

# SLR, GRACE and SWARM gravity field determination and combination

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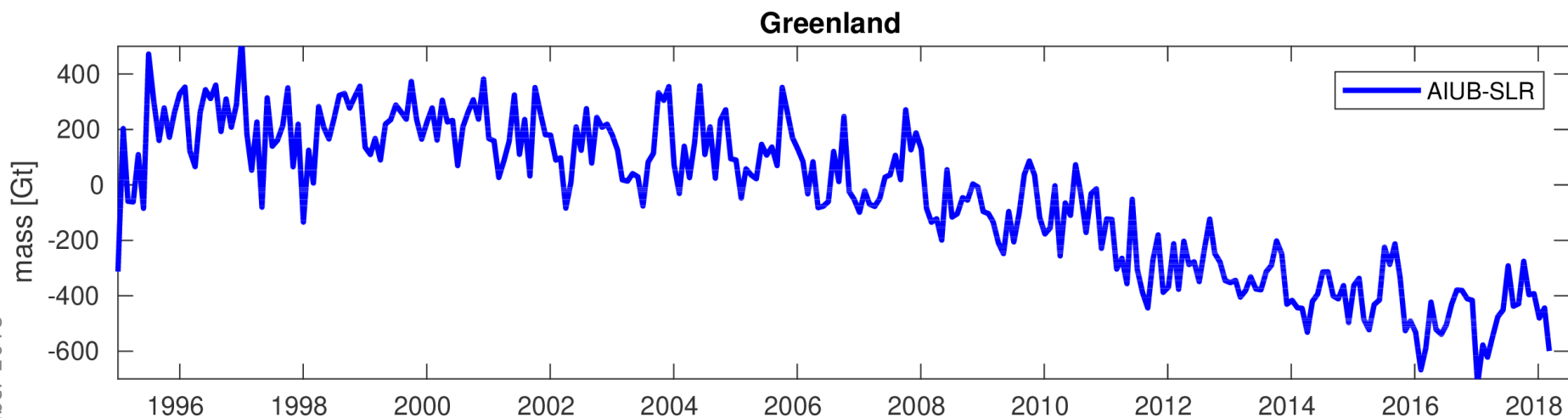
ILRS Workshop Canberra, 05 November 2018

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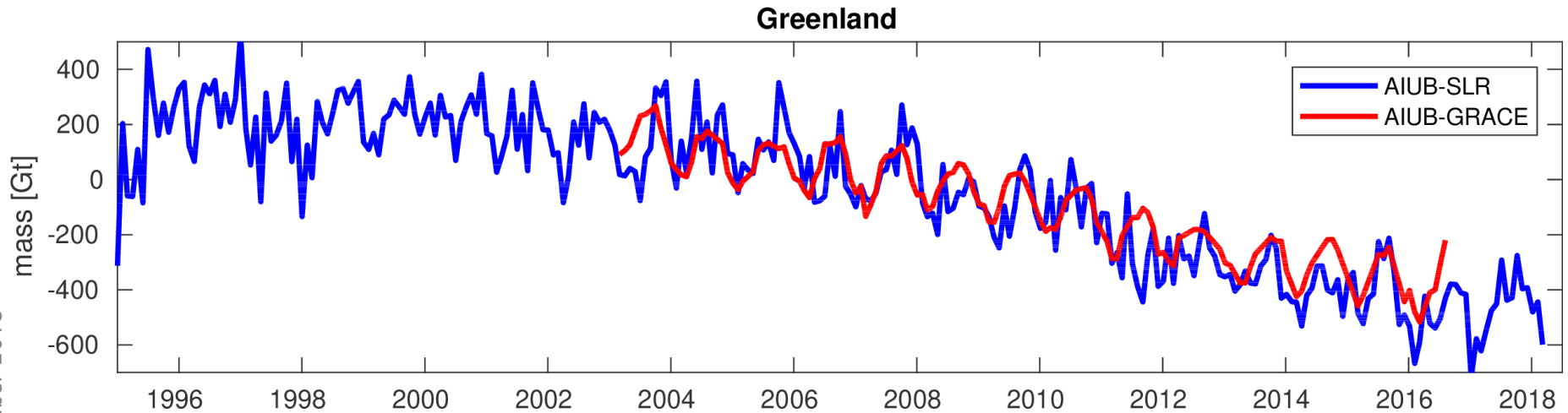
- **Monthly mass variations in Greenland:**
  - SLR
  - GRACE
  - SWARM
- **Interpretation:**
  - Spatial resolution
  - Spectral leakage
- **Combination of normal equations:**
  - SWARM + SLR
- **Summary and Outlook**

# Ice melt in Greenland from SLR



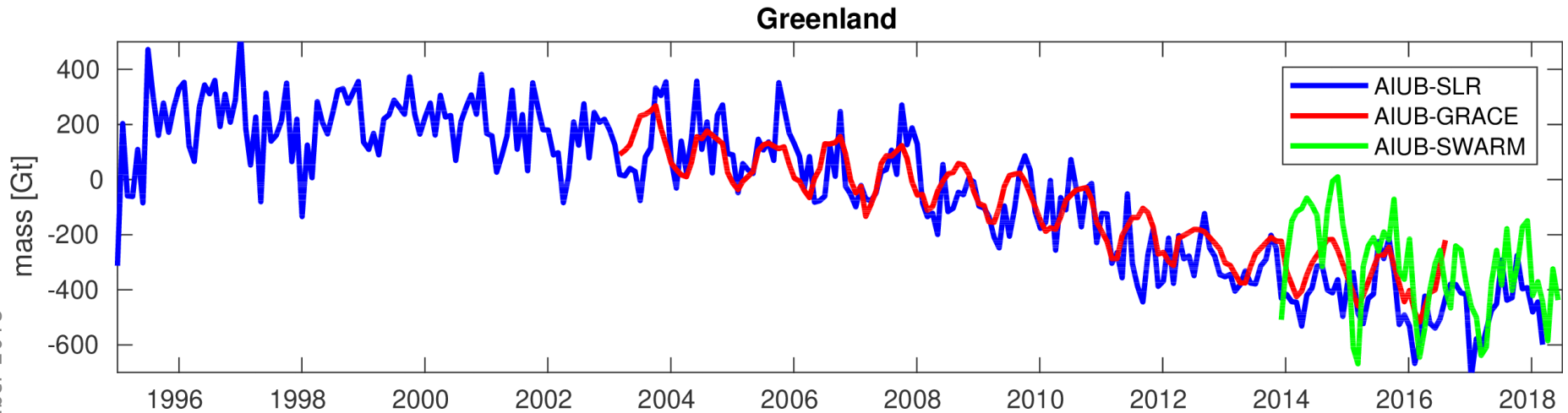
- **LAGEOS 1+2: 30 d solutions based on 10 d arcs.**
- **SLR-LEOS (Beacon-C, Ajisai, Starlete, Stella, Larets, Lares): 30 d solutions based on 1 d arcs.**
- **Gravity field:  $5 \times 5 + C_{61}$  and  $S_{61}$ ;  $C_{50}$  constrained.**
- **A priori gravity: static 7 y GRACE (AIUB-APR).**
- **A priori orbits: LAGEOS own predictions, LEOS CPF**

# Ice melt in Greenland from GRACE



- **GRACE GPS+K-band: monthly 90 x 90 gravity field solutions, truncated at degree / order 6.**
- **Degree 2 excluded.**
- **Degree 1 fixed to 0.**
- **No filter applied.**

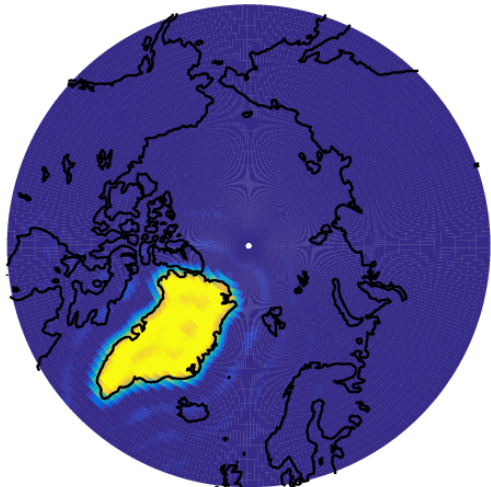
# Ice melt in Greenland from SWARM



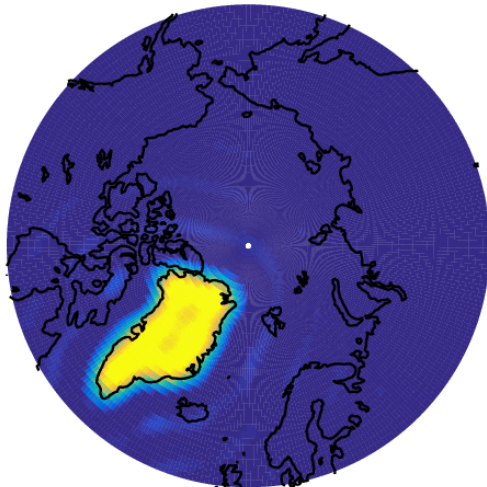
- **SWARM GPS: monthly 70 x 70 gravity field solutions, truncated at degree / order 6.**
- **Degree 2 excluded.**
- **Degree 1 fixed to 0.**
- **No filter applied.**

# Spatial resolution and leakage

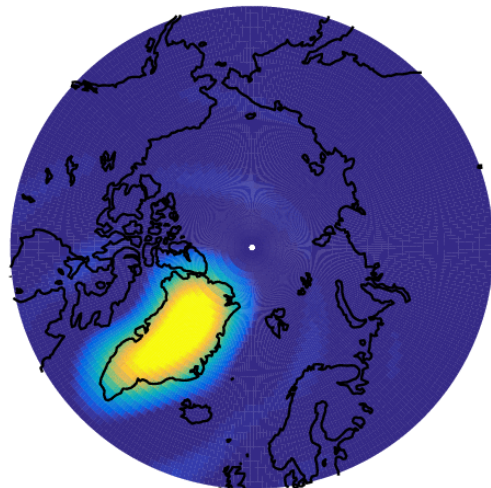
reproduced mass (90): 94%



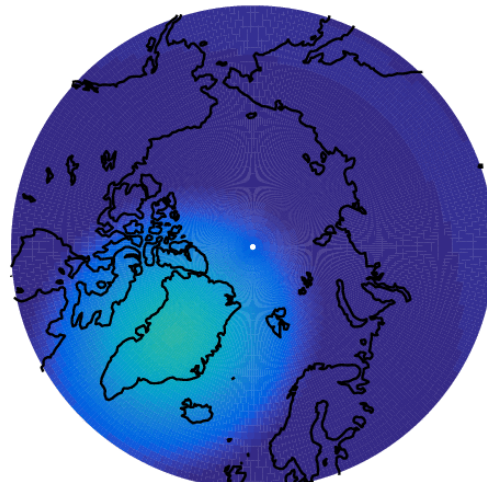
reproduced mass (60): 91%



reproduced mass (30): 82%



reproduced mass (10): 40%

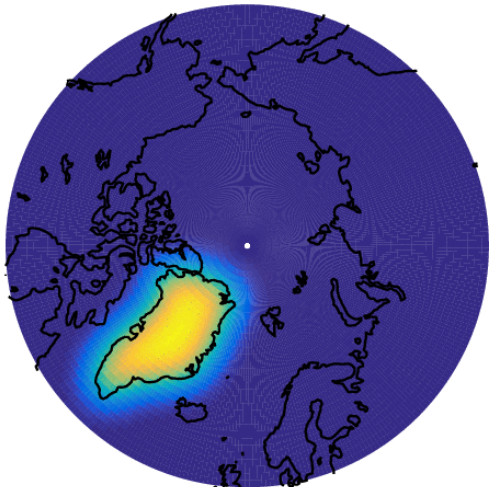


- The truncation of a spherical harmonic expansion leads to signal leakage.
- Sensitivity for monthly mass variations:
  - GRACE : 60–90
  - SWARM: 12–20
  - SLR: 6–10
- With knowledge about the original mass distribution leakage can be corrected by scaling.

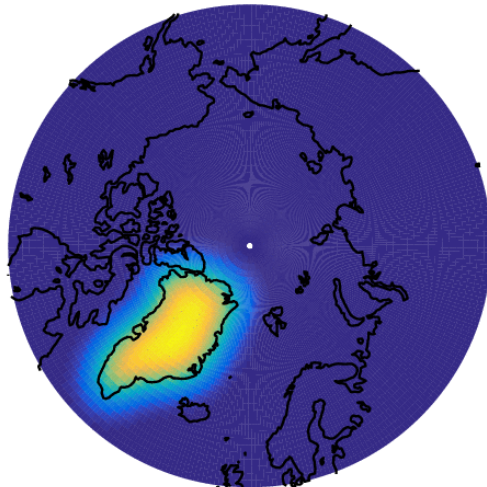


# Spatial resolution and leakage

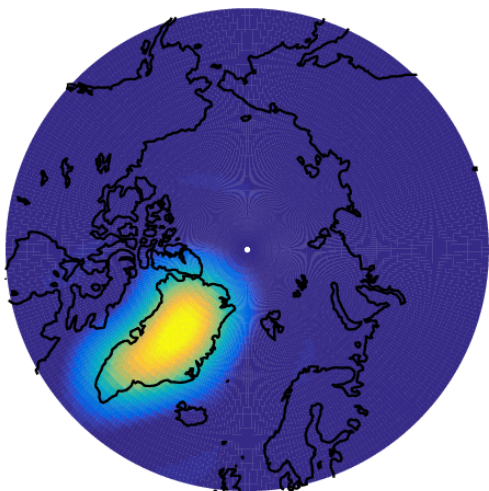
reproduced mass (90): 73 %



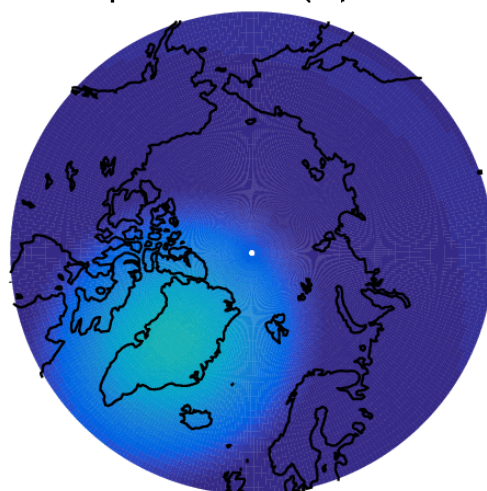
reproduced mass (60): 73 %



reproduced mass (30): 71 %

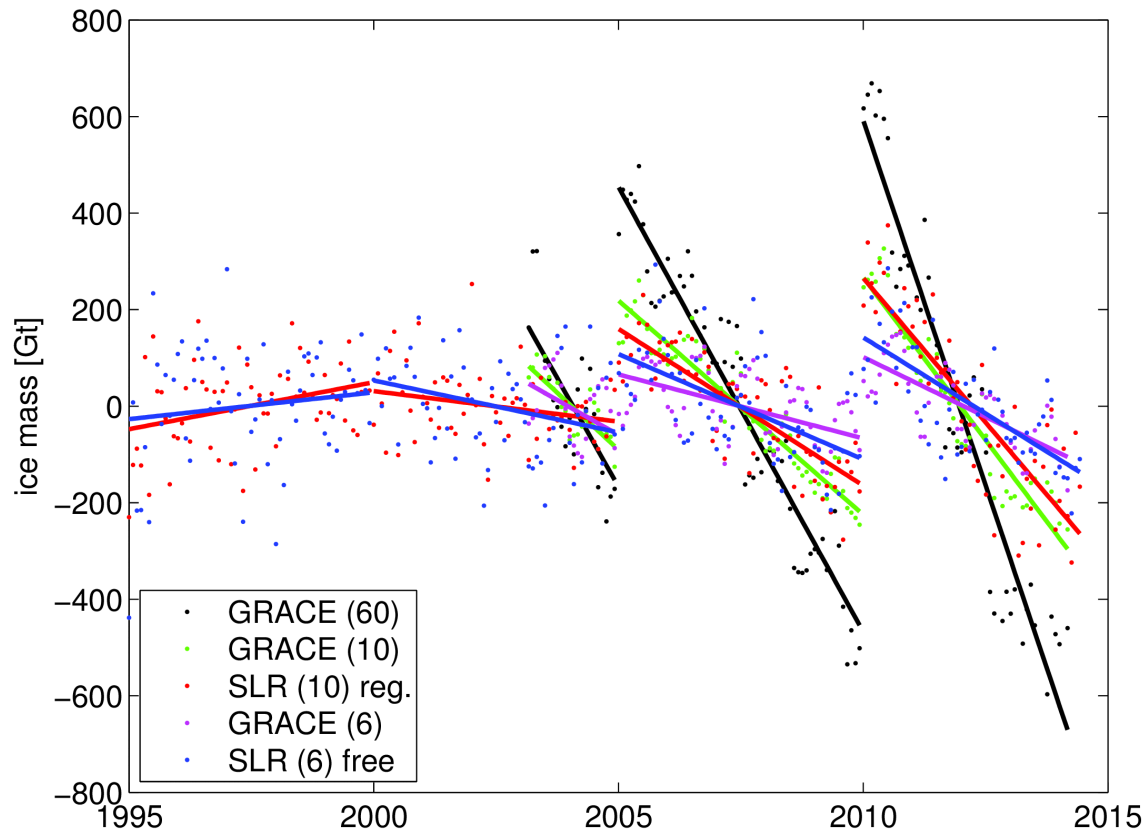


reproduced mass (10): 38 %



- Common filters (e.g. Gauss 300km ) lead to drastic leakage even for GRACE.
- All signal above degree 60, and significant signal above degree 30 is attenuated!
- In case of SLR no filter is applied.

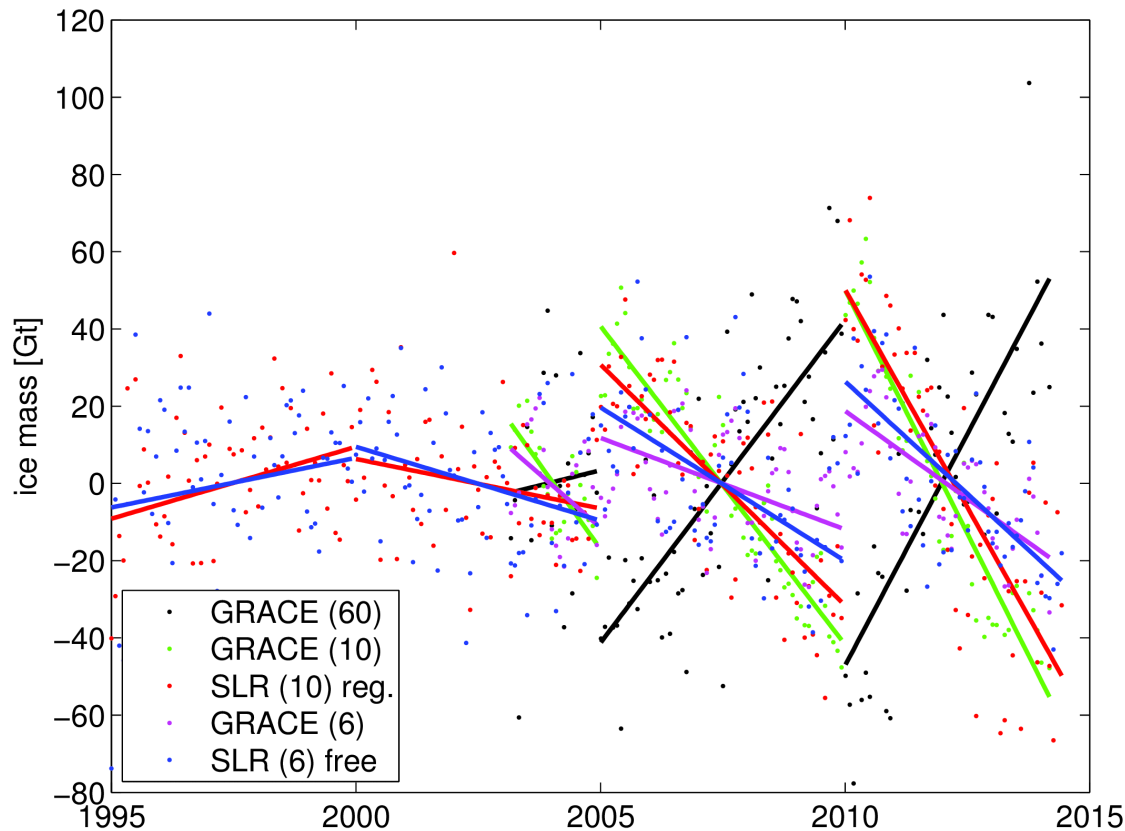
# Ice mass change: Greenland Coast



- SLR and GRACE provide consistent mass trends when truncated at the same degree / order.
- By scaling, the original amount of mass loss can be recovered almost completely (but not the spatial detail).



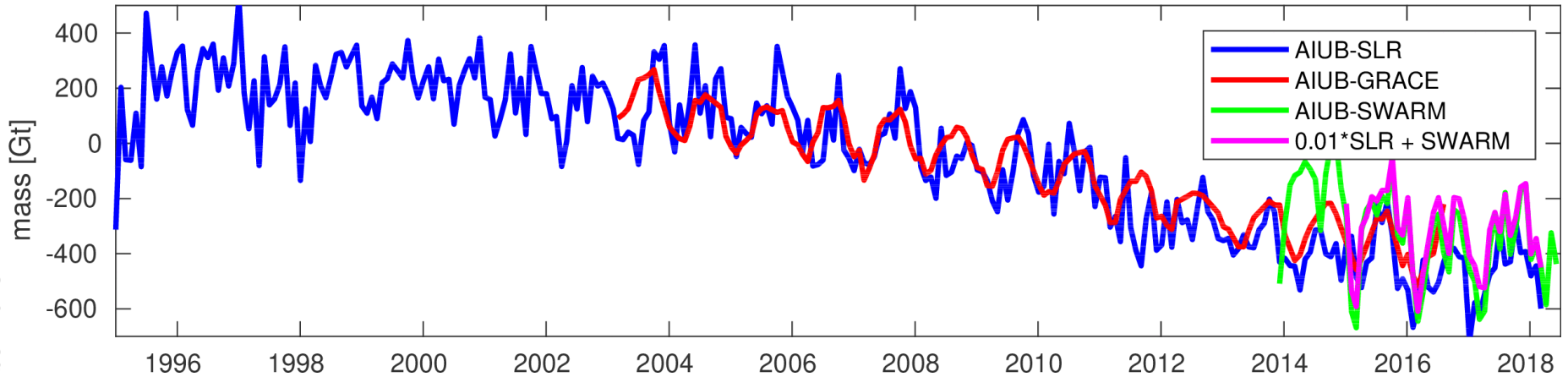
# Ice mass change: Greenland Inland



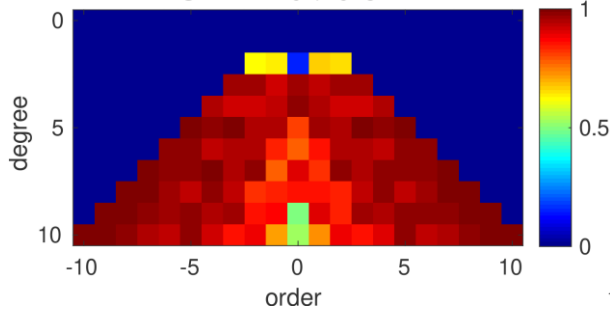
- Details at small spatial scales are lost. A separation between Greenland coast and inland is not possible with SLR.

# Combination of NEQs: SWARM + 0.01 \* SLR

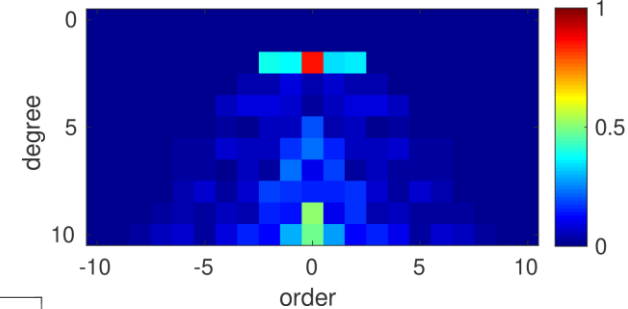
## Greenland



SWARM: 01/2018

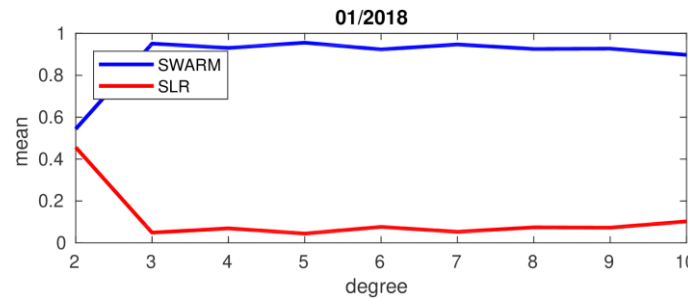


SLR: 01/2018



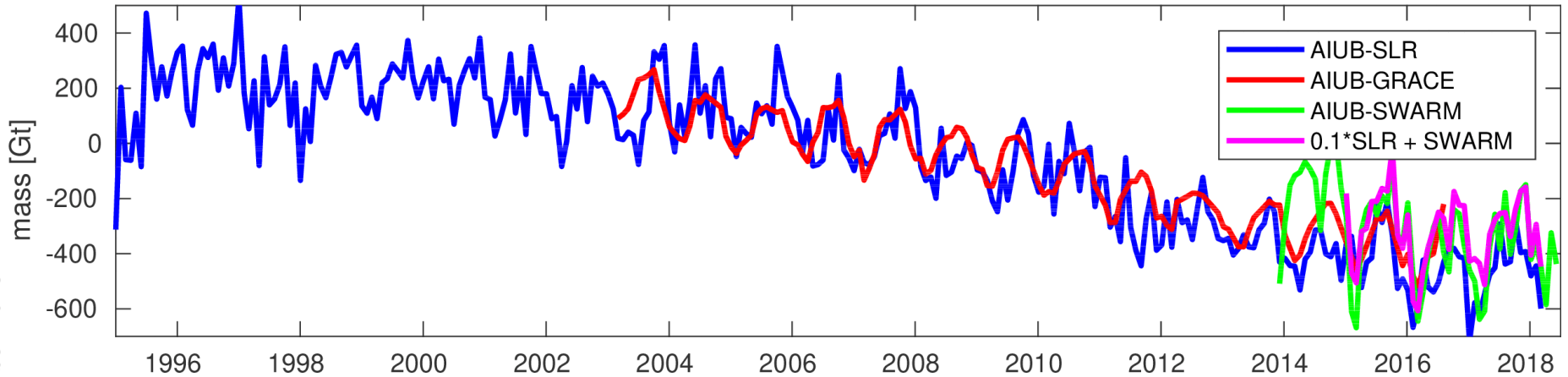
Contribution analysis per SH coefficient.

Mean contribution per degree.

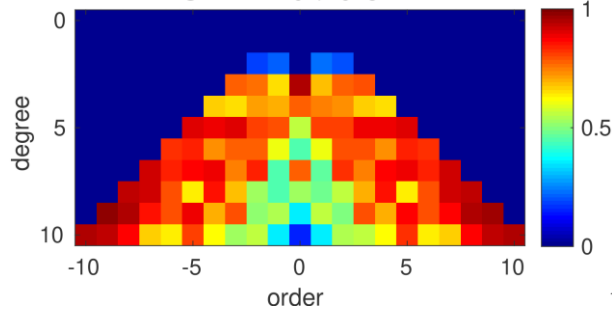


# Combination of NEQs: SWARM + 0.1 \* SLR

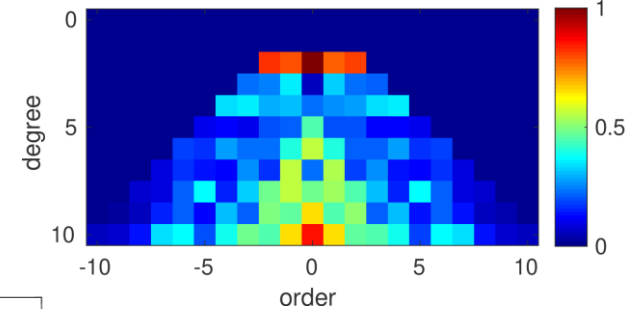
## Greenland



SWARM: 01/2018

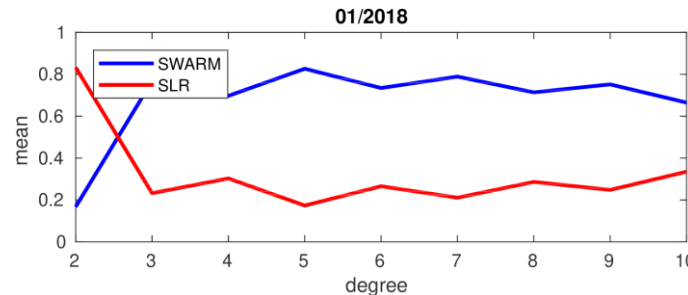


SLR: 01/2018



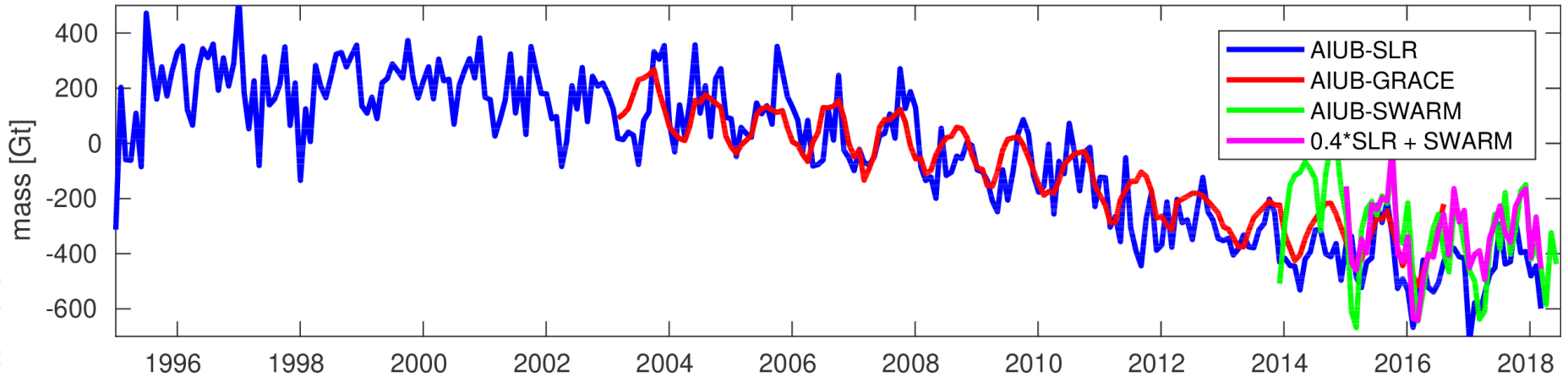
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Mean contribution per degree.

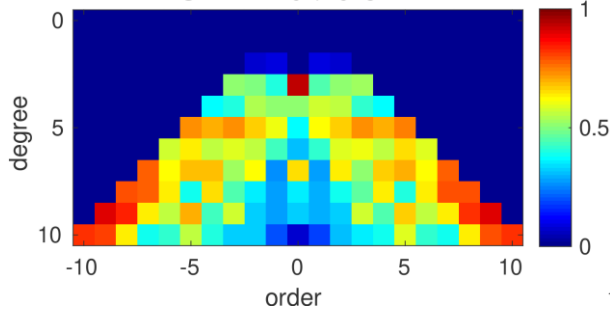


# Combination of NEQs: SWARM + 0.4 \* SLR

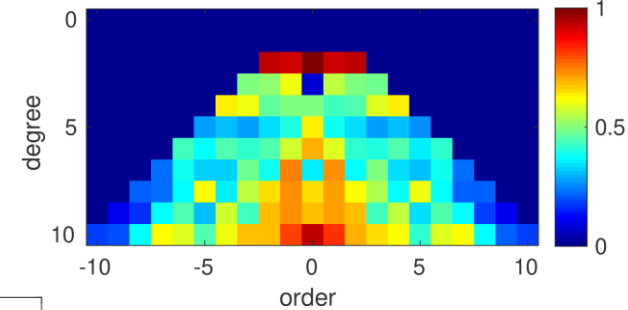
## Greenland



SWARM: 01/2018

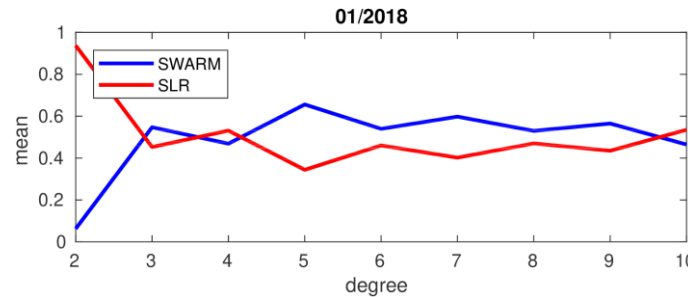


SLR: 01/2018



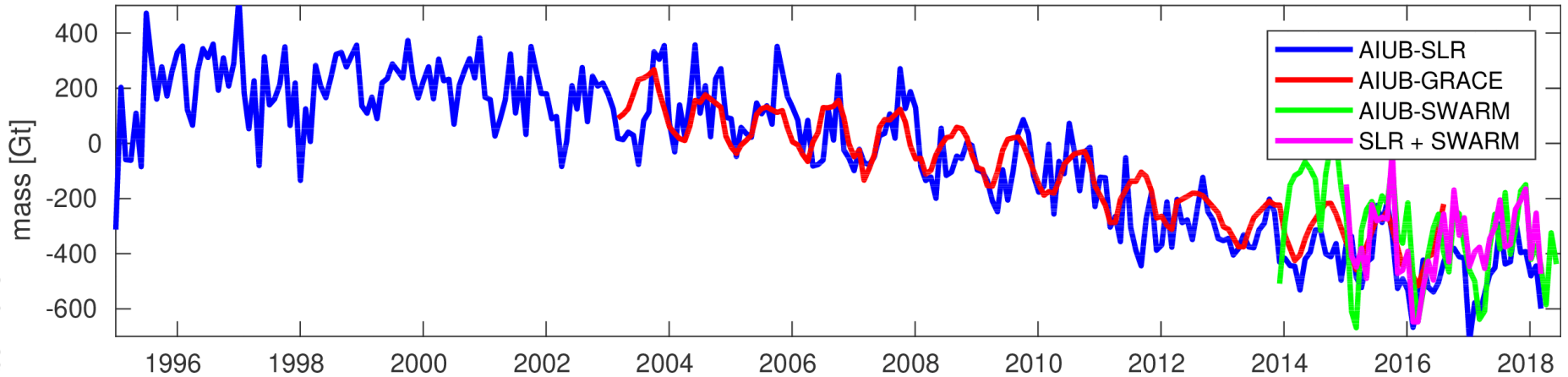
Contribution analysis per SH coefficient.

Mean contribution per degree.

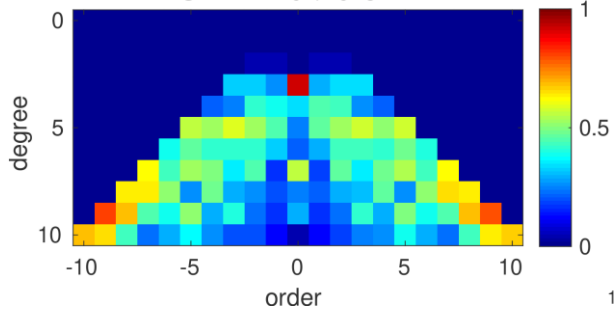


# Combination of NEQs: SWARM + SLR

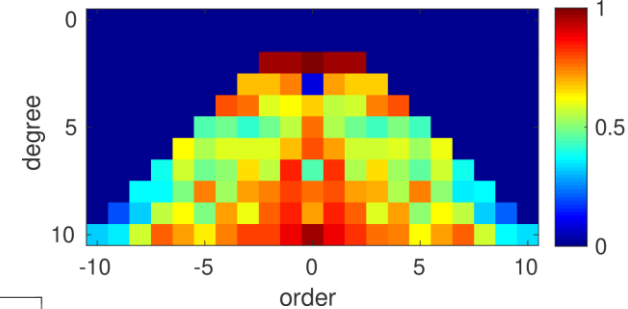
## Greenland



SWARM: 01/2018

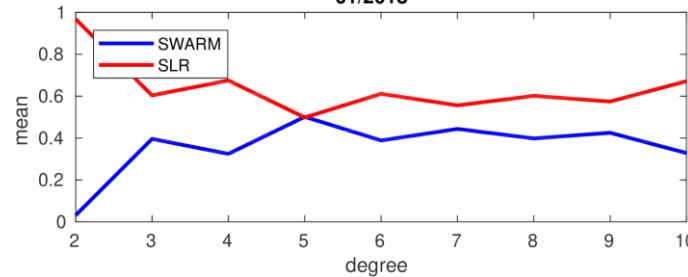


SLR: 01/2018



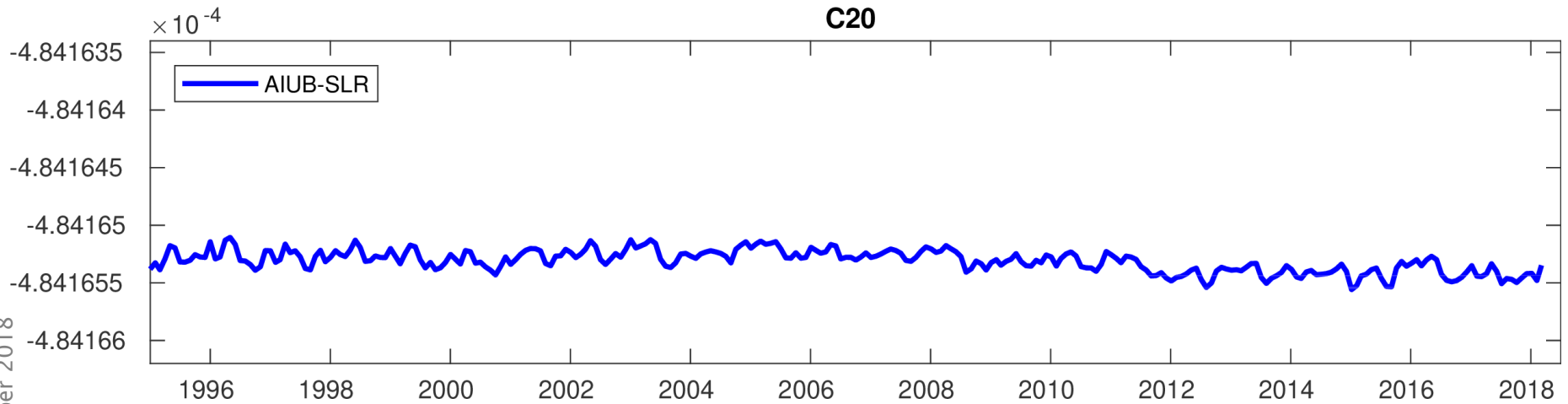
Contribution analysis per SH coefficient.

01/2018



Mean contribution per degree.

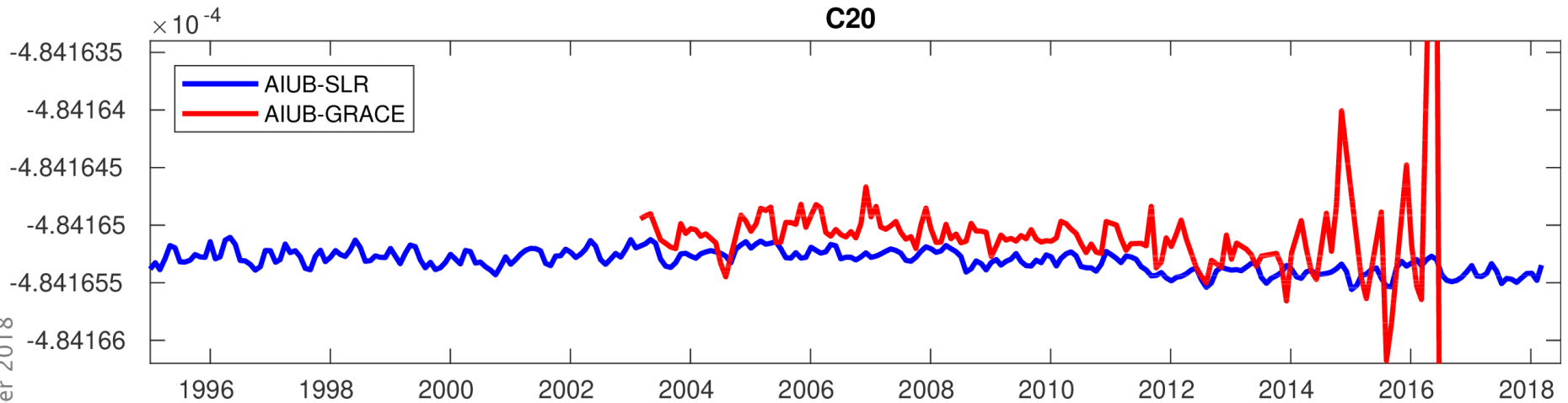
# C20



- **LAGEOS + SLR-LEOs: 30 d C<sub>20</sub> values**

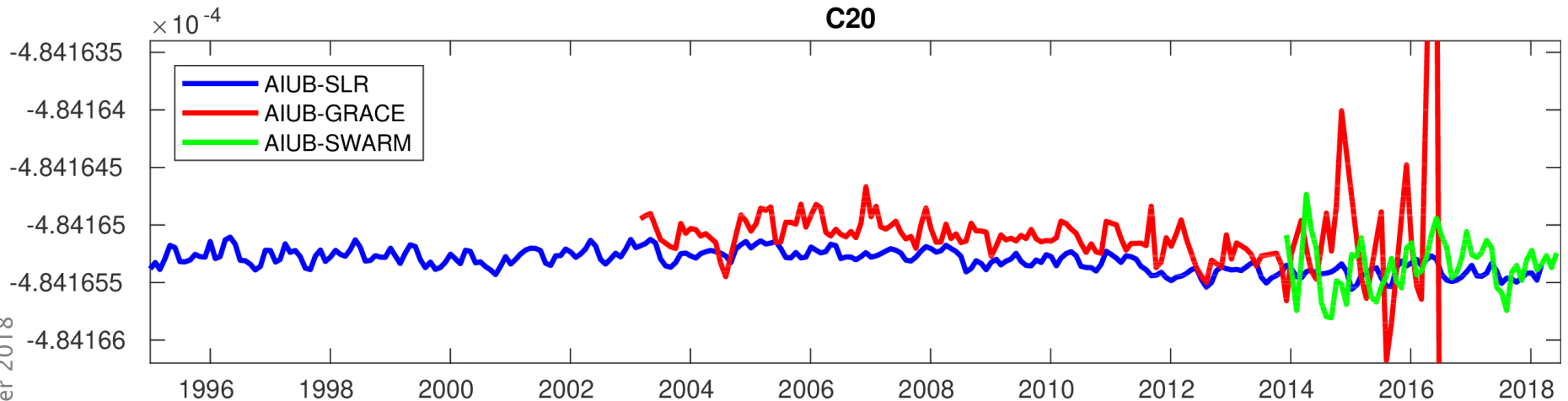


# C20



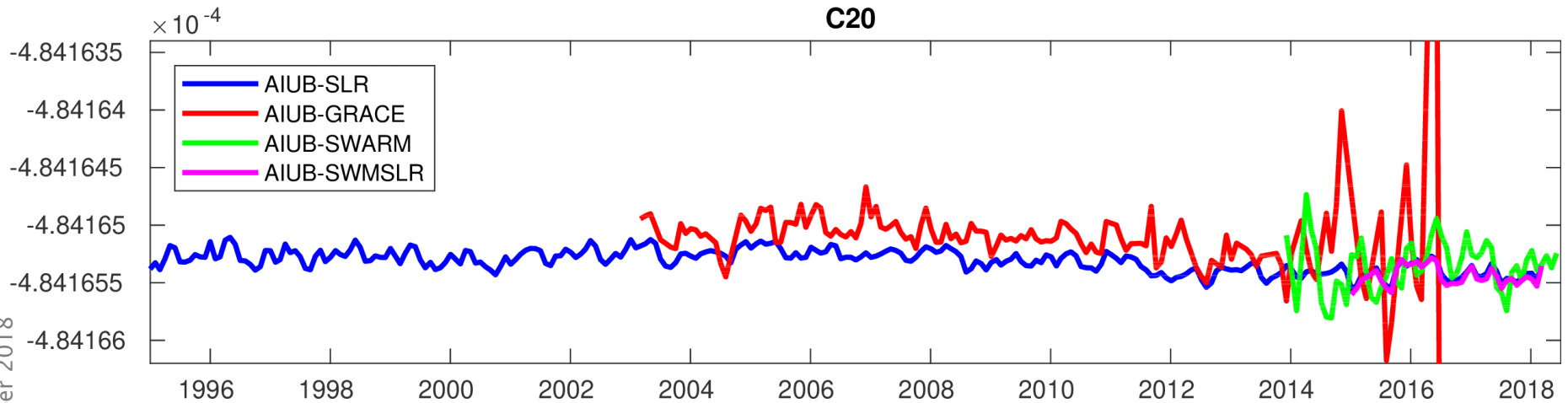
- **LAGEOS + SLR–LEOs: 30 d C<sub>20</sub> values**
- **GRACE: monthly C<sub>20</sub> values, strong correlation with accelerometer temperature**

# C20



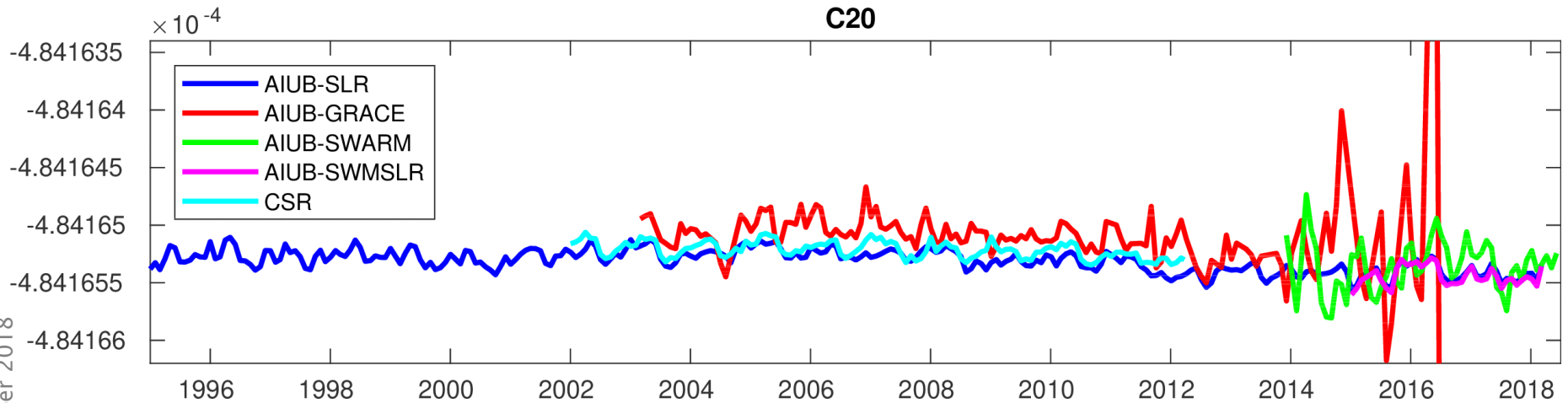
- LAGEOS + SLR–LEOs: 30 d  $C_{20}$  values.
- GRACE: monthly  $C_{20}$  values, strong correlation with accelerometer temperature.
- SWARM: monthly  $C_{20}$  values (no accelerometers used for signal separation).

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- LAGEOS + SLR–LEOs: 30 d  $C_{20}$  values.
- GRACE: monthly  $C_{20}$  values, strong correlation with accelerometer temperature.
- SWARM: monthly  $C_{20}$  values (no accelerometers used for signal separation).
- SLR + SWARM:  $C_{20}$  dominated by SLR

# C20



- **LAGEOS + SLR–LEOs: 30 d  $C_{20}$  values.**
- **GRACE: monthly  $C_{20}$  values, strong correlation with accelerometer temperature.**
- **SWARM: monthly  $C_{20}$  values (no accelerometers used for signal separation).**
- **SLR + SWARM:  $C_{20}$  dominated by SLR**
- **Reference CSR: monthly  $C_{20}$  values for GRACE**

# Summary and Outlook

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- Truncated to the same spherical harmonic resolution the three space geodetic techniques SLR, high–low–SST (GPS) and low–low–SST (K–band) provide comparable ice mass trends.
- Taking spectral leakage into account the low resolution SLR mass trends are in agreement with high resolution GRACE results.
- Best SLR + SWARM combination results are achieved with equal weighting.