# Supplements to Examining NHD vs QHD in the GCM THOR with non-grey radiative transfer for the hot Jupiter regime 

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## 1 GCM SIMULATIONS

1.1 Altering Rotation Rate at low gravity
1.2 Altering Gravity
1.3 Altering Irradiance Temperature at low gravity
1.4 Altering Rotation Rate at high gravity
1.5 Altering Irradiance Temperature at high gravity

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|  |  |  |
| :---: | :---: | :---: |
| $\Omega=10^{-5} \mathrm{rads}^{-1}$ | $T_{\text {irr }}=$ <br> $\Omega=10^{-4.5} \mathrm{rads}^{-1}$ | $\Omega=10^{-4} \mathrm{rads}^{-1}$ |



Figure 1. Horizontal wind speed at $10^{\prime} 000 P a$ for the NHD and QHD equation sets with $g=10 m s^{-2}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $\Omega$.

|  |  |
| :---: | :---: | :---: |
| irr | $=2000 \mathrm{~K}, \mathrm{~g}=10 \mathrm{~ms}^{-2}$ |
| $\Omega=10^{-4.5} \mathrm{rads}^{-1}$ | $\Omega=10^{-4} \mathrm{rads}^{-1}$ |



Figure 2. Horizontal wind speed at $100^{\prime} 000 P a$ for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $\Omega$.


Figure 3. Zonal wind speed at each grid point for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $\Omega$. The coloured lines indicate momenta profiles along the equator and its coordinates by the colourbar. The dotted black thin line shows momenta profiles at the latitudes $87^{\circ} \mathrm{N}$ and $87^{\circ}$. The bold coloured lines represent momenta profiles at the western, eastern terminators, sub- and antistellar point. The grey lines represents all the other momenta profiles.


Figure 4. Overturning circulation depicted by the streamfunction $\Psi^{\prime}$ for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $\Omega$.


Figure 5. Overturning circulation depicted by the streamfunction $\Psi$ for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $\Omega$.

|  |  |  |
| :---: | :---: | :---: |
| $\Omega=10^{-5} \mathrm{rads}^{-1}$ | $T_{\text {irr }}=$ <br> $\Omega=10^{-4.5} \mathrm{rads}^{-1}$ | $\Omega=10^{-4} \mathrm{rads}^{-1}$ |



Figure 6. Divergent component of the Helmholtz decomposition at $10^{\prime} 000 \mathrm{~Pa}$ for the NHD and QHD equation sets with $g=10 m s^{-2}, T_{i r r}=2^{\prime} 000 K$ and with altering $\Omega$.

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|  |  |  |
| :---: | :---: | :---: |
| $\Omega=10^{-5} \mathrm{rads}^{-1}$ | $T_{\text {irr }}=$ <br> $\Omega=10^{-4.5} \mathrm{rads}^{-1}$ | $\Omega=10^{-4} \mathrm{rads}^{-1}$ |



Figure 7. Rotational eddy component of the Helmholtz decomposition at $10^{\prime} 000 \mathrm{~Pa}$ for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $\Omega$.

|  |  |  |
| :---: | :---: | :---: |
| $=10^{-5} \mathrm{rads}^{-1}$ | $T_{\text {irr }}$ <br>  <br> $\Omega=10^{-4.5} \mathrm{rads}^{-1}$ | $\Omega=10^{-4} \mathrm{rads}^{-1}$ |



Figure 8. Rotational jet component of the Helmholtz decomposition at $10^{\prime} 000 \mathrm{~Pa}$ for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $\Omega$.

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|  |  |  |
| :---: | :---: | :---: |
| $\Omega=10^{-5} \mathrm{rads}^{-1}$ | $T_{\text {irr }}=$ <br> $\Omega=10^{-4.5} \mathrm{rads}^{-1}$ | $\Omega=10^{-4} \mathrm{rads}^{-1}$ |



10000 Pa

Figure 9. Sign of $\frac{v \tan (\Phi)}{10 w}-1$ at $10^{\prime} 000 P a$ for the NHD and QHD equation sets with $g=10 m s^{-2}, T_{i r r}=2^{\prime} 000 K$ and with altering $\Omega$. Dark blue and bright blue regions show negative and positive values


Figure 10. Horizontal acceleration for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $\Omega$.


Figure 11. Vertical acceleration for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, \boldsymbol{T}_{\text {irr }}=2^{\prime} 000 \mathrm{~K}$ and with altering $\Omega$.


Figure 12. Vertical wind speed at each grid point for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $\Omega$. The coloured lines indicate momenta profiles along the equator and its coordinates by the colourbar. The dotted black thin line shows momenta profiles at the latitudes $87^{\circ} \mathrm{N}$ and $87^{\circ}$ S. The bold coloured lines represent momenta profiles at the western, eastern terminators, sub- and antistellar point. The grey lines represents all the other momenta profiles.

|  |  |
| :---: | :---: | :---: |
| $=10^{-5} \mathrm{rads}^{-1}$ | $2000 \mathrm{~K}, \mathrm{~g}=10 \mathrm{~ms}^{-2}$ |
| $\Omega=10^{-4.5} \mathrm{rads}^{-1}$ | $\Omega=10^{-4} \mathrm{rads}^{-1}$ |



Figure 13. Vertical wind speed at $10^{\prime} 000 P a$ for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $\Omega$. The arrows indicate the horizontal wind speed

|  |  |
| :---: | :---: | :---: |
| irr | $=2000 \mathrm{~K}, \mathrm{~g}=10 \mathrm{~ms}^{-2}$ |
| $\Omega=10^{-4.5} \mathrm{rads}^{-1}$ | $\Omega=10^{-4} \mathrm{rads}^{-1}$ |



Figure 14. Vertical wind speed at $100^{\prime} 000 P a$ for the NHD and QHD equation sets with $g=10 m s^{-2}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $\Omega$.The arrows indicate the horizontal wind speed

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| $\Omega=10^{-5} \mathrm{rads}^{-1}, T_{i r r}=2000 \mathrm{~K}$ |  |
| :---: | :---: |
| $g=25 \mathrm{~ms}^{-2}$ | $g=47.39 \mathrm{~ms}^{-2}$ |



Figure 15. Horizontal wind speed at $10^{\prime} 000 P a$ for the NHD and QHD equation sets with $\Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $g$.


Figure 16. Zonal wind speed at each grid point for the NHD and QHD equation sets with $\Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $g$. The coloured lines indicate momenta profiles along the equator and its coordinates by the colourbar. The dotted black thin line shows momenta profiles at the latitudes $87^{\circ} \mathrm{N}$ and $87^{\circ} \mathrm{S}$. The bold coloured lines represent momenta profiles at the western, eastern terminators, sub- and antistellar point. The grey lines represents all the other momenta profiles.


Figure 17. Overturning circulation depicted by the streamfunction $\Psi^{\prime}$ in tidally locked coordinates for the NHD and QHD equation sets with $\Omega=1 \cdot 10^{-5} r a d / s$, $T_{i r r}=2^{\prime} 000 K$ and with altering $g$.


Figure 18. Overturning circulation depicted by the streamfunction $\Psi$ for the NHD and QHD equation sets with $\Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}, T_{\text {irr }}=2^{\prime} 000 \mathrm{~K}$ and with altering $g$.

| $\Omega=10^{-5} \mathrm{rads}^{-1}, T_{i r r}=2000 \mathrm{~K}$ |  |
| :---: | :---: |
| $g=25 \mathrm{~ms}^{-2}$ | $g=47.39 \mathrm{~ms}^{-2}$ |



Figure 19. Divergent component of the Helmholtz decomposition at $10^{\prime} 000 \mathrm{~Pa}$ for the NHD and QHD equation sets with $\Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $g$.

| $\Omega=10^{-5} \mathrm{rads}^{-1}, T_{i r r}=2000 \mathrm{~K}$ |  |
| :---: | :---: |
| $g=25 \mathrm{~ms}^{-2}$ | $g=47.39 \mathrm{~ms}^{-2}$ |



Figure 20. Rotational eddy component of the Helmholtz decomposition at $10^{\prime} 000 \mathrm{~Pa}$ for the NHD and QHD equation sets with $\Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}$, $T_{i r r}=2^{\prime} 000 K$ and with altering $g$.

| $\Omega=10^{-5} \mathrm{rads}^{-1}, T_{i r r}=2000 \mathrm{~K}$ |  |
| :---: | :---: |
| $g=25 \mathrm{~ms}^{-2}$ | $g=47.39 \mathrm{~ms}^{-2}$ |



Figure 21. Rotational jet component of the Helmholtz decomposition at $10^{\prime} 000 \mathrm{~Pa}$ for the NHD and QHD equation sets with $\Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}, T_{\text {irr }}=2^{\prime} 000 \mathrm{~K}$ and with altering $g$.

| $\Omega=10^{-5} \mathrm{rads}^{-1}, T_{i r r}=2000 \mathrm{~K}$ |  |
| :---: | :---: |
| $g=25 \mathrm{~ms}^{-2}$ | $g=47.39 \mathrm{~ms}^{-2}$ |



10000 Pa

Figure 22. Sign of $\frac{v \tan (\Phi)}{10 w}-1$ for the NHD and QHD equation sets with $\Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $g$. Dark blue and bright blue regions show negative and positive values


Figure 23. Horizontal acceleration for the NHD and QHD equation sets with $\Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $g$.


Figure 24. Vertical acceleration for the NHD and QHD equation sets with $\Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $g$.


Figure 25. Vertical wind speed at each grid point for the NHD and QHD equation sets with $\Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $g$. The coloured lines indicate momenta profiles along the equator and its coordinates by the colourbar. The dotted black thin line shows momenta profiles at the latitudes $87^{\circ} \mathrm{N}$ and $87^{\circ} \mathrm{S}$. The bold coloured lines represent momenta profiles at the western, eastern terminators, sub- and antistellar point. The grey lines represents all the other momenta profiles.

| $\Omega=10 \mathrm{~ms}^{-2}$ | -5 <br> $\mathrm{rads}^{-1}, T_{\text {irr }}=2000 \mathrm{~K}$ <br> $g=25 \mathrm{~ms}^{-2}$$\quad g=47.39 \mathrm{~ms}^{-2}$ |
| :---: | :---: |



Figure 26. Vertical wind speed at $10^{\prime} 000 \mathrm{~Pa}$ for the NHD and QHD equation sets with $\Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $g$.The arrows indicate the horizontal wind speed

| $\Omega=10^{-5} \mathrm{rads}^{-1}, T_{i r r}=2000 \mathrm{~K}$ |  |
| :---: | :---: |
| $g=25 \mathrm{~ms}^{-2}$ | $g=47.39 \mathrm{~ms}^{-2}$ |



Figure 27. Vertical wind speed at $100^{\prime} 000 P a$ for the NHD and QHD equation sets with $\Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $g$.The arrows indicate the horizontal wind speed

|  |
| :--- | :--- |
| $T_{\text {irr }}=1000 \mathrm{~K}$ | | $\Omega=10^{-5} \mathrm{rads}^{-1}, \mathrm{~g}=10 \mathrm{~ms}^{-2}$ |
| :---: |
| $T_{\text {irr }}=1500 \mathrm{~K}$ |$\quad T_{\text {irr }}=2000 \mathrm{~K}$



Figure 28. Horizontal wind speed at $10^{\prime} 000 \mathrm{~Pa}$ for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, \Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}$ and with altering $T_{i r r}$.


Figure 29. Zonal wind speed at each grid point for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, \Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}$ and with altering $T_{i r r}$. The coloured lines indicate momenta profiles along the equator and its coordinates by the colourbar. The dotted black thin line shows momenta profiles at the latitudes $87^{\circ} \mathrm{N}$ and $87^{\circ} \mathrm{S}$. The bold coloured lines represent momenta profiles at the western, eastern terminators, sub- and antistellar point. The grey lines represents all the other momenta profiles.


Figure 30. Overturning circulation depicted by the streamfunction $\Psi^{\prime}$ for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, \Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}$ and with altering $T_{i r r}$.


Figure 31. Overturning circulation depicted by the streamfunction $\Psi$ for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, \Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}$ and with altering $T_{i r r}$.

|  |  |
| :---: | :---: |
| $T_{\text {irr }}=1000 \mathrm{~K}$ | $\Omega=10^{-5} \mathrm{rads}^{-1}, g=10 \mathrm{~ms}^{-2}$ |
| $T_{\text {irr }}=1500 \mathrm{~K}$ | $T_{\text {irr }}=2000 \mathrm{~K}$ |



Figure 32. Divergent component of the Helmholtz decomposition for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, \Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}$ and with altering $T_{i r r}$.

|  |  |
| :---: | :---: | :---: |
| $T_{i r r}=1000 \mathrm{~K}$ | $\Omega=10^{-5} \mathrm{rads}^{-1}, g=10 \mathrm{~ms}^{-2}$ |
| $T_{\text {irr }}=1500 \mathrm{~K}$ | $T_{\text {irr }}=2000 \mathrm{~K}$ |



Figure 33. Rotational eddy component of the Helmholtz decomposition for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, \Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}$ and with altering $T_{i r r}$.

|  |  |
| :---: | :---: |
| $T_{\text {irr }}=1000 \mathrm{~K}$ | $\Omega=10^{-5} \mathrm{rads}^{-1}, g=10 \mathrm{~ms}^{-2}$ |
| $T_{\text {irr }}=1500 \mathrm{~K}$ | $T_{\text {irr }}=2000 \mathrm{~K}$ |



Figure 34. Rotational jet component of the Helmholtz decomposition for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, \Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}$ and with altering $T_{i r r}$.

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| :---: | :---: | :---: |
| $T_{i r r}=1000 \mathrm{~K}$ | $\Omega=10^{-5} \mathrm{rads}^{-1}, g=10 \mathrm{~ms}^{-2}$ |
| $T_{\text {irr }}=1500 \mathrm{~K}$ | $T_{\text {irr }}=2000 \mathrm{~K}$ |



10000 Pa

Figure 35. Sign of $\frac{v \tan (\Phi)}{10 w}-1$ for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, \Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}$ and with altering $T_{i r r}$. Blue and red regions show negative and positive values


Figure 36. Horizontal acceleration for the NHD and QHD equation sets with $\Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}, g=10 \mathrm{~ms}^{-2}$ and with altering $T_{i r r}$.

$\begin{array}{cccccccc}-5 e-03 & -1 e-04 & -5 e-06 & -1 \mathrm{e}-07 & 0 \mathrm{e}+00 & 1 \mathrm{e}-07 & 5 \mathrm{e}-06 & 1 \mathrm{e}-04 \\ & & \text { Difference in density } & 5 \mathrm{e}-03\end{array}$

Figure 37. Vertical acceleration for the NHD and QHD equation sets with $\Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}, g=10 \mathrm{~ms}^{-2}$ and with altering $T_{i r r}$.



| 0 | 30 | 60 | 90 | 120 | 150 <br> Longitude [ ${ }^{\circ}$ ] | 240 | 270 | 300 | 330 | 360 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Figure 38. Vertical wind speed at each grid point for the NHD and QHD equation sets with $g=10 \mathrm{~ms}^{-2}, \Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}$ and with altering $T_{i r r}$. The coloured lines indicate momenta profiles along the equator and its coordinates by the colourbar. The dotted black thin line shows momenta profiles at the latitudes $87^{\circ} \mathrm{N}$ and $87^{\circ} \mathrm{S}$. The bold coloured lines represent momenta profiles at the western, eastern terminators, sub- and antistellar point. The grey lines represents all the other momenta profiles.

$\Omega=10^{-5} \mathrm{rads}^{-1} \quad$| $T_{i r r}=2000 \mathrm{~K}, \mathrm{~g}=47.39 \mathrm{~ms}^{-2}$ |
| :---: |
| $\Omega=10^{-4.5} \mathrm{rads}^{-1}$ |$\quad \Omega=10^{-4} \mathrm{rads}^{-1}$



Figure 39. Temperature and wind speed at $10^{\prime} 000 P a$ for the the NHD and QHD equation sets with $g=47.39 \mathrm{~ms}^{-2}, T_{\text {irr }}=2^{\prime} 000 \mathrm{~K}$ and with altering $\Omega$.


Figure 40. Zonal mean wind at each grid point for the NHD and QHD equation sets with $g=47.39 \mathrm{~ms}^{-2}, T_{i r r}=2^{\prime} 000 \mathrm{~K}$ and with altering $\Omega$.

$\Omega=10^{-5} \mathrm{rads}^{-1} \quad$| $T_{\text {irr }}=2000 \mathrm{~K}, \mathrm{~g}=47.39 \mathrm{~ms}^{-2}$ |
| :---: |
| $\Omega=10^{-4.5} \mathrm{rads}^{-1}$ |$\Omega=10^{-4} \mathrm{rads}^{-1}$



Figure 41. Temperature and wind speed at $10^{\prime} 000 \mathrm{~Pa}$ for the the NHD and QHD equation sets with $g=47.39 \mathrm{~ms}^{-2}, \Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}$ and with altering $T_{i r r}$.


Figure 42. Zonal mean wind at each grid point for the NHD and QHD equation sets with $g=47.39 \mathrm{~ms}^{-2}, \Omega=1 \cdot 10^{-5} \mathrm{rad} / \mathrm{s}$ and with altering $T_{i r r}$.

