

Perspective on the next generation of ultra-low noise fiber supercontinuum sources and their emerging applications in spectroscopy, imaging, and ultrafast photonics

Anupamaa Rampur,¹ Dirk-Mathys Spangenberg,¹ Benoît Siervo,¹ Pascal Hänzi,¹ Mariusz Klimczak,² and Alexander M. Heidt^{1, a)}

¹⁾*Institute of Applied Physics, University of Bern, Sidlerstrasse 5, 3012 Bern, Switzerland*

²⁾*Faculty of Physics, University of Warsaw, Pasteura 5, 02-093 Warsaw, Poland*

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A new generation of ultrafast and low-noise supercontinuum (SC) sources is currently emerging, driven by the constantly increasing demands of spectroscopy, advanced microscopy, and ultrafast photonics applications for highly stable broadband coherent light sources. In this perspective, we review recent progress enabled by advances in nonlinear optical fiber design, detail our view on the largely untapped potential for noise control in nonlinear fiber optics, and present the noise fingerprinting technique for measuring and visualizing the noise of SC sources with unprecedented detail. In our outlook we highlight how these SC sources push the boundaries for many spectroscopy and imaging modalities, and focus on their role in the development of ultrafast fiber lasers and frequency combs with ultra-low amplitude and phase noise operating in the 2 μm spectral region and beyond in the mid-IR.

INTRODUCTION

Optical spectroscopy and imaging using broadband coherent light sources that cover multiple molecular absorption bands and spectroscopic regimes have enabled fascinating insights into the world of molecular dynamics, revealing how greenhouse gases interact with pollutant particles or the unexpected complexities of water molecule vibrations^{1,2}. Supercontinuum (SC) generation based on the nonlinear spectral broadening of high-intensity laser pulses in dispersion-engineered specialty optical fibers is a particularly convenient technique for generating broadband coherent light at wavelengths that are otherwise hard to access³, and these compact and robust light sources have become indispensable tools in many scientific laboratories. However, due to the ever-increasing sensitivity and speed of spectroscopic detection and imaging techniques, the noise properties, shot-to-shot stability and temporal characteristics of fiber-based SC sources are now becoming increasingly relevant.

SC sources in the visible and near-IR have been commercially available for over a decade, and are the excitation source of choice for a range of advanced microscopy techniques, such as multiphoton- and stimulated emission depletion (STED) microscopy⁴ or optical resolution photoacoustic microscopy⁵. In optical coherence tomography (OCT), SC sources facilitate high-speed, high-resolution 3D-imaging across several medical specialties, including ophthalmology and cardiology⁶, and provide an important diagnostic tool in dermatology for the early-stage detection of skin cancer and other skin diseases⁷. Pumped by high repetition-rate pico- or nanosecond pulsed lasers and equipped with the high beam quality of optical fibers, the brightness of these fiber-based SC sources is unparalleled. Table-top SC sources now outperform synchrotron beamlines in the entire range

from visible to mid-IR wavelengths, thus removing the necessity of scarce access to expensive facilities, e.g. for IR microspectroscopy applications⁸. However, due to the stochastic nature of the nonlinear processes involved in spectral broadening, these SC sources provide spatially but not temporally coherent light and exhibit very large pulse-to-pulse fluctuations of spectral amplitude and phase⁹. Although the correspondingly large relative intensity noise (RIN) in the order of 50% can often be reduced by long-term averaging, this SC noise has become the predominating factor limiting acquisition speed, sensitivity, and resolution in many applications¹⁰.

Pumping with mode-locked femtosecond lasers results in considerably more stable SC that preserve the temporal coherence of the pump pulses, and thus enable the formation of phase-stable broadband frequency combs or ultrashort pulses with only a few optical cycles duration^{11,12}. Nevertheless, even in this regime the noise and temporal properties of SC sources are becoming increasingly limiting factors, which are closely linked to the design of the nonlinear fiber used to achieve spectral broadening. Conventional SC sources employ fiber designs with single zero dispersion wavelength (ZDW) closely matched to the central wavelength of the pump pulses, which are injected in the region of anomalous group velocity dispersion (GVD) (Fig. 1 (a)). The resulting coherent nonlinear dynamics dominated by soliton fission generate large spectral bandwidths but rather complex and highly structured spectral and temporal profiles that are mostly unsuitable for ultrafast photonics applications. An additional drawback of this fiber design lies in its facilitation of quantum noise amplification by modulational instability (MI) leading to substantial pulse-to-pulse fluctuations and temporal coherence degradation if it is allowed to dominate, which can only be avoided using very short pump pulse durations and fiber lengths³.

Driven by the increased application demand for ultra-low noise broadband coherent light sources, all-normal dispersion (ANDi) SC sources have recently attracted attention as a promising alternative to conventional SC sources. Their

^{a)}Electronic mail: alexander.heidt@unibe.ch

FIG. 1. Properties of typical fiber SC sources pumped by high peak power femtosecond pulses. Fiber dispersion profiles (top) and projected axes spectrogram (bottom) for (a) conventional SC and (b) all-normal dispersion (ANDi) SC. Pump wavelengths are indicated with arrows. Both fiber designs can be adapted for a large range of different pump wavelengths and can cover wavelengths from the UV to the mid-IR. Spectrograms shown here are simulated, but corresponding measurements are available in literature^{13–15}.

FIG. 2. Origin of SC noise. Simulated spectral evolution of 5 ps, 5 kW pulses in (a) conventional and (b) ANDi fiber from Fig. 1. On top, the mean spectrum is displayed in red, obtained from averaging 20 simulations with random noise seeds. Gray traces show single shot spectra. Arrows indicate primary gain bands for amplification of quantum noise.

entirely normal GVD induces coherent nonlinear dynamics dominated by self-phase modulation (SPM) and optical wave-breaking (OWB), which generate flat and smooth spectra of high quality and power density and preserve an ultrashort pulse that is easily recompressed to few- or even single-cycle durations (Fig. 1 (b))^{16–18}. While the concept was introduced already over a decade ago, it is now rapidly gaining popularity as it becomes increasingly apparent that the fiber design strongly suppresses the gain for noise-amplifying incoherent nonlinear dynamics¹⁹.

The renewed interest in low-noise SC sources has generated new insights into the origins of noise during nonlinear spectral broadening and how it can be suppressed using specialty optical fiber design. In this perspective, we detail our view on the largely untapped potential of dispersion engineering for noise control in nonlinear fiber optics and introduce the noise fingerprinting technique, which visualizes for the first time the close correlation between SC noise and the cross-sectional geometry of a particular nonlinear fiber. We review the motives behind the recent emergence of highly birefringent ANDi fibers as the key-enabling technology for the next generation of ultra-low noise ultrafast SC sources²⁰, and highlight how they are beginning to push the boundaries in several spectroscopy and imaging applications. We further focus on their vital role in the development of ultra-low noise ultrafast fiber lasers and frequency combs operating in the $2\mu\text{m}$ spectral region and beyond in the mid-IR.

ORIGIN OF SUPERCONTINUUM NOISE

The noise properties of SC sources can be understood in terms of a competition between coherent and incoherent nonlinear processes. Low-noise and phase-coherent SC can be generated in the normal dispersion regime under a wide range of conditions when SPM and OWB dominate¹⁹, or in the anomalous dispersion regime when soliton fission dominates, i.e. using pump pulses with very short durations and low soliton numbers³. However, these coherent dynamics can be disturbed by incoherent nonlinear effects, which can build up new spectral components from quantum noise and whose in-

fluence grows with longer pump pulse durations³. Examples of this noise amplification are illustrated in Fig. 2 showing SC generated by (a) four-wave mixing (FWM)-induced modulation instability (MI) and (b) stimulated Raman scattering (SRS). Both nonlinear effects generate gain bands spectrally separated from the input pulse spectrum, providing enormous exponential gain to any seed signal injected into these bands. When this gain remains unseeded, as in these examples, then random quantum fluctuations serve as the seed and are amplified to become significant and eventually dominate the nonlinear dynamics. The noise-seeded spectral components contained in the MI and SRS peaks exhibit random fluctuations in amplitude and phase from shot to shot and are thus incoherent with the pump. With further propagation, cascaded Stokes (redshifted) and anti-Stokes (blueshifted) gain bands emerge and eventually distribute noise throughout the SC pulse. Similar noise amplifying nonlinear effects exist when coherent and incoherent mode coupling between the two principal polarization axes of a fiber is considered.

Is it possible to control or suppress this nonlinear noise amplification with appropriate fiber design? This question is currently being tackled by several research groups, and here we present our perspective on the effective control of noise in nonlinear fiber optics through suitably designed dispersion profile and fiber transversal geometry.

NOISE CONTROL BY DISPERSION ENGINEERING

In order to develop strategies for controlling the stability of SC sources, it is helpful to compare the strength of coherent and incoherent nonlinearities and their dependence on the fiber dispersion profile. The strength of coherent nonlinear dynamics is only weakly dependent on the dispersion regime, as can be concluded from the almost identical expressions for the characteristic length scales of soliton fission and OWB^{21,22}. Therefore, the noise properties of a particular SC source are mainly determined by the gain of incoherent nonlinear effects dominated by MI and SRS. Traditionally, these incoherent dynamics have been treated separately, depending on the fiber dispersion regime; MI is regarded as a dominating mechanism of decoherence in anomalous dispersion²³. In normal dispersion, MI is usually suppressed, and SRS is considered the predominant effect²⁴. Here we provide a different, more comprehensive perspective on noise amplification in nonlinear fiber optics that allows us to unveil the significant potential for control and suppression of noise provided by the well-known concepts of dispersion engineering in specialty optical fibers.

Since the seminal work of Bloembergen and Shen²⁵, it is known that a nonlinear coupling of SRS and FWM occurs in the regime of low dispersion and high nonlinearity, i.e. exactly in the conditions relevant to SC generation. In a single-mode fiber, the interaction between these two nonlinear processes can be described by the mixed parametric Raman (MPR) gain²⁶ and given by

FIG. 3. Mixed parametric Raman (MPR) gain g_{MPR} , Eq. (1), normalized by the standard Raman gain g_R . We use the MPR gain to describe the dispersion dependence of noise-amplifying incoherent nonlinearities in SC generation dynamics. Typical conditions for octave-spanning SC generation for ANDi and conventional SC from Fig. 1 are indicated.

$$g_{MPR} = 2\gamma\Re\left(\sqrt{K(2q-K)}\right), \quad (1)$$

where $K = -\beta_2\Omega_R^2/(2\gamma P_0)$ describes the ratio of chromatic dispersion and nonlinearity, with fiber dispersion coefficient β_2 and nonlinear parameter γ , peak angular frequency shift of the Raman gain Ω_R , and pulse peak power P_0 . The factor $q = (1 - f_R) + f_R\chi_R^{(3)}(-\Omega_R)$ contains the Raman susceptibility $\chi_R^{(3)}$ and fractional contribution f_R (~ 0.18 for silica) of the Raman effect to the total nonlinear response of the fiber material. Fig. 3 shows g_{MPR} for a silica fiber as a function of K , normalized to the standard Raman gain coefficient $g_R \simeq 0.5\gamma$.

Eq.(1) describes an explicit dependence of the Raman gain on chromatic dispersion and nonlinearity, and its validity in nonlinear fibers has been experimentally verified^{27,28}. However, so far its implications for the control of nonlinear noise amplification by engineering the fiber dispersion profile have not been fully realized. While our recent work has shown the important role of the MPR gain for the noise properties of ANDi SC¹⁹, we believe that it can in fact be applied more universally to explain the observed noise properties of SC generated in both dispersion regimes. In Fig. 3 (c), mainly the region $|K| < 1$ is relevant to SC generation, where we observe a strong suppression of the MPR gain in normal dispersion, while MPR-induced noise-amplification is strongly amplified in the anomalous dispersion region. The peak of the MPR gain is located at $K \simeq 1 - f_R/2$, where Stokes and anti-Stokes Raman sidebands are effectively amplified by MI, whose role in the coherence collapse of conventional SC has been investigated since the early days of fiber-based SC generation^{23,29}. When we consider the typical conditions for octave-spanning SC generation, we find that the MPR gain and associated noise amplification can be decreased by over one order of magnitude by changing from the conventional to the ANDi fiber design. In fact, this order of magnitude difference in noise susceptibility is a recurrent factor found in many theoretical and experimental studies, as we detail below, and can be seen as the main reason behind the attraction of ANDi fibers for low-noise SC source development.

From this fundamental physics perspective, we expect ANDi SC to be significantly more stable than conventional SC. Detailed numerical and experimental studies have confirmed this expectation. The competition between the coherent and incoherent dynamics typically leads to a threshold pulse duration T_{crit} or threshold soliton number N_{crit} above which the nature of the SC changes from coherent to incoherent^{3,30}. The ANDi fiber design exhibits about 10x higher T_{crit} and 50x higher N_{crit} than its conventional counterparts for octave-spanning bandwidths¹⁹. Describing inco-

FIG. 4. Noise fingerprints of various ANDi SC (a-e) and conventional SC (f) pumped by an Er: fiber laser (80 fs, 40 MHz) at 1550 nm, generating comparable bandwidths in the range 1.2-2.2 μm . (a) Microscope image of low-birefringence all-solid ANDi photonic crystal fiber (PCF)³¹. (b) Integrated RIN values (in %) of SC generated in fiber (a) shown in a polar plot in dependence of pump pulse polarization orientation. Corresponding orientation of the fiber geometry shown in background. The fiber's slow axis is aligned to zero degrees. The red-dotted line shows the RIN of the pump laser (0.05%). (c) Detailed noise spectra in a range 10 Hz–20 MHz for positions 48° and 83° (fast axis) of noise fingerprint in (b), and position 0° (slow axis) of noise fingerprint in (d). Pump laser noise and detection noise floor shown for comparison. (d) Noise fingerprint of SC generated in silica polarization-maintaining (PM) air-hole microstructured PCF³², (e) nanohole suspended-core ANDi fiber³³, and (f) commercial conventional fiber NKT PM-1550-01.

herent nonlinear dynamics in terms of the MPR gain is therefore a successful concept for explaining the superior stability of ANDi SC. It also provides a new perspective on the considerable potential for noise control in nonlinear fiber optics. A future challenge will therefore lie in the development of new fiber designs specifically tailored for low-noise operation in a variety of nonlinear frequency conversion applications.

NOISE CONTROL BY DESIGNING FIBER GEOMETRY AND BIREFRINGENCE

Every fiber exhibits a certain amount of birefringence that breaks the degeneracy of polarization modes. Birefringence might be induced unintentionally by unavoidable external stresses or bending of the fiber, or it can be engineered, e.g. by including stress rods or asymmetries into the design of the fiber cross-sectional geometry. The coherent and incoherent coupling of the fiber's polarization modes leads to several nonlinear effects that, in addition to the MPR gain, have the potential to amplify quantum noise and result in unpredictable fluctuations of the polarization state. In the context of ANDi SC sources especially relevant are polarization modulation instability (PMI)^{34,35}, cross-phase modulation instability (XMI)^{36,37}, and Raman amplification assisted by cross-phase modulation^{38,39}.

In general, the occurrence of noise amplification is a complex function of fiber birefringence and dispersion, as well as relative orientation of input pulse polarization and fiber axes. In Fig. 4 we present preliminary results of high resolution polarization-dependent RIN measurements visualizing this complexity. For these measurements, pulses from an ultrafast Er: fiber laser (80 fs, 40 MHz, 0.05% RIN) were coupled into ANDi fibers with similar dispersion profiles, but very different geometries and birefringence, generating SC with comparable spectral bandwidths in the range 1.2 – 2.2 μm . A rotating half-wave plate in front of the fiber and a synchronized analyzer at the fiber exit control the plane of pump pulse and detection polarization with respect to the fiber geometry. Polarization-dependent RIN values are measured with an angular resolution of approximately 0.2° using a pho-

todiode and electronic spectrum analyzer and visualized in polar plots. These plots were found to be unique for each tested fiber and are therefore referred to as "noise fingerprints".

These measurements reveal a strong correlation between the nonlinear noise amplification and the cross-sectional geometry of a particular fiber, which we attribute to the unique stress profile associated with each fiber structure and its drawing conditions. The ANDi fiber in Fig. 4(a, b) is designed as an all-solid microstructured PCF made from two different soft glasses forming the photonic lattice and inclusions. The structure causes a complex stress pattern due to different thermal expansion coefficients of the two glasses. Since there is no intentional stress axis defined in this design, the resulting birefringence is random and the polarization axes are not well defined, evident by the 83° angle measured between the axes. The complex stress profile is also reflected in the highly polarization-dependent nonlinear noise amplification pattern, which we found to be highly susceptible to environmental disturbances, such as bending the fiber, different clamping conditions, or day-to-day temperature changes.

Since for each angular RIN measurement a full noise spectrum is available, we can identify the underlying noise amplification process for every feature of the fingerprint by analyzing its characteristic noise frequencies (Fig. 4(c)). For example, at 49° the noise spectrum of the SC is shifted upward in comparison to the pump laser due to a significant contribution of excess white noise, which is a characteristic signature of quantum noise amplification, and can therefore be attributed to the occurrence of XMI and PMI. Near the fast axis, on the other hand, we mainly observe low-frequency noise, which indicates polarization instability caused by the cancellation of the small linear fiber birefringence by the nonlinear Kerr effect. In general, we observe a complex superposition of these effects.

Fig. 4 also illustrates that birefringence is an effective control parameter to reduce polarization-dependent noise in ANDi SC generation. With increasing birefringence the noise fingerprints become more regular and environmentally stable, as shown for the airhole-microstructured silica PCF with Germanium-doped core in Fig. 4 (d). Near the slow axis (0°) of this fiber the noise spectrum is virtually identical to the noise of the pump laser (Fig. 4(c)), while we continue to observe a strong correlation of noise features and fiber geometry for off-axis pumping. Eventually, we observe complete suppression of noise-amplifying nonlinear processes for extremely birefringent ANDi fiber designs, such as the nanohole suspended core fiber in Fig. 4 (e), even when the pump polarization is not aligned to one of the principal fiber axes. In contrast, the noise fingerprint of a comparable polarization-maintaining conventional SC source (Fig. 4(f)) is significantly more complex, and shows noise amplification up to a factor of 40. In the test conditions the soliton number is $N \simeq 6$, such that a stable SC is generated when the polarization of the pump pulses is exactly aligned to a principal axis of the fiber. However, even slight misalignment of the polarization in the order of just 1° causes a significant rise of the SC noise.

These measurements highlight the importance of the cross-sectional fiber geometry and the homogeneity of the stress

FIG. 5. (a) Schematic overview of extending and power-scaling Er: fiber ultrafast lasers and frequency combs via nonlinear spectral broadening and coherent seeding of Tm- or Ho: fiber amplifiers operating in the $2 \mu\text{m}$ spectral region. Sources of excess noise of each stage are also indicated. (b) Measured spectrum of a Tm/Ho-codoped chirped pulse fiber amplifier seeded by ANDi SC. (c) Measured pulse at the output of the all-fiber system. Noise spectra of amplified pulses in a system built with low-birefringence fibers (d) and after upgrade of the entire system to PM fibers (e). (b)-(d) Adapted from Heidt et al., *Sci. Rep.* **10**, 16734 (2020)⁴³; licensed under a Creative Commons Attribution (CC BY) license. (e) Adapted with permission from Rampur et al., *Opt. Express* **27**, 35041 (2019)⁴⁴. Copyright 2019 The Optical Society.

profile, in addition to dispersion engineering, for the realization of high-quality, low-noise SC sources. ANDi SC sources designed with these considerations in mind are currently emerging also for other pump wavelengths, providing further experimental evidence for the excellent quality and stability of these broadband coherent light sources²⁰.

APPLICATIONS AND FUTURE DIRECTIONS

The availability of low-noise ultrafast SC sources has a profound impact on the development of next-generation ultrashort pulse sources and frequency combs operating, for example, in the $2 \mu\text{m}$ spectral region. This waveband is particularly important as stepping stone for the exploration of the molecular fingerprint region in the mid-infrared via nonlinear frequency conversion. As schematically illustrated in Fig. 5(a), such systems are often based on mode-locked Erbium (Er)-fiber systems, which are spectrally broadened to the $2 \mu\text{m}$ region in highly nonlinear fibers and used for the coherent seeding of Thulium (Tm)- or Holmium (Ho)-doped fiber amplifiers^{40,41}. This is a convenient approach for extending and power-scaling of Er: fiber technology, which has served as the workhorse for ultrafast photonics and frequency metrology over the past decade and, consequently, has been commercially developed to offer robust, turnkey operation with ultra-low amplitude and phase noise in the $1.55 \mu\text{m}$ window.

However, stable nonlinear spectral broadening dynamics are absolutely critical with this approach, as any noise seed created in the nonlinear fiber will grow exponentially in the subsequent amplifier. In the past, conventional nonlinear fiber designs, often with low-birefringence, were employed in such systems, which made them susceptible to the polarization- and MPR-induced quantum noise amplification discussed above. The resulting RIN values of the amplified output pulse at $2 \mu\text{m}$ were in the range 0.3-0.7%, which corresponds to about an order of magnitude noise amplification compared to the Er: fiber seed laser⁴⁰⁻⁴². This nonlinear noise amplification has recently been identified as the major performance limiting factor in the further development of high-power frequency comb sources at $2 \mu\text{m}$ ⁴².

In recent proof-of-principle experiments we demonstrated that making use of ANDi fibers in the nonlinear broadening stage overcomes these limitations and significantly re-

duces nonlinear noise amplification. A $2\ \mu\text{m}$ Tm/Ho-codoped chirped pulse fiber amplifier system coherently seeded by an ANDi SC was realized⁴³. Fig. 5 (b) shows its spectrum with a -20 dB bandwidth of 320 nm and the comparison to the ANDi SC seed. High quality 66 fs pulses with 70 kW peak power could be obtained at the output of the all-fiber system without employing any additional pulse shortening techniques (Fig. 5 (c)). Due to the suppression of MPR gain in ANDi fibers, the amplified pulses exhibit a RIN of only 0.07%. However, the noise frequency spectrum shown in Fig. 5(d) still shows significantly elevated noise in comparison to the Er: fiber seed laser, crucially also at high frequencies, which is a signature of PMI and XMI occurring in the low-birefringence fibers used in this first implementation. With the upgrade of the complete system to highly birefringent polarization-maintaining fibers any type of nonlinear noise amplification could be suppressed, as evident from Fig. 5 (c), and the amplifier RIN lowered to 0.03%, virtually identical to the Er: fiber seed laser⁴⁴. These experiments also proved that in addition to the suppression of incoherent nonlinearities, the coherent seeding of the entire amplifier gain spectrum with the broadband ANDi SC also effectively suppresses amplified spontaneous emission noise in the amplifier. In combination, the results represent an order of magnitude improvement of amplifier noise over conventionally seeded implementations.

Recent experiments convincingly demonstrated the advantages of ANDi SC over conventional SC in the construction of stabilized frequency combs⁴⁵. In combination with the progress of fiber amplifiers described above, these studies have laid the foundations for exciting opportunities arising from using ANDi SC seed sources for the next generation of ultra-low noise frequency combs and ultrafast fiber amplifiers operating in the $2\ \mu\text{m}$ spectral region, which are currently of tremendous interest for extending the coverage of frequency combs to the molecular fingerprint region (3-20 μm). Two pathways seem particularly attractive for reaching the mid-IR:

(i) *parametric downconversion* in mid-IR transparent nonlinear crystals, which are mostly opaque at $1\ \mu\text{m}$ wavelength, where high power driving lasers would be readily available. Hence, an urgent demand exists for the development of powerful, ultra-low-noise ultrafast fiber laser systems at wavelengths $> 1.5\ \mu\text{m}$ ⁴⁶. The spectral broadening in PM-ANDi fibers discussed in this perspective letter should in future allow the straightforward power scaling of Er: fiber frequency combs in Tm- and Ho: fiber or even Er:ZBLAN amplifiers without significant noise penalties.

(ii) *SC generation in mid-IR transparent ANDi fibers*, e.g. made from chalcogenide glasses, which have seen a fast-paced development in recent years and have achieved spectral coverage up to $12\ \mu\text{m}$ ⁴⁷. A remaining challenge is the realization of highly birefringent fiber designs that can stabilize the polarization state of the SC over such a broad spectral region and avoid polarization-induced quantum-noise amplification. Circular birefringence induced by intentional spinning of the preform during fiber drawing was recently shown to stabilize the polarization state of near-IR SC sources and is a particularly elegant concept to extend to the mid-IR⁴⁸. The helical twisting adds another dimension and degree of freedom to

the fiber design process and could be simpler to realize than comparable methods of controlling linear birefringence when working with technologically less mature soft glass materials. Stable and temporally recompressible ANDi SC generation in the mid-IR is a promising approach to realize all-fiber single-cycle pulse sources, widely tunable femtosecond lasers, and ultra-low noise phase-stable frequency combs in this emerging waveband^{47,49-51}.

While our discussion has so far focused on intensity noise, nonlinear spectral broadening in the normal dispersion regime also has substantial advantages when phase noise or relative timing jitter (RTJ) between the spectral components is considered. ANDi SC generate new spectral components that are temporally synchronized to the pump pulse with RTJ in the order of only 100 attoseconds, while conventional SC exhibit up to 2 orders of magnitude larger fluctuations⁵²⁻⁵⁴. This is due to the coupling of amplitude and phase noise during soliton propagation in anomalous GVD, which is significantly reduced in SPM-dominated spectral broadening in normal GVD. This tight passive temporal synchronization on time scales much shorter than an optical cycle enables exciting prospects that have barely been exploited, e.g. for two-colour pump-probe spectroscopy, coherent combining, or optical parametric chirped pulse amplification.

Low-noise ultrafast ANDi SC sources have also started to push the boundaries in several spectroscopy and imaging modalities. Their recent implementation in hyperspectral SRS microscopy for label-free, chemical-specific biomedical and mineralogical imaging is particularly impressive, as source noise is critically important in this technique and has excluded the use of many other nonlinear spectral broadening schemes⁵⁵. In high-resolution spectral-domain OCT ANDi SC sources have led to a paradigm shift, where image quality is no longer limited by SC source noise but by detection shot-noise⁵⁶. ANDi SC are also starting to replace white-light generation in bulk media like YAG, sapphire or CaF₂ in ultrafast spectroscopy, removing the need for expensive amplified laser systems⁵⁷. In combination with digital pulse shaping and ptychographic algorithms, they facilitate significant signal-to-noise and thus speed improvements in single-beam coherent anti-Stokes Raman scattering (CARS) micro-spectroscopy and multiphoton imaging^{58,59}. The combination of multiphoton microscopy and hyperspectral CARS imaging based on digitally programmable ANDi SC pulses has resulted in an extremely versatile platform for biomedical imaging, offering the potential to translate label-free molecular histopathology for disease diagnosis into routine clinical use⁶⁰. Even without the relatively expensive digital pulse shaping device, broadband multimodal CARS and multi-photon imaging systems based on ANDi SC sources have recently been demonstrated⁶¹. From our perspective this is really just the beginning of a movement that will see these versatile sources of broadband, low-noise, and ultrashort pulses being used in an increasing numbers of applications which so far were not able to use conventional fiber-based SC sources due to their noise or complex temporal pulse shapes.

In nonlinear fiber optics, dispersion engineering has been a highly successful concept to control nonlinear effects and

tailor the properties of a particular light source to application demands. However, this approach has so far mainly focused on coherent dynamics. Its full potential to control or suppress noise amplification by influencing the gain of incoherent dynamics is yet to be explored. Based on the concepts presented in this perspective, we expect the development of new fiber designs specifically tailored to suppress noise in a multitude of nonlinear wavelength conversion processes. Effective noise engineering will also require the consideration of the fiber cross-sectional geometry and stress profile. Highly birefringent fiber designs will probably play a more important role in the future as they seem to inhibit most noise-amplifying nonlinear effects arising from coherent or incoherent coupling of the polarization modes. It is also worth reconsidering longitudinally varying dispersion designs, e.g. by slow tapering of the fiber and adjusting the taper rate for minimizing MPR gain and related build-up of noise. This adds another dimension to the fiber design and enables a variety of innovative hybrid approaches, which exploit both enhanced spectral broadening in anomalous GVD as well as enhanced stability in the normal GVD. While theoretical studies have investigated such designs already over a decade ago³⁰, their experimental realization would be a logical next step given today's substantially increased interest in low-noise SC sources.

DATA AVAILABILITY

The data that support the findings of this study are openly available in the Bern Open Research Information System (BORIS) at <http://dx.doi.org/10.48350/156485>.

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