Combination of Swarm gravity field models on normal equation level

ESA/DISC project "Multi-approach gravity field models from Swarm GPS data"

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Outline

- 1. Multi-approach gravity field models from Swarm GPS data
- 2. Combination strategy
- 3. Combination at normal equation level
- 4. Conclusion



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 - AIUB: Celestial Mechanics Approach
 - ASU: Decorrelated Acceleration Approach
 - IfG: Short-Arc Approach
 - OSU: Improved Energy Balance Approach (not considered here)

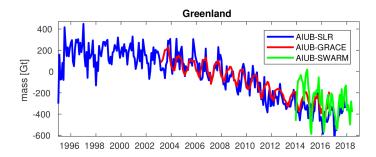


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- GRACE-derived mass variations serve as reference
- All gravity fields truncated at degree 6 (max. resolution of SLR), no extra filter applied
- Swarm results: more noisy and larger signal amplitude (unknown reason)



Same kinematic orbits, different ACs

 Combination is based on the assumption that all contributions contain the same signal but differ in noise

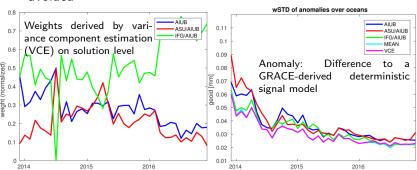
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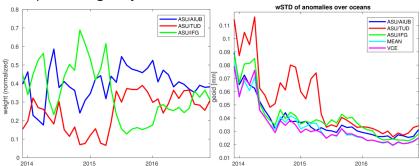


 The combination (on solution level) based on AIUB kin. orbits shows advantages for the IfG processing strategy



Same AC, different kinematic orbits

Example: ASU gravity fields based on different kinematic orbits

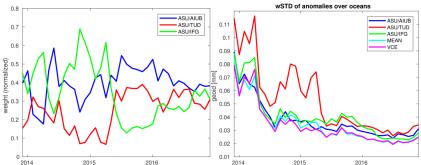


 Advantages for IfG orbits during periods of high solar activity, for AIUB orbits during periods of reduced solar activity or improved tracking



Same AC, different kinematic orbits

Example: ASU gravity fields based on different kinematic orbits



- Advantages for IfG orbits during periods of high solar activity, for AIUB orbits during periods of reduced solar activity or improved tracking
- TUD orbits suffer from artifacts due to ionospheric disturbances during times of high solar activity



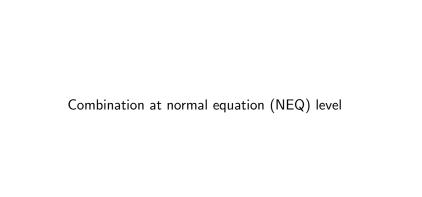
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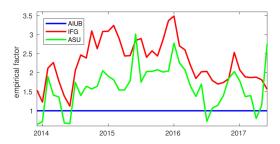
- Optimal in terms of biases would be a combination of all independent analysis centers and input kinematic orbits
- If certain orbits show pronounced problems, the AC processing these orbits will get lower weights (unattractive)





Relative weighting/scaling of NEQs (1)

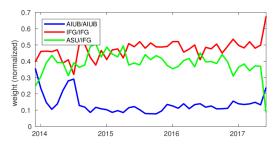
- Only apply one scaling factor per time series to keep relative accuracy information between months





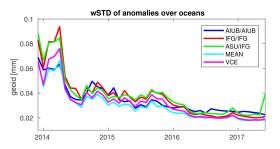
Relative weighting/scaling of NEQs (2)

Weights derived from VCE (on solution level):



- Weights are biased, since kinematic orbits are used unevenly (2×IfG, 1×AIUB) → AIUB solution systematically differs from other solutions and gets downweighted
- Not applied for final combined solutions

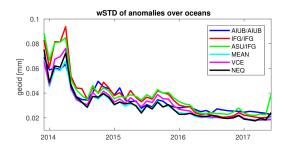
Validation: noise over ocean areas



• Combination on solution level: VCE is not optimal (orbit bias) and is out-performed by the arithmetic mean

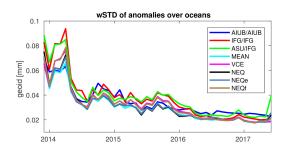


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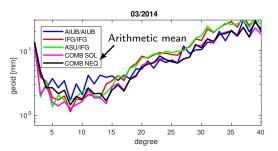
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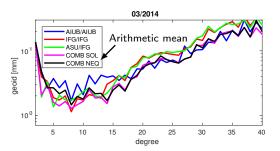
- Combination on solution level: VCE is not optimal (orbit bias) and is out-performed by the arithmetic mean
- The arithmetic mean at NEQ level closely resembles the arithmetic mean at solution level
- Applying VCE-based weights at NEQ-level (NEQf) closely reproduces the combination by VCE at solution level.
- Introduction of monthly empirical scaling factors (NEQe) will not result in significant improvement



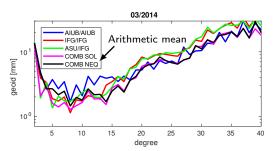


• At high degrees the two combined solutions are very comparable



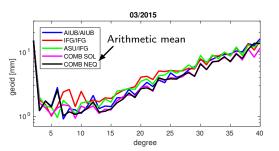


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- At low degrees the combination on NEQ level is driven by the AIUB solution, which has unrealistically small formal errors at low degrees



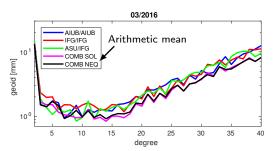
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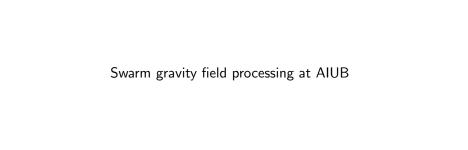


Conclusions

- Swarm kinematic orbits from different processing centers show different performances, depending on ionospheric activity
- An unbiased combination of Swarm-derived gravity fields from different ACs requires a homogeneous use of kinematic orbits, otherwise VCE will downweight solutions which are derived from underrepresented kinematic orbits
- At low degrees combination on NEQ level is dominated by AIUB solution due to its (too) low formal errors. This is problematic during high ionospheric activity, where the AIUB solutions are degraded in the lower degrees
- → Tests with revised strategies to mitigate ionosphere-induced artifacts in AIUB orbits on-going (however, seems to improve mainly higher degrees)

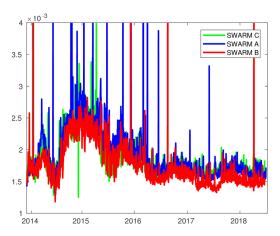






Quality control (1)

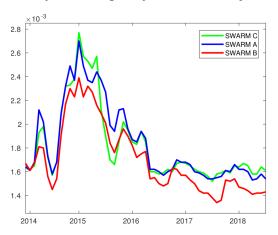
Daily RMS of orbit fit reflects ionospheric disturbances due to solar activity:





Quality control (2)

So does the monthly RMS of gravity field model adjustment:

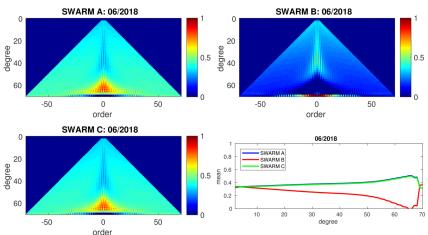




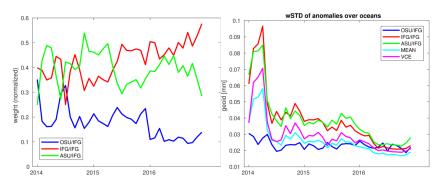
Daniel Arnold: Combination of Swarm gravity field models on normal equation level 8th Swarm Data Quality Workshop, 08-12 October 2018

Contribution analysis

Contribution of individual Swarm satellites to monthly gravity field solutions:



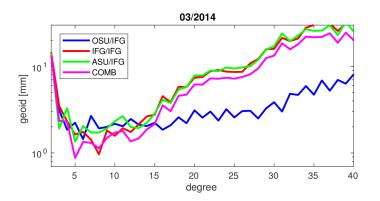




- Combination by Variance Component Estimation (VCE) on solution level (convergence after 3-4 iterations)
- Noise is evaluated independently by variability over ocean areas
- Low weights together with low noise indicate damaged signal



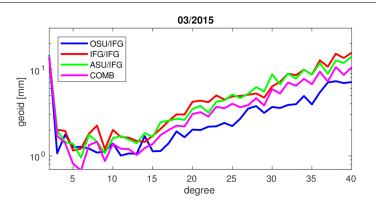
Quality checks of individual contributions (2)



 OSU time series biased towards static GRACE a priori model due to use of satellite velocities taken from dynamic orbits



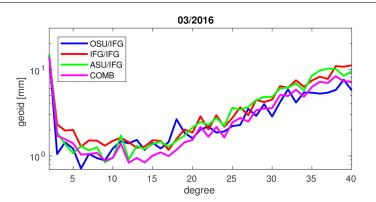
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- With decreasing noise in 2015 and 2016 the regularization of OSU gravity fields is less obvious, but correlation analysis with GRACE solutions still reveals attenuated signal content

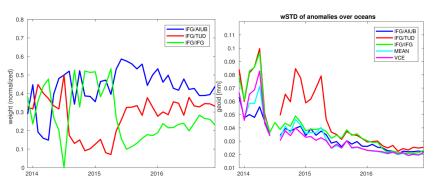


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Example: IfG gravity fields based on different kinematic orbits



 Combination of IfG gravity fields based on different kinematic orbits confirms the findings of the ASU combination

