p = 6 \text{ M}_{\oplus})$ but with a solar-composition atmosphere (mean molecular weight $\bar{\mu} = 2.33$), and a T_{eq} of 1000 K. The ratio h/R_p is 0.023. We considered several different atmosphere scenarios with solar composition: two 'clear' atmospheres with no hazes or clouds, with and without H₂O vapour and six hazy atmospheres with characteristic particle sizes r_{part} of 0.01, 0.05 and 0.1 µm, and cloud/haze-top pressure heights z_{cloud} of 1 µbar and 1 mbar. We considered a range of host star spectra, that is, T_{eff} of 3000–7000 K with solar metallicity and main-sequence surface gravity as proscribed by the empirical M_*-R_* relation of Pecaut & Mamajek (2013).

The fractional transit depth difference is plotted versus $T_{\rm eff}$ in Fig. 6. In all cases with $T_{\rm eff} > 3000$ K, the *CHEOPS* transits are deeper (the difference is positive) because a planet's atmosphere is usually more opaque and/or scattering at shorter wavelengths where *CHEOPS* is more sensitive. The difference increases with increasing stellar $T_{\rm eff}$ because hotter stars have more flux at $\lambda < 580$ nm, where *CHEOPS* but not *TESS* is sensitive. The calculations using empirical

⁴ The SNR of a *single CHEOPS* transit observation is expected to be similar to that of the total *TESS* photometry.

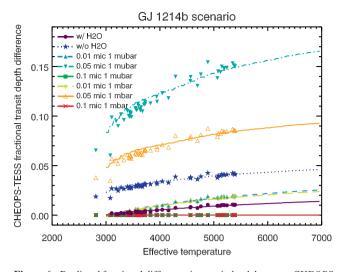


Figure 6. Predicted fractional difference in transit depth between *CHEOPS* and *TESS* for a planet with the surface gravity of GJ 1214b and an equilibrium temperature of 1000 K. Eight different atmosphere scenarios are considered; two clear atmosphere with and without water, and six hazy atmosphere with different particle size and haze heights. The curves are based on PHOENIX model spectra and the points are based on actual flux-calibrated spectra of K and M dwarfs.

spectra (points in Fig. 6) confirm the calculations based on models of stellar spectra and show that the variations due to stellar metallicity and surface gravity are modest.

Transits of planets with clear atmospheres lacking clouds or hazes will appear similar (<5 per cent difference) in observations by *TESS* and *CHEOPS*. This is particularly true of clear atmospheres with H₂O vapour, which heavily absorbs at the reddest wavelengths and balances the molecular Rayleigh scattering at shorter wavelengths. Atmospheres with aerosols dominated either by 0.01 µm or 0.1 µm particles also do not produce much of a difference in transit depth. Atmospheres containing a haze with a 0.05 µm particles generate the largest differences (up to ≈15 per cent), with the higher haze (1 µbar pressure height) producing the largest signal. Aerosols of this size are efficient Rayleigh scatterers at wavelengths probed best by *CHEOPS* but inefficient at the redder wavelengths sensed by *TESS*.

In principle, the fractional contribution of a homogeneous absorbing/scattering atmosphere to the transit depth should be proportional to h/R_p , thus the fractional difference in transit depth due to an atmosphere should also scale linearly with that ratio. We tested this assumption by performing the same calculation for the Earth-size planet *Kepler*-289d, which has an estimated h/R_p larger by a factor of 1.58 than GJ 1214b (assuming identical T_{eq} and atmospheric composition). We used the GJ 1214b and *Kepler*-289d results to calculate a power-law index β that equates the ratio of h/R_p values to the ratio of *CHEOPS-TESS* difference Δ , that is, $\Delta \propto (h/R_p)^{\beta}$. $\beta = 1$ represents linearity. Fig. 7 plots β as a function of stellar T_{eff} for the eight different scenarios. The reader is reminded that this is the *scaleheight dependence* of the difference in transit depth, not the difference itself.

Several scenarios follow approximate linearity ($\beta \approx 1$). These include the clear, H₂O-free atmosphere in which Rayleigh scattering dominates at visible wavelengths. Hazy atmospheres containing particles with $r_{part} = 0.01 \,\mu\text{m}$, which act as Rayleigh scatterers at all wavelengths, have similar behaviour. Intermediatesize particles ($r_{part} = 0.05 \,\mu\text{m}$) act as Rayleigh scatterers only at shorter wavelengths, but produce a flat spectrum at longer wavelengths. This introduces a spectral dependence on the

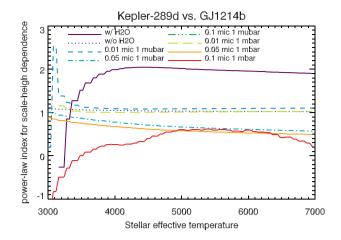


Figure 7. Power-law index β relating the predicted fractional difference in transit depths observed by *CHEOPS* and *TESS* to the ratio of scaleheight to planet radius h/R_p . These use the calculations for planets with the masses and radii of *Kepler*-289d and GJ 1214b, but with solar metallicity atmospheres. $\beta = 1$ is the linear dependence predicted for a simple scattering/absorbing atmosphere. See text for an explanation of deviations from non-linearity and dependence on stellar T_{eff} .

signal and a slow change with $T_{\rm eff}$. In the atmosphere with large $(r_{\rm part} = 0.1 \,\mu{\rm m})$ haze particles at high altitude $(z_{\rm cloud} = 1 \,\mu{\rm bar})$, all spectral features are obscured. There is no difference between *CHEOPS* and *TESS* observations because the spectrum is flat at all wavelengths and the scaleheight dependence is ill-defined. In an atmosphere with particles confined to a lower pressure altitude $(z_{\rm cloud} = 1 \,{\rm mbar})$, the only atmospheric features are the resonant absorption lines of neutral sodium and potassium doublets near 589 and 768 nm; these produce some difference in the transit depth. The individual contributions of the lines at different wavelengths also make the signal dependent on the stellar spectrum and hence $T_{\rm eff}$.

6 DETECTING THE HAZY ATMOSPHERES OF *TESS* PLANETS

The possibility that planets with hazy atmospheres can exhibit significantly different transit depths in *CHEOPS* and *TESS* observations motivated an estimate of the total number of *TESS*-detected planets with detectable differences. We calculated the transit depths that *CHEOPS* and *TESS* would observe for the planets in the simulated detection catalogue of Sullivan et al. (2015).

The spectral difference will depend on R_p , h, T_{eq} , r_{part} , z_{cloud} , the composition of the atmosphere and the stellar spectrum (i.e. T_{eff}). For a homogeneous scattering or absorbing atmosphere, the fractional difference in transit depth due to the atmosphere scales as h/R_p . This assumption clearly fails for certain atmospheres, e.g. atmospheres with large hazes sizes, hazes at low altitude and clear atmospheres containing H₂O vapour (Fig. 7). But in such cases, the difference in transit depth is small and probably not detectable, regardless.

We performed a set of calculations with different values of h/R_p for high altitude haze particles to demonstrate the approximate linear dependence for the most detectable cases. If this scaling holds, one can estimate the signal from any planet by calculating h/R_p and scaling the fractional transit depth difference determined for a reference case, that is, a GJ 1214b-like planet. Fig. 8 shows the case for $r_{part} = 0.01$ and 0.05 µm, all for $z_{cloud} = 1$ µbar, solar metallicity

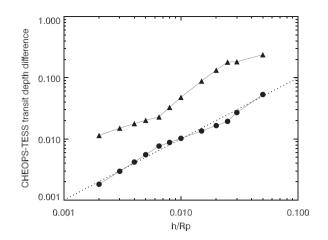


Figure 8. Fractional difference in *CHEOPS-TESS* transit depth versus atmospheric scaleheight to planet radius ratio h/R_p for planets having solar metallicity atmospheres with hazes with $z_{cloud}1$ µbar pressure height. The top and bottom curves are for $r_{part} = 0.05$ and 0.01 µm hazes, respectively.

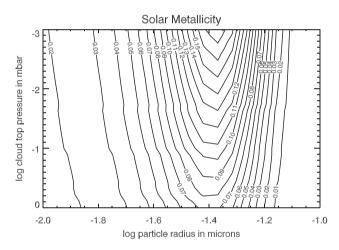


Figure 9. Fractional difference in *CHEOPS-TESS* transit depth versus haze parameters for a planet with $T_{\rm eq} = 1000$ K, $h/R_{\rm p} = 0.023$, a solar metallicity atmosphere ($\bar{\mu} = 2.33$) and a solar-type spectrum for the host star.

composition and $T_{eq} = 1000$ K. The best-fitting power-law indices are 0.96 and 1.09, respectively, demonstrating linearity.

We next calculated the *CHEOPS-TESS* difference in transit depth for the reference case (GJ 1214b, 1000 K) and ranges of haze particle sizes and pressure altitudes. Figs 9 and 10 show the results for a solar metallicity composition ($\mu = 2.33$) and 10 × solar metallicity composition, using a solar-type host star. These show the expected sensitivity to particle size, with ~0.04 µm particles producing the maximum signal, as well as the dependence on pressure height, with higher hazes intercepting more starlight and producing a greater difference. Also as expected, more metal-rich atmospheres have a smaller scale height and generate a smaller signal. Since Rayleigh scattering occurs only at wavelengths less than the particle size, there is also a dependence on the host star spectrum: the particle size producing the maximum difference is longer for planets transiting cooler stars that emit more at longer wavelengths.

The number of simulated *TESS*-detected planets with a detectable difference in *CHEOPS* and *TESS* transit depths was calculated for a range of haze particle sizes and pressure heights. Detection was assumed to require SNR > 5, with the *TESS* signal to noise calculated by Sullivan et al. (2015) and assuming unlimited *CHEOPS*

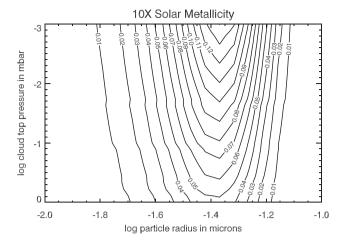


Figure 10. Same as Fig. 9 but for planet atmospheres with $10 \times \text{solar}$ metallicity ($\bar{\mu} = 2.56$).

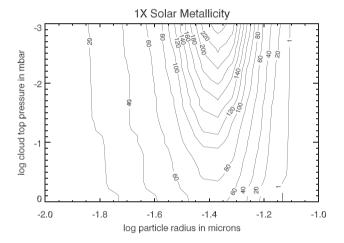


Figure 11. Number of significant (5σ) detections of a difference between *CHEOPS*- and *TESS*-measured transit depths for the simulated catalogue of *TESS* planet detections by Sullivan et al. (2015), assuming every planet has a hazy atmosphere, versus characteristic haze particle size and haze (cloud-top) altitude. A solar metallicity atmosphere is assumed.

signal to noise. The scaleheight for each planet was calculated assuming the radius given by Sullivan et al. (2015), a mass from the mass–radius relation of Chen & Kipping (2017), T_{eq} was calculated using the irradiance level given by Sullivan et al. (2015) and assuming an albedo of 0.1. The difference in transit depths was calculated using a grid of transit depth differences with particle size and cloud-top height calculated for the nominal GJ 1214b-like case with $T_{eq} = 1000$ K and solar metallicity atmosphere (h/R = 0.023), and assuming linear scaling with h/R as demonstrated in Fig. 8.

Figs 11 and 12 plot the numbers and distribution of atmosphere detections versus haze parameters, assuming every planet has such an atmosphere. The distribution reflects the magnitude of the signal in Fig. 9 and peaks at 262 detections, or about 13 per cent of the total. The overall yield is sensitive to the heavy element abundance of the atmosphere via its influence on the scaleheight, but the trend is not monotonic because of the effect on atmospheric opacity as well. In the case of atmospheres with 10 × solar metallicity ($\bar{\mu} = 1.56$), the distribution is similar (Figs 13 and 14), but the numbers are smaller (Fig. 10) and peak at 155. For $30 \times (\bar{\mu} = 3.02)$ and $50 \times (\bar{\mu} = 3.48)$ solar metallicity, the distributions (not shown) peak at 179 and 143,

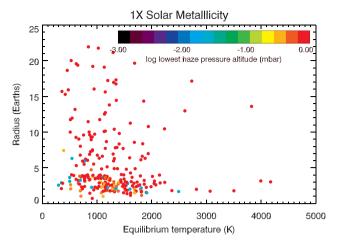


Figure 12. Equilibrium temperature and radius of planets with significant detections of a difference in the *CHEOPS* and *TESS* transit depths from the Sullivan et al. (2015) for any of the haze scenarios considered in Fig. 11. The colour of the point is coded to the lowest pressure altitude (largest pressure) of the cloud-top at which the haze could still be detected.

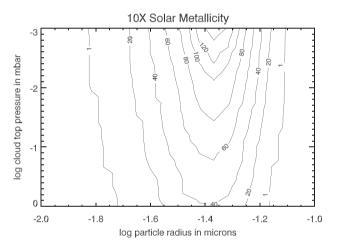


Figure 13. Same as Fig. 11, except for atmospheres with $10 \times$ solar metallicity.

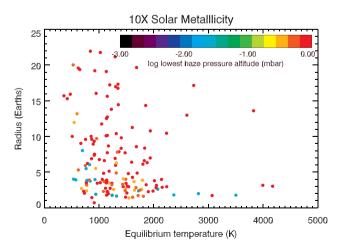


Figure 14. Same as Fig. 12, except for atmospheres with $10 \times \text{solar}$ metallicity.

respectively. Note that these last three numbers do not differ by amounts much larger than the expected variance due to counting statistics.

7 SUMMARY AND DISCUSSION

We have examined three ways in which differences in the response function of *CHEOPS* and *TESS* will manifest themselves. First, a blended companion star or unrelated background star with a different $T_{\rm eff}$ and spectrum will produce a difference in transit depth with a sign that depends on whether the planet orbits around the principal target star or the companion/background star. However, this effect is predicted to be both rare and minor. While unrelated blends are likely for *TESS* (21 arcsec pixels), they are very unlikely for *CHEOPS* (1 arcsec pixels). Regardless, simulations suggest that in only 3.4 per cent of cases will the effect exceed 1 per cent. Companion stars (separations of a few au or less) that are unresolved both by *TESS* and *CHEOPS* can give rise to transit depth differences of up to 3 per cent (maximal when the secondary star is ~800 K cooler than the primary).

Secondly, a difference in the secondary eclipse depth of a hot Jupiter as measured by *CHEOPS* and *TESS* can be used to disambiguate the reflected light from the planet and its thermal emission. Among the catalogue of 1948 predicted *TESS* detections by Sullivan et al. (2015), for only ~5 planets will the expected difference in eclipse depth significantly exceed the *TESS* photometric error alone. However, since the contribution of thermal emission to the transit depth is important in each of those cases, observations of these by *CHEOPS* should be a priority.

Thirdly, the presence of an atmosphere around a planet can produce a difference in the transit depths and since atmospheres are more opaque/scattering at shorter wavelengths, the transit depth observed by CHEOPS, which is more sensitive to bluer light, will be slightly deeper than that observed by TESS. The effect will be negligible if the atmosphere has a haze/cloud of very small or large particles, or is clear but has significant water vapour that 'flattens' the effect by the Rayleigh scattering. A larger difference can occur if the planet is both dry and haze/cloud free. Since water is presumed to have accreted as ice in small planets, if the close-in planets detected by TESS lack water, it is an indication that they accreted inside the 'ice line' rather than migrating inwards from outside. The largest differences occur for hazy atmospheres containing particles with a characteristic size of $\sim 0.05 \,\mu\text{m}$. If each TESS-detected planet possessed such an atmosphere, we estimate that ~ 100 would be detected by comparing TESS and CHEOPS photometry, depending on the atmospheres' heavy element abundance.

The hazes detected by a comparison of CHEOPS and TESS photometry do not preclude investigation of the atmospheres at the longer wavelengths to be probed by JWST and ARIEL. Fig. 15 plots three normalized model transit spectra, all for a GJ 1214b analogue with a solar metallicity atmosphere, $T_{eq} = 1000$ K, and a 1 µbar cloud top, but with three different particle sizes. The intermediatesize particles (middle, yellow curve) produce the largest CHEOPS-TESS signal, while the smaller and larger particle sizes are essentially undetectable. The 0.043 µm haze particles have a negligible effect on the strength of the H₂O and other molecular bands in the infrared. Therefore, detection of the Rayleigh scattering by CHEOPS+TESS is a valid selection criterion for targets for JWST or ARIEL. On the other hand, non-detection does not necessarily mean that the planets lack an atmosphere that could be observed in the infrared (e.g. very small haze particles, no haze at all and/or very high mean molecular weight).

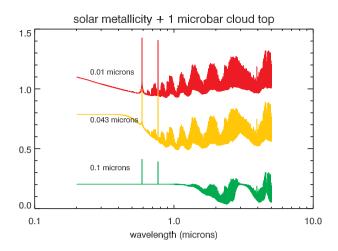


Figure 15. Three simulated, normalized transmission spectra of a GJ 1214b with a hazy solar metallicity atmosphere. The cloud top is at 1 µbar in each case, but the particle sizes differ. Only the intermediate-particle size (0.043 µm) case produces a detectable difference in *CHEOPS-TESS* transit depths, but the haze does not significantly affect the strength of molecular bands at infrared wavelengths.

Other astrophysical effects and systematic errors could produce differences in the transit depth as measured by the two observatories. These include wavelength-dependent limb darkening; at the shorter wavelengths to which CHEOPS is more sensitive than TESS, the limb of a star is darker relative to the centre of the disc. This will make a transit with a non-zero impact parameter appear shallower in CHEOPS data. This will produce a negative CHEOPS-TESS transit depth difference. A star-spot that is crossed by the planet during the transit that is observed by TESS but not by CHEOPS(or vice versa) can cause a difference of either sign, but these events are often obvious since the spot crossing time is much shorter than the transit duration. Non-occulted spots on the stellar disc will cause the transit signal to be deeper at bluer wavelengths, thus mimicking the effect of the Rayleigh scattering in a planet's atmosphere (Oshagh et al. 2014). This is a potentially serious problem for transit spectroscopy in general, but might be controlled by constraining the spot distribution by other observations. Finally, there may be a systematic instrumental offset between CHEOPS and TESS, although this can be identified and removed if enough transiting systems are observed.

As shown in Fig. 1 and discussed by Angerhausen et al. (2015), the band-pass of Kepler/K2 is similar to that of CHEOPS and in principle the same analyses could be performed using TESS and Kepler/K2 data. However, the Kepler prime mission observed only $\approx 115 \text{ deg}^2$ of the sky and only a handful of overlapping detections. K2 is restricted to the ecliptic plane that the primary TESS mission will not observe. Comparison of TESS observations with the PLATO mission (Rauer et al. 2014), scheduled for launch in 2025, will provide a more promising avenue for intercomparison. PLATO will observe several short-duration (~3 month) and long-duration (up to 2 yr) fields. The response functions of the PLATO cameras are not yet determined, but all but two will operate without a filter and should have a total response function similar to that of Kepler and CHEOPS. Two high-cadence cameras will have distinct red and blue filters, which will offer colour information for systems in a more limited part of the sky.

Ground-based transit photometry can be performed through a passband that has little or no overlap with *TESS*, e.g. *V* or *JHK*, allowing larger signals to be detected, albeit with less accuracy. We

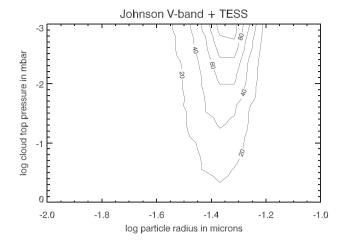


Figure 16. Numbers of 5σ -detected hazy, solar metallicity atmospheres ($T_{eq} = 1000 \text{ K}$) around all simulated *TESS*-detected planets in the catalogue of Sullivan et al. (2015), based on the expected difference between transit depths measured by *TESS* and ground-based observations through a Johnson *V* filter.

calculated the fractional difference in transit depths between TESS and Johnson V band for the scenario of a hazy atmosphere on a GJ 1214b-like planet. We then calculated the number of possible detections among the Sullivan et al. (2015) catalogue of simulated TESS planets. We assumed 10^{-3} photometry per 1 min observation and a reduction in noise with observation time t as $t^{-0.3}$. The use of -0.3 as the exponent rather than -0.5 for uncorrelated ('white') noise reflects the importance of correlated (red) noise in limiting ground-based observations (Pont, Zucker & Queloz 2006). These parameters produce a median photometric accuracy over the transit interval of 230 ppm, consistent with the best performance achieved on 10-metre class telescopes (Nortmann et al. 2016), but well short of the predicted median of 120 ppm for TESS observations (Sullivan et al. 2015). Numbers of detected hazy, solar-composition atmospheres ($T_{eq} = 1000$ K) versus particle size and cloud-top height are plotted in Fig. 16. Even with this optimistic assumption for photometric accuracy, the numbers of detection are reduced by a factor of ~ 2 (maximum of 102) compared to CHEOPS observations. This illustrates one limitation of ground-based compared to space-based observations: others are weather and nocturnal observing windows.

An alternative is to fly an observatory capable of transit and eclipse multiwavelength photometry or spectroscopy on a large number of exoplanets. The proposed *ARIEL* mission, which is one of three candidate European Space Agency *M3* missions for possible launch in 2026, would observe several hundred systems. Selection of *TESS* targets based on a *CHEOPS-TESS* intercomparison would improve the scientific yield of such a mission.

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APPENDIX: DETECTION OF WAVELENGTH-DEPENDENT PHASE OF LIGHT-CURVE MAXIMA

In addition to detecting differences in the depth of secondary eclipses with different band-passes, it might be possible to detect differences in the phase of the maximum in the emitted plus reflected light curve of the planet with respect to the secondary eclipse. These phase shifts are thought to be produced by equatorial jets on the rotating planet; heat is advected from the day-side over the eastern terminator to the night-side, causing the maximum in the thermal signal to lead the secondary effects, and clouds that form on the cooler night-side being advected over the western terminator to the day-side, causing the maximum in the reflected signal to lag the secondary eclipse (e.g. Shporer & Hu 2015). For hot Jupiters where the observed signal is a mixture of reflected and emitted light, these two effects act against each other. However, inspection of the phase curves in two passbands that have different relative contributions of thermal and reflected signal, could show a shift.

Approximating the normalized phase curve in passband A as the sum of two (reflected and thermal) sinusoidal signals shifted by θ ,

$$s(\theta) = \cos(\phi) + r\cos(\phi + \theta), \tag{A1}$$

where r is the relative contribution of the thermal signal to a particular passband. This function peaks at

$$\phi = -\arctan\frac{r_A \sin\theta}{1 + r_A \cos\theta},\tag{A2}$$

The relative shift $\delta \phi$ due to a small difference Δr between two passbands is approximately

$$\delta\phi \approx \frac{\delta r \sin\theta}{1 + 2r \cos\theta + r^2}.$$
(A3)

Assuming the values for the Kepler-43 system and $\theta \sim 100$ deg, based on Angerhausen et al. (2015), then *r* is 0.31 and 0.09 for *TESS* and *CHEOPS*, respectively, and the phase difference $\phi \approx$ 13 deg, which might be detectable; fits with *Kepler* data typically have errors of a few degrees (Angerhausen et al. 2015).

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