Transmission dynamics of *Chlamydia trachomatis* affect the impact of screening programmes

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Abstract

1

To assess the impact of screening programmes in reducing the prevalence of 2 Chlamydia trachomatis, mathematical and computational models are used as a 3 guideline for decision support. Unfortunately, large uncertainties exist about the 4 5 parameters that determine the transmission dynamics of C. trachomatis. Here, we 6 use a SEIRS (susceptible-exposed-infected-recovered-susceptible) model to critically analyze the turnover of C. trachomatis in a population and the impact of a 7 screening programme. We perform a sensitivity analysis on the most important 8 steps during an infection with C. trachomatis. Varying the fraction of the infections 9 becoming symptomatic as well as the duration of the symptomatic period within 10 the range of previously used parameter estimates has little effect on the transmis-11 sion dynamics. However, uncertainties in the duration of temporary immunity and 12 the asymptomatic period can result in large differences in the predicted impact of 13 a screening programme. We therefore analyze previously published data on the 14 persistence of asymptomatic C. trachomatis infection in women and estimate the 15 mean duration of the asymptomatic period to be longer than anticipated so far, 16 namely 433 days (95% CI: 420–447 days). Our study shows that a longer duration 17 of the asymptomatic period results in a more pronounced impact of a screening 18 programme. However, due to the slower turnover of the infection, a substantial 19 reduction in prevalence can only be achieved after screening for several years or 20 decades. 21

²² Introduction

Infection with *Chlamydia trachomatis* is the most common bacterial sexually transmit-23 ted disease in many developed countries (World Health Organization, 2001). In women, 24 infection can lead to pelvic inflammatory disease (PID) which can result in chronic 25 pelvic pain, ectopic pregnancy or infertility (Cates and Wasserheit, 1991). Whilst acute 26 infection can cause urethral discharge and pain on urination in men and symptoms such 27 as vaginal discharge in women, most infections are asymptomatic and therefore remain 28 undiagnosed. Screening and treatment of young adult women (Centers for Disease Con-29 trol and Prevention, 2006) or women and men (Department of Health, 2004) is widely 30 promoted as an intervention to reduce the duration of infection and thus lower the 31 prevalence of *C. trachomatis* and reduce the incidence of possible sequelae. 32

Mathematical and computational models that describe the transmission of C. tra-33 chomatis have been applied to inform and guide public health decisions about screening 34 programmes (Kretzschmar et al., 1996, 2001; Turner et al., 2006a; Low et al., 2007; 35 Regan et al., 2008). Other models have been used to investigate aspects of immunity 36 (Brunham et al., 2005), to assess the potential impact of vaccines (Gray et al., 2009) or 37 to gain general insights into the transmission dynamics of C. trachomatis (Sharomi and 38 Gumel, 2009). Since transmission occurs through sexual contact and screening strategies 39 can be targeted to women only, women and men or specific core groups, many models 40 incorporate detailed descriptions of contact patterns between people. However, there 41 are great uncertainties about the parameters that describe sexual behavior and the val-42 ues used for disease-specific parameters. These have led to conflicting results about the 43 potential impact of screening programmes (Kretzschmar et al., 2009). It is therefore 44 essential to critically investigate the impact of different parameter assumptions in order 45 to quantify the transmission dynamics of C. trachomatis and the potential impact of 46 public health interventions. 47

In a simple epidemiological model, the basic reproductive number, R_0 , determines the endemic prevalence of an infection. R_0 can be defined as the product of the duration of an infection and the rate at which an infected individual transmits the disease to a sus-

ceptible. Whereas the first is a disease-specific parameter, the latter is also influenced 51 by behavioral parameters that describe contacts between people. Hence, for a given 52 prevalence of C. trachomatis within the population, the overall turnover of the infection 53 is simply determined by the duration of the infection, i.e., is given by disease-specific 54 parameters only. By treating the rate at which individuals engage in sexual contacts 55 as a function of the endemic prevalence, we can analyze carefully the parameters that 56 characterize the transitions through an infection and their influence on the predicted 57 impact of a screening programme. Generally, the longer a person is infected, the more 58 likely it is that they will be reached by a screening programme and will receive treat-59 ment. C. trachomatis infection is indeed characterized by a long asymptomatic period 60 (Molano et al., 2005), but the duration of this period is not known. In addition, it is 61 unclear what fraction of infections will cause symptoms that prompt treatment seeking 62 behavior (Korenromp et al., 2002), or whether natural clearance is followed by a period 63 of temporary immunity (Brunham and Rey-Ladino, 2005). Previous studies have inves-64 tigated the impact of disease-specific parameters on the impact of different screening 65 strategies (Hu et al., 2006; Regan et al., 2008). Unfortunately, due to the complexity of 66 these models, it is difficult to perform sensitivity analysis over a wide range of parameter 67 values. 68

The objective of this paper is to perform a sensitivity analysis of disease-specific 69 parameters on the predicted impact of a screening programme. To this end, we devise a 70 basic epidemiological model of C. trachomatis transmission dynamics that describes the 71 overall turnover of the infection within a general population. In addition, we also derive 72 a new estimate of the duration of the asymptomatic period by reanalyzing previously 73 published data on the persistence of C. trachomatis in asymptomatically infected women. 74 We discuss the implications of our results, which highlight the importance of continued 75 evaluation of parameter estimates for mathematical and computational models that aim 76 to assess the impact of screening programmes. 77

78 Methods

79 SEIRS model

We used a SEIRS (susceptible-exposed-infected-recovered-susceptible) model, which is widely used in the infectious disease modeling literature (Anderson and May, 1991; Diekmann and Heesterbeek, 2000; Keeling and Rohani, 2008), to devise a simple mathematical model of *C. trachomatis* transmission that takes into account the major transitions of infected people during an infection.

We assume a closed population where susceptibles, S, may become infected with 85 C. trachomatis. They move through an incubation time, E, of the pathogen to become 86 either asymptomatically, I_a , or symptomatically infected, I_s . Asymptomatic people that 87 recover naturally, R, may develop temporary immunity against re-infection. Symptomat-88 ically infected people have a shorter period of infection that can be ascribed to treatment 89 seeking due to symptoms. Both asymptomatically and symptomatically infected people 90 can get screened and directly treated (Fig. 1). Although most infections with C. tra-91 chomatis happen through sexual contacts between women and men, we strictly assume 92 a homogeneous population where both genders become infected and pass through the 93 infected stages at equal rates. This is a valid assumption because, even though differ-94 ences in gender-specific parameters of C. trachomatis infection have been observed, the 95 purpose of our study is a sensitivity analysis over a broad range of parameter estimates 96 which is wider than the gender-specific differences. We also do not assume separate risk 97 groups that exhibit different sexual behavior but we illustrate in the Appendix that a 98 stochastic implementation of our model exhibits a realistic amount of heterogeneity (see 99 also *Discussion*). The model can be described by the following set of ordinary differential 100

101 equations:

$$\frac{dS}{dt} = -\beta (I_a + I_s)S + cI_a + (r_s + c)I_s + \mu R, \qquad (1)$$

$$\frac{dE}{dt} = \beta (I_a + I_s)S - \gamma E, \qquad (2)$$

$$\frac{dI_a}{dt} = f\gamma E - (r_a + c)I_a,\tag{3}$$

$$\frac{dI_s}{dt} = (1-f)\gamma E - (r_s + c)I_s,\tag{4}$$

$$\frac{dR}{dt} = r_a I_a - \mu R. \tag{5}$$

There is a wide range of published estimates for the duration of the incubation 102 time, $1/\gamma$, the fraction of infections becoming asymptomatic, f, and the duration of the 103 asymptomatic and symptomatic period, $1/r_a$ and $1/r_s$, respectively (Table 1). Based 104 on observations from studies in mice, it has been suggested that natural clearance may 105 be followed by temporary immunity of length $1/\mu$ (Brunham and Rey-Ladino, 2005). 106 The parameter c denotes the effect of screening the population where asymptomatically 107 or symptomatically infected people are diagnosed and treated so that they immediately 108 become susceptible again. The rate at which susceptible people have contact with in-109 fected people and in which such contact results in transmission of C. trachomatis is not 110 known. In our model, this rate is given by the parameter β , where $\lambda = \beta (I_a + I_s)$ can 111 be described as the 'force of infection'. Since it is exceedingly difficult to get a direct 112 estimate of β or λ , we adjust the rate at which people make a potentially infectious 113 contact, β , to obtain a given prevalence of the infection in the total population. 114

Assuming the prevalence of *C. trachomatis* to be in a steady-state, the derivatives of Eq. (1) – (5) can be set to zero. Since we assume a closed population, we can set the total population size to $S + E + I_a + I_s + R = 1$, which allows us to express all compartments as fractions of the total population. By solving the system of equations for the prevalence $p = I_a + I_s$, we obtain

$$p = \frac{\gamma \mu (\beta - a - b)}{\beta (\gamma \mu + a\gamma + a\mu + b\mu)},\tag{6}$$

120 where

$$a = \frac{fr_a(r_s + c)}{fr_s + (1 - f)r_a + c} \quad \text{and} \quad b = \frac{(r_a + c)(1 - f)r_s}{fr_s + (1 - f)r_a + c} + c.$$
(7)

The expression for the prevalence p as a function of a and b can be explained by a simpler SEIRS model that does not distinguish between symptomatic and asymptomatic states. In such a model, a denotes the rate at which infected people recover and develop temporary immunity and b the rate at which infected people become directly susceptible again. The steady-state prevalence, p, of this simpler model is directly given by Eq. (6). The necessary 'infection rate' β to obtain a given prevalence p is:

$$\beta = \frac{\gamma\mu(a+b)}{(1-p)\gamma\mu - p(a\gamma + a\mu + b\mu)}.$$
(8)

By choosing a and b as in Eq. (7), we can distinguish between symptomatically and 127 asymptomatically infected individuals as described in the full model from Eq. (1) - (5). 128 For any given combination of disease-specific parameters, we wish to calculate the 129 expected prevalence of C. trachomatis in a population that receives screening at a rate 130 c. To this end, we first assume a prevalence p_0 in absence of screening and denote the 131 corresponding 'infection rate' β_0 which is given by Eq. (8) for c = 0. We then calculate 132 the new steady-state prevalence in the presence of screening (c > 0) by Eq. (6) with 133 β_0 as the 'infection rate'. This scenario is considered to reflect the long-term impact 134 of opportunistic screening, where a relatively small proportion of the total population 135 is tested in health care settings. In contrast to opportunistic screening, an organized 136 screening programme aims to reduce the prevalence of the infection by targeting a larger 137 proportion of the population at regular intervals. Further, the reduction in prevalence 138 will now depend on the time that has passed since the organized screening programme 139 was introduced. To contrast this with the first scenario, we also perform numerical 140 simulations starting at the pre-screening steady-state, p_0 , to calculate the reduction in 141 prevalence after an organized screening programme (c > 0) has been active for a certain 142 number of years. 143

Since we can express β_0 as a function of the disease-specific parameters and the pre-screening prevalence, we can analyze the impact of screening over a wide range of

parameters. To express the uncertainties of previously used estimates, we use the upper 146 and lower bounds of disease-specific parameters that have been used in various models of 147 C. trachomatis transmission dynamics (Kretzschmar et al., 1996; Brunham et al., 2005; 148 Turner et al., 2006a; Low et al., 2007; Regan et al., 2008; Gray et al., 2009; Sharomi 149 and Gumel, 2009). As baseline parameters, we use the mean value of the respective 150 ranges (Table 1). Since the upper bound for the duration of temporary immunity $(1/\mu)$ 151 is life long, we cannot provide the mean value of the range and therefore set the baseline 152 duration of immunity arbitrarily to 90 days. 153

Analytical results were derived in Mathematica (Wolfram Research, Inc., 2008) and numerical integrations were performed in C using the routine odeint (Runge-Kutta with adaptive stepsize control) from Numerical Recipes (Press et al., 1992). Code files can be obtained freely on request from the authors.

¹⁵⁸ Parameter estimation

To estimate the natural clearance rate of C. trachomatis, we used data from a previously 159 published study. Molano et al. (2005) analyzed data from women who had endocervical 160 specimens taken every 6–9 months for up to 5 years during a follow-up study about 161 human papillomavirus infection. After the end of the study, stored specimens were 162 also tested for C. trachomatis from which a survival function of the persistence of C. 163 trachomatis infection could be derived. The date of chlamydia clearance was defined as 164 the midpoint between the last positive test and a negative test. Data about antibiotic 165 treatment for chlamydia and sexual partner change that might have resulted in a new 166 infection were not collected but both were thought to be rare. We devise a mathematical 167 model that describes the persistence of C. trachomatis in asymptomatically infected 168 women: 169

$$\frac{dI_a}{dt} = -r_a I_a + \alpha S,\tag{9}$$

$$\frac{dS}{dt} = r_a I_a - \alpha S. \tag{10}$$

Here, asymptomatically infected women, I_a , can clear the infection at a rate r_a . Being susceptible again, they are at risk of re-infection at a rate α . Molano et al. (2005) provide data on 82 women, all of whom are infected with *C. trachomatis* at the beginning, so we can set $I_a(0) = 1$ and S(0) = 0 and solve for $I_a(t)$:

$$I_a(t) = \frac{\alpha + r_a e^{-(r_a + \alpha)t}}{\alpha + r_a}.$$
(11)

The natural clearance rate and the re-infection rate can now be estimated by fitting Eq. (11) to the data from figure 1 in Molano et al. (2005). The data were digitized using Plot Digitizer (http://plotdigitizer.sourceforge.net) and we excluded time points within the first 4.5 months to ensure that all women have been tested at least once during the follow-up period. The model was fitted using the FindFit routine that minimizes the sum of squared residuals (SSR) from the software package Mathematica (Wolfram Research, Inc., 2008).

181 Results

¹⁸² Impact of an organized screening programme

To investigate the impact of organized screening in the general population, we first 183 assume the pre-screening prevalence of C. trachomatis in the population to be 5%. This 184 roughly corresponds to the prevalence observed in sexually active young adults (Fenton 185 et al., 2001). Now, we can follow the decrease in prevalence after the introduction 186 of three different organized screening programmes (Fig. 2). Screening the population 187 randomly at a rate of 0.05 per year (i.e., every individual is screened once every 20 year 188 on average) reduces the prevalence of infection only slightly (solid line). Increasing the 189 screening rate to 0.25 per year (individuals are screened once every 4 years on average, 190 dashed line) or even 0.5 per year (individuals are screened once every 2 years on average, 191 dotted line) results in a pronounced impact within 5 to 10 years of screening. Clearly, 192 the longer a screening programme is in place, the more pronounced is the reduction in 193 prevalence. The new steady-state prevalence that will be approached in the presence of 194

a screening programme will therefore be further reduced. In this model, screening the 195 population at a rate higher than 0.1 per year would eventually be sufficient to eradicate 196 the infection from the population (Fig. 3, dashed line). However, the slow decline in 197 prevalence after introducing a screening programme (Fig. 2) illustrates that such a state 198 can only be achieved after screening for several decades. The impact of a screening 199 programme implemented for 5 years (Fig. 3, dotted line) or 10 years (Fig. 3, solid line) 200 is less pronounced, highlighting the difficulties in reducing the prevalence of an infection 201 that exhibits a slow turnover within a reasonable time span. 202

²⁰³ Parameter sensitivity on the impact of screening

Due to the large uncertainties of disease-specific parameters that determine the trans-204 mission dynamics of C. trachomatis (Table 1), it is essential to perform a sensitivity 205 analysis if one wants to assess the impact of screening the general population. We have 206 shown above that it is important to distinguish between the effects of a screening pro-207 gramme over different time spans. Both, the temporal impact of screening during a given 208 time period and the expected long-term prevalence if screening is prolonged give impor-209 tant insights into screening strategies. For our sensitivity analysis, we thus consider two 210 different screening scenarios; an organized screening programme with a screening rate of 211 0.25 per year implemented for 10 years, and opportunistic screening at a rate of 0.05 per 212 year, in which the new steady-state prevalence is shown after long-term implementation. 213 Arguably the most critical steps during an infection with C. trachomatis are the 214 fraction of infections that become asymptomatic (f) and the durations of the asymp-215 tomatic and symptomatic period, $1/r_a$ and $1/r_s$, respectively. During these stages C. 216 trachomatis is assumed to be infectious so changes in these values should determine the 217 overall transmission within a population. Varying the fraction of infections becoming 218 asymptomatic at levels greater than 20%, however, has little effect on the predicted 219 outcome of a screening programme (Fig. 4A, grav area). As long as the asymptomatic 220 period is substantially longer than the symptomatic period, the screening intervention 221 detects mostly asymptomatically infected people and only a small proportion of trans-222 mission events is caused by symptomatic individuals. Similarly, changing the duration 223

of the symptomatic period hardly affects the impact of screening (Fig. 4B). If the du-224 ration is short, little transmission is caused by symptomatics. As the duration of the 225 symptomatic period increases, it becomes more likely that symptomatically infected in-226 dividuals are also detected by the screening programme. A different picture arises when 227 we vary the duration of the asymptomatic period (Fig. 4C). Here, the predicted long-228 term impact of screening is much more pronounced if the asymptomatic period is at the 229 upper bound of the previously used parameter range (gray area). This property also 230 holds if, for example, the fraction of infections that becomes asymptomatic is varied 231 at the same time (see two-way sensitivity analysis in the Appendix). Interestingly, the 232 impact of screening for 10 years is much less affected. This is because increasing the du-233 ration of the asymptomatic period results in a slower turnover of C. trachomatis within 234 the population, which will decelerate the effect of screening. We performed the same 235 analysis for different pre-screening prevalences of C. trachomatis which can be found in 236 different risk groups (1% - 15%), results not shown). Higher pre-screening prevalences of 237 C. trachomatis imply an elevated turnover of the infection. While this does not affect 238 the qualitative results of the sensitivity analysis for a long-term screening intervention, 239 the effect of screening for 10 years changes. Due to the elevated turnover, the impact of 240 screening for 10 years becomes effective earlier and more closely resembles the effect of a 241 long-term screening programme. Thus, different durations of the asymptomatic period 242 can result in a substantially different impact of screening during an intervention period 243 of a few years. 244

In addition, we perform a sensitivity analysis on the parameters that describe the 245 stages of an infection which are not infectious, i.e., the period of temporary immunity 246 after natural clearance of an asymptomatic infection $(1/\mu)$ and the incubation time 247 $(1/\gamma)$. Although the incubation time is generally assumed to be short (gray area), 248 the sensitivity analysis illustrates that changing this parameter over a wider range of 249 values can affect the predicted impact of a screening programme (Fig. 5A). For a longer 250 duration of the incubation time, more infected people will be screened during the time 251 when the infection is assumed not to be detectable or infectious yet. Hence, the impact 252 of screening the general population at a certain rate diminishes slightly. Assuming 253

temporary immunity also results in a less pronounced impact of screening. Increasing the duration of temporary immunity decreases the impact of screening even more (Fig. 5B). Regarding the wide range of immunity that has been used in different models so far (gray area), this effect becomes especially strong in the long-term. Here, screening and treating asymptomatically infected people prevents the development of temporary immunity and renders them susceptible immediately. This somewhat counterbalances the otherwise strong impact of screening.

²⁶¹ Estimating the duration of the asymptomatic period

We have shown that the long-term outcome of a screening programme is most sensi-262 tive to the duration of the asymptomatic period. In the modeling literature of C. tra-263 chomatis transmission dynamics, values for this parameter range from 180 to 420 days, 264 emphasizing the uncertainty. A recent study that followed a large number of asymp-265 tomatic chlamydia-infected women indicated that the infection can persist for several 266 years (Molano et al., 2005). However, it was mentioned that repeated infections from an 267 untreated male sex partner might have biased the data in such a way that the estimated 268 duration of the asymptomatic period only serves as an upper limit. In order to test the 269 assumption of re-infection and to provide a robust estimate of the natural clearance rate 270 in asymptomatically infected women, we fit a mathematical model to the data (Fig. 6). 271 The estimated re-infection rate is low (0.01 per year; 95% CI: -0.01–0.03 per year) which 272 indicates that the data are mainly described by natural clearance. With an estimated 273 clearance rate of 0.84 per year (95% CI: 0.82–0.87 per year), we obtain a mean duration 274 of the asymptomatic period of 433 days (95% CI: 420–447 days). 275

276 Discussion

We developed a basic epidemiological model that captures the most essential transitions through an infection with *C. trachomatis* to assess the importance of disease-specific parameters on the impact of chlamydia screening programmes. Sensitivity analyses show that the duration of temporary immunity and the duration of the asymptomatic period

strongly affect the long-term impact of screening. Longer periods of temporary immunity 281 diminish the effect of screening. A longer duration of the asymptomatic period, however, 282 results in a more pronounced impact of such a programme. Using previously published 283 data, we estimated the average duration of the asymptomatic period at 433 days, which 284 is substantially higher than most estimates used in mathematical and computational 285 models. Interestingly, previous studies have indicated an even longer duration of the 286 asymptomatic period than we estimate here (McCormack et al., 1979; Morré et al., 287 2002). As those studies followed a much smaller number of women than Molano et al. 288 (2005) and did not explicitly take the effect of re-infection into account, our new estimate 289 is likely to be more robust. 290

The simplicity of our model facilitates the understanding of basic properties of the 291 transmission dynamics of C. trachomatis. Previous attempts to investigate C. trachoma-292 tis transmission and the potential impact of public health interventions have often been 293 performed with more detailed models (Kretzschmar et al., 1996; Brunham et al., 2005; 294 Turner et al., 2006a; Low et al., 2007; Regan et al., 2008; Gray et al., 2009; Sharomi 295 and Gumel, 2009). However, as more complicated models can be difficult to analyze and 296 interpret, it is sometimes reasonable 'to keep it simple' in order to address some gen-297 eral principles of the transmission dynamics of an infectious disease (May, 2004; Regan 298 and Wilson, 2008). In this study, we have shown the utility of a simple epidemiological 299 model, especially for performing a sensitivity analysis over a wide range of parameters. 300

In contrast to our assumption of homogeneous mixing, transmission of sexually trans-301 mitted infections (STIs) has been found to be driven by 'core groups'. This concept is 302 especially important to describe the transmission of bacterial STIs with short infec-303 tious periods, such as gonorrhea (Hethcote and Yorke, 1984). However, C. trachomatis 304 appears to be more evenly spread across subpopulations due to its longer duration of 305 infection (Chen et al., 2009). Since we assume a homogenous population, it is worth-306 while analyzing the values of the 'infection rate' β that we obtained by adjusting the 307 pre-screening prevalence to 5%. Changing disease-specific parameters within the range 308 that has been previously used results in values of β that are between 1.3 and 3.9 per 309 person per year (Fig. 9). The infection rate can be expressed as the product of the 310

sexual partner change rate and the transmission probability per partnership. Given a transmission probability of around 0.7 (Quinn et al., 1996), the sexual partner change rates are in the range of 0.9 and 2.7 per year which is in agreement with reported data from young adults in Britain (Johnson et al., 2001). Thus, it appears that our model captures the overall transmission dynamics of *C. trachomatis* reasonably well.

Based on our results, we can test whether differences in the duration of the infection 316 are able to explain the conflicting results that have been found in Kretzschmar et al. 317 (2009). Looking at the mean duration of C. trachomatis infection in men, the model 318 with the longest duration indeed predicts the largest impact of a screening programme 319 (Turner et al., 2006a). In contrast, the model with the shortest duration of infection in 320 men results in the smallest impact of screening (Low et al., 2007). The same pattern does 321 not hold for the average duration of infection in women, however. Thus, it is likely that 322 different assumptions of the underlying sexual partnership dynamics further contribute 323 to the observed differences in the predicted impact of a screening programme. 324

Besides the qualitative insights of this study, we can also provide some quantita-325 tive predictions. For example, the results of our study, showing that screening the 326 population at a rate of 0.25 - 0.5 per year over a period of 5 - 10 years can result 327 in a pronounced decrease in the prevalence of C. trachomatis, are similar to those of 328 more complicated compartmental or individual-based models (Kretzschmar et al., 2001; 329 Turner et al., 2006b; Regan et al., 2008). Nevertheless, quantitative conclusions from 330 our model should be interpreted cautiously. Our simplifying assumptions neglect poten-331 tial effects that will counter against the effect of an organized screening programme. As 332 mentioned above, we do not assume a core group with a higher sexual activity than the 333 general population. High prevalences of C. trachomatis could persist in such core groups 334 if they are not targeted directly. If there is ongoing transmission between the core group 335 and the general population, this could diminish the effect of population-wide screening 336 programmes. Further, we assume perfect screening uptake and do not explicitly consider 337 sexual partnerships between people. Re-infection of treated cases within steady part-338 nerships is expected to counter the desired effect of screening (Lamontagne et al., 2007; 339 Low et al., 2009). These processes and the impact of partner notification have to be 340

taken into account to fully evaluate the potential of different screening programmes. To
investigate those questions, more sophisticated mathematical and computational models
that treat people as individuals with current and previous partners are necessary.

Interestingly, our analysis contrasts somewhat with the sensitivity analysis of the 344 study by Regan et al. (2008). There, the duration of the asymptomatic period had less 345 influence on the impact of screening than what we found here. Also, they found that 346 the duration of temporary immunity only affects the reduction in prevalence through 347 screening moderately. Differences between these results can be explained, at least partly, 348 by the narrow ranges of parameter values investigated in the sensitivity analysis of Regan 349 et al. (2008). For example, the average time to recover from an asymptomatic infection 350 was assumed to be between 44 to 52 weeks, i.e., 310 to 360 days. The sensitivity analyses 351 presented here covered a much wider range of parameters and our new estimate for the 352 average duration of the asymptomatic period in women, 433 days, exceeds their upper 353 limit. We are also able to show the effects of a wider range of assumptions about the 354 duration of temporary immunity and find that it can drastically diminish the effect of 355 screening. Whether natural clearance of asymptomatic infection is followed by a period 356 of temporary (or partial) immunity is still a matter of debate (Brunham and Rey-Ladino, 357 2005). In our model, we made the assumption that temporary immunity can only 358 develop in asymptomatic individuals who clear the infection naturally. Thus, screening 359 and treatment directly interfere with establishing immunity, causing a diminished effect 360 of screening in our model (Brunham and Rekart, 2008). In order to fully evaluate the 361 role of immunity on the impact of screening programmes, we need further insights about 362 the possibility of temporary immunity to C. trachomatis infection in humans and the 363 timing of its development. 364

To summarize, we have shown how simple epidemiological models can give important insights into the transmission dynamics of *C. trachomatis*. Our sensitivity analysis illustrates that disease-specific parameters can critically influence the impact of a screening programme. This emphasizes the importance of continued evaluation of parameter estimates for mathematical and computational models that are used to inform and guide public health decisions about chlamydia screening. Based on a new estimate for the average duration of the asymptomatic period in women, we conclude that *C. trachomatis* exhibits a slow turnover within the sexually active population and interventions that aim to reduce the prevalence will only become apparent after screening for several years or decades.

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383 Appendix

³⁸⁴ Heterogeneity in risk behavior

Deterministic models of infectious diseases that assume a homogenous population imply 385 that all people are, on average, subject to the same behavior. In the case of the SEIRS 386 model presented in *Methods*, it can be seen that everyone obeys the same 'infection 387 rate' β . However, the time interval at which a susceptible makes potentially infectious 388 contacts to other persons is exponentially distributed. Stochastic models can make use 389 of this implicit variation if each process is drawn separately from such a distribution. 390 With time, this will inevitably cause variation in peoples behavior if we could look at 391 them on an individual level. 392

To illustrate this effect, we implemented a stochastic version of the SEIRS model in an individual-based population. This method allows us to store all previous contacts of an individual in the memory. To keep track of all contacts of an individual (including the non-infectious ones), it is necessary that susceptibles not only make contacts to

infected people but also to other susceptibles or recovered people. For simplicity, we 397 assume that all contacts happen at the same rate β and that transmission occurs in any 398 case if a susceptible makes a contact to an infectious individual. The individuals can 399 now be grouped according to their past history of contacts at any given time. Further, 400 we can calculate the prevalence of C. trachomatis for each specific group. We use the 401 baseline parameters from Table 1 and run the simulation for 100 years to approach 402 the steady-state in absence of any screening intervention. The simulations were run in 403 the R software environment for statistical computing (R Development Core Team, 2009) 404 using the package *Rstisim* (Althaus et al., manuscript in preparation). For the graphical 405 representation of the contact network, we use the network package (Butts et al., 2008). 406 The simulation shows that people can have widely different numbers of contacts, 407 exemplifying the intrinsic property of variation in the individuals behavior (Fig. 7A). 408 People with no or few contacts within the last year have a lower prevalence of C. tra-409 chomatis than the average population (Fig. 7B). By chance, a small fraction of people 410 will have a high number of contacts and the prevalence in those groups can be much 411 higher than the average. Therefore, a stochastic implementation of our SEIRS model 412 in an individual-based population illustrates that, although we assume a 'homogenous' 413 population, such models do account for a certain variation in people's behavior. 414

415 Two-way sensitivity analysis

For reasons of clarity, we restricted our sensitivity analysis in the *Results* section to 416 be univariate. However, it is important to analyze the combined effect of changing 417 critical parameters. Since we found the duration of the asymptomatic period to be im-418 portant, it is natural to investigate its impact together with changing the fraction of 419 infections that become asymptomatic (Fig. 8A). It can be seen that the duration of 420 the asymptomatic period remains a critical parameter whereas the fraction of infections 421 that become asymptomatic has little impact within the range of parameters that has 422 been previously used (white dashed rectangle). We also investigated the combined ef-423 fect of varying the duration of the asymptomatic period together with the duration of 424 temporary immunity (Fig. 8B). Here, both parameters strongly affect the impact of a 425

screening programme and we observe that the predicted outcome can vary from only little reduction in prevalence (top left corner) to close to extinction of the infection (lower
right corner).

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Table 1: Parameters for *C. trachomatis* transmission dynamics. The baseline values of diseasespecific parameters for the SEIRS model are given as the mean values from the range of parameters that have been used in several mathematical and computational models so far (Kretzschmar et al., 1996; Brunham et al., 2005; Turner et al., 2006a; Low et al., 2007; Regan et al., 2008; Gray et al., 2009; Sharomi and Gumel, 2009). As an exception, we assume 90 days for the baseline duration of temporary immunity $(1/\mu)$. Given the baseline parameter values, we obtain $\beta = 1.95$ per person per year for the infection rate and $R_0 = 1.07$ for the basic reproductive number.

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Figure 1: SEIRS model illustrating infection with *C. trachomatis* and subsequent transitions through the different stages of infection. Susceptibles, *S*, get infected by infected people, $I_a + I_s$, at a rate β . They then move through an incubation period (*E*) at a rate γ to become either asymptomatically infected (I_a) or symptomatically infected (I_s). *f* denotes the fraction of infections that become asymptomatic. Asymptomatically infected people recover through natural clearance at a rate r_a and develop temporary immunity to re-infection (*R*) for a duration of $1/\mu$. Symptomatically infected people clear the infection at a rate r_s that can be ascribed to treatment seeking due to symptoms. Both asymptomatically and symptomatically infected people get screened and directly treated at a rate *c*. **Figure 2:** Declining prevalence of *C. trachomatis* after the introduction of a screening programme. Only high screening rates can achieve a significant reduction in prevalence within a reasonable time span. Solid line, screening rate of 0.05 per year; dashed line, screening rate of 0.25 per year; dotted line, screening rate of 0.50 per year.

Figure 3: Prevalence of *C. trachomatis* as a function of the rate at which the population receives screening. In the long-term, screening more than 10% of the population would eradicate *C. trachomatis* from the population. Due to the slow decline in prevalence, however, this is only expected after screening over several decades. Dotted line, prevalence after 5 years of screening; solid line, prevalence after 10 years of screening; dashed line, new steady-state that is expected in presence of a screening programme.

Figure 4: (A) Prevalence of *C. trachomatis* as a function of the fraction of infections that become asymptomatic. For the most reasonable estimates of f, the reduction in prevalence is only slightly affected. (B) Prevalence of *C. trachomatis* as a function of the duration of the symptomatic period. The reduction in prevalence is only slightly affected by the duration of the symptomatic period. (C) Prevalence of *C. trachomatis* as a function of the duration of the asymptomatic period. Most estimates on the duration of the asymptomatic period are within 200–400 days, which results in large differences of the predicted impact of long-term screening programmes. In all graphs: Dotted line, baseline prevalence in the absence of a screening programme; dashed line, long-term prevalence if the population receives screening at a rate of 0.05 per year; solid line, prevalence after screening the population at a rate of 0.25 per year for 10 years; gray area, parameter range; black dots, baseline scenario as given in Table 1. Figure 5: (A) Prevalence of C. trachomatis as a function of the duration of the incubation time, i.e., the time people are infected but not yet infectious. (B) Prevalence of C. trachomatis as a function of the duration of temporary immunity. In all graphs: Dotted line, baseline prevalence in the absence of a screening programme; dashed line, long-term prevalence if the population receives screening at a rate of 0.05 per year; solid line, prevalence after screening the population at a rate of 0.25 per year for 10 years; gray area, parameter range; black dots, baseline scenario as given in Table 1.

Figure 6: Persistence of *C. trachomatis* in asymptomatically infected women as given in (Molano et al., 2005). Fitting a mathematical model that includes natural clearance and re-infection (see *Methods*) results in a natural clearance rate of $r_a = 0.84$ per year (95% CI: 0.82–0.87 per year) and a re-infection rate of $\alpha = 0.01$ per year (95% CI: -0.01–0.03 per year). The low re-infection rate indicates that the data is mainly described by natural clearance and we obtain a mean duration of the asymptomatic period of 433 days (95% CI: 420–447 days).

Figure 7: Stochastic implementation of the SEIRS model in an individual-based population. (A) Contact network during a period of one year. For illustrative purposes, the population size was limited to 100 which results in higher connected components compared to larger population sizes. (B) Variation in *C. trachomatis* prevalence if the population is stratified by sexual behavior. Each bar represents a risk group with a given number of contacts within the last year. The width of the bar represents the fraction of the population that belongs to the specific risk group (see legend). The height of the bar indicates the prevalence of *C. trachomatis* within that group. The gray area within each bar corresponds to the total amount of infections within the group. The overall prevalence is given by the dashed line. Population size: 10'000.

Figure 8: Two-way sensitivity analysis of disease-specific parameters on the impact of a screening programme. The density plots describe the new steady-state prevalence of *C. trachomatis* in the presence of a screening programme (c = 0.05 per year). (A) Varying the duration of the asymptomatic period $(1/r_a)$ together with the fractions of infections becoming asymptomatic (f). (B) Varying the duration of the asymptomatic period $(1/r_a)$ together with the fractions of infections becoming used is outlined by the white dashed rectangle and the baseline scenario is given by the white dots (Table 1). The white area indicates extinction of the infection from the population.

Figure 9: Infection rate β and the mean duration of infectiousness as a function of diseasespecific parameters. Changing the fractions of infections becoming asymptomatic (A), the duration of the symptomatic period (B) and the duration of the asymptomatic period (C) within the range that has been previously used (gray area) results in values of β (solid lines) that are between 1.3 and 3.9 per person per year. Taking into account symptomatic and asymptomatic infections, the mean duration of infectiousness $(f/r_a + (1-f)/r_s)$, dashed lines) is in the range of 101–300 days.