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Fast Monte Carlo dose calculation in proton therapy

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Fast Monte Carlo Dose Calculation in Proton Therapy

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Conflicts of Interest Notification

No conflicts of interest to report.

Ethical considerations

This research was approved by the Mayo Clinic Arizona institutional review board (IRB, 13-005709). The informed consent was waived by IRB protocol. Only CT image and dose-volume data were used in this study. All patient-related health information was removed prior to the analysis and publication of the study. research was conducted in accordance with the principles embodied in the Declaration of Helsinki.

Data Availability Statement

The data are available from the corresponding author upon reasonable request.

Abstract

This article examines the critical role of fast Monte Carlo dose calculations in advancing proton therapy techniques, particularly in the context of increasing treatment customization and precision. As adaptive radiotherapy and other patient-specific approaches evolve, the need for accurate and precise dose calculations, essential for techniques like proton-based stereotactic radiosurgery, becomes more prominent. These calculations, however, are time-intensive, with the treatment planning/optimization process constrained by the achievable speed of dose computations. Thus, enhancing the speed of Monte Carlo methods is vital, as it not only facilitates the implementation of novel treatment modalities but also leads to more optimal treatment plans. Today, the state-of-the-art in Monte Carlo dose calculation speeds is 10⁶ - 10⁷ protons per second. This review highlights the latest advancements in fast Monte Carlo dose calculations that have led to such speeds, including emerging artificial intelligence-based techniques, and discusses their application in both current and emerging proton therapy

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Introduction

The standard delivery technique for proton therapy today is pencil beam scanning (PBS)¹⁻ ⁹. PBS involves raster scanning proton beamlets across the tumor volume at discrete locations, spot by spot in the lateral dimension, layer by layer in the longitudinal dimension. The spot position within one energy layer is controlled by two orthogonal steering magnets while the proton range is controlled by changing the proton energy, either by the accelerator directly (synchrotron) or by incorporating energy degraders (cyclotron). The number of protons delivered to each spot position is determined by optimizing the spot weights such that dosimetric objectives are met by introducing dosimetric constraints appropriately together with machine-specific minimum monitor unit limits and by post-processing to adjust the optimized spot weights to be deliverable. These constraints aim to produce a dose distribution conformal to the tumor shape and uniform across the entire tumor volume while minimizing the dose to healthy tissues and in particular, organs at risk (OARs)¹⁰⁻¹³.

The number of degrees of freedom in optimizing radiotherapy treatment plans for cancer patients treated with PBS are vast. For this reason, as computational power has increased since the advent of PBS, the complexity of techniques used to deliver the optimized radiotherapy treatment plans have increased in equal measure. One of the most widely utilized and computationally intensive treatment planning optimization techniques in proton therapy today is known as robust optimization^{14,41}. In robust optimization, the dose is calculated for many potential real-world treatment perturbation scenarios^{42,43} that include patient positioning errors, proton range errors, etc. For each perturbation scenario, *k*, the dose from each discrete spot, *j*, must be calculated once for each geometrical voxel, *i*, during the plan optimization. As an example, for robust optimization in a volume composed of 1,000,000 voxels irradiated by 1,000 spots with 10 perturbation scenarios

considered, 10 matrices (per the number of perturbation scenarios), known as the dose influence matrix, D_{ij}^k (k = 1,2,...,10), are calculated for each spot, each matrix containing 1,000,000,000 elements. The spot weights are then optimized until the dosimetric constraints are met according to the robust optimization approach taken, broadly categorized in two ways, worst-case and stochastic. In the worst-case method, the worst-case perturbation scenario (maximum dose for OARs, minimum dose for target coverage, and maximum dose for target hot spot)¹⁷ is optimized until the dosimetric constraints are met. In the stochastic method, the expected plan quality (weighted average among all scenarios) is optimized. With many optimization iterations, a treatment plan which is "robust" to the perturbation scenarios will emerge. Even as robust optimization is quite complex already, considering that in a time-resolved treatment (4D) that follows the respiratory motion of the patient, the number of dose calculations grows much further still.

An exciting and sophisticated development in the clinical workflow of proton therapy is the concept of adaptive radiation therapy⁴⁴⁻⁵⁰. In a typical course of treatment, the patient will need to make many visits to the hospital to be treated with a fraction of the total prescribed dose, known simply as a "fraction". Ideally, for each fraction, the patient staged for treatment would receive a CT scan and if necessary, the original treatment plan would be adjusted based on the new CT. Finally, the patient would be treated with the newly adapted plan. The plan adaption process, taking place after the CT and before treatment, should not put too much stress on the patient or radiation therapists and should not slow down the proton therapy clinic. Crucially, minimizing the duration of the adaptive process not only alleviates stress on both patients and radiation therapists but also significantly enhances the accuracy and effectiveness of the treatment plan. To allow for adaptive radiotherapy while incorporating other advanced optimization techniques such as 4D robust optimization, beam angle optimization, spot position optimization, linear-energy-transfer-based and relative biological effectiveness optimization^{26,51-64}, the efficiency of Monte Carlo dose calculation methods must be improved greatly.

While optimization and clinical techniques have grown in complexity, so too have dose calculation techniques. Because Monte Carlo-based dose calculations have historically been quite slow, treatment planning has typically been performed using analytical methods⁶⁵⁻⁶⁸. However, it is generally accepted that the most accurate dose calculation techniques utilize the Monte Carlo method as evidenced by the high percentage of clinical utilization more recently⁶⁹. Monte Carlo techniques can reduce range uncertainty by several millimeters versus analytical methods⁷⁰. Additionally, for some emerging techniques in PBS proton therapy (PBSPT), such as dynamic collimation⁷¹⁻⁷⁴ and magnetic resonance (MR)-guided proton therapy⁷⁵, Monte Carlo methods are the only way to handle the relevant complicated particle transports.

In proton therapy, Monte Carlo dose calculation involves tracking individual protons and secondary particles step by step within the patient geometry. At each step, many interactions are possible with varying probabilities, based on physics. The Monte Carlo approach is to sample each independent interaction possibility, at each step, based on their respective probability, and apply the result. As more protons are simulated and the phase space of potential interactions for the entire treatment plan are sufficiently sampled, an accurate dose distribution will converge. The statistical uncertainty in dose for each voxel is therefore directly related to the number of protons which were simulated within the voxel.

General-purpose Monte Carlo simulations developed by the larger physics community have been in continual development for many years and even decades. The most well-known of these codes are Geant4⁷⁶, FLUKA⁷⁷, MCNPX⁷⁸, and PHITS⁷⁹. TOPAS⁸⁰, based on Geant4, is a

popular tool used in proton therapy. Many of the known radiation physics processes and their respective cross sections, built up over generations of experimentation across the world, have been compiled and inserted into these Monte Carlo codes. These codes allow for extreme precision and accuracy in calculations relating to radiation. In proton therapy, these eodes are rightfully considered to be the gold standard for dose calculation. However, these codes are generally not viewed as being viable within the daily clinical workflow as they are much too slow, requiring hours, days, or even weeks to calculate the dose for a single proton therapy plan. For this reason, there has been much effort put into the development of fast Monte Carlo dose calculators specifically tailored for proton therapy⁸¹⁻⁹³ dose calculations. Typically, these specialized Monte Carlo codes are then validated against the gold standard general-purpose Monte Carlo codes. In this article, we will discuss the current status of Monte Carlo dose calculation methods in proton therapy followed by some recent developments which may enable the use of Monte Carlo dose calculation in the most demanding clinical workflows.

Current Monte Carlo dose calculation methods in proton therapy

A. Physics models of Monte Carlo dose calculation methods in proton therapy

The predominant types of interactions between protons and atoms or nuclei of media, with the proton energy in the therapeutic range (usually from 70 to 250 MeV⁹⁴), include Coulombic interactions with atomic electrons, elastic and inelastic interactions with atomic electrons (ionization), Coulombic interactions with atomic nuclei, and inelastic nuclear interactions. Since protons undergo huge numbers of Coulombic interactions with either atomic electrons or atomic nuclei, it is impractical to simulate such Coulombic interactions one by one using Monte Carlo methods. Therefore, continuous models are used for Coulombic interactions. On the contrary, the occurrence of inelastic nuclear interactions, for example, is much less frequent and can therefore

be considered as discrete events. Nonetheless, such discrete events are considerably more complex, requiring a plethora of physics models for the proton-nuclei interaction, which will often lead to the generation of secondary particles including δ -electrons, positrons, neutrons, protons, deuterons, tritons, alphas, and gamma-rays, etc. Consequently, each discrete event requires independent addressment. Based on the aforementioned high-level diagram of the fundamental physics mechanism beneath the proton transport, a Class II Monte Carlo algorithm⁹⁵ is usually implemented to model the proton track in a step-by-step fashion, where associated physics processes are divided into condensed-history (continuous) models and point-like (discrete) models. The step length *d* is determined using $d = \min(d_{vol}, d_{hard}, [d_{max}])$ (the bracket denotes optional variables). d_{vol} is the translational distance between the current position of the proton and the next simulating volume interface, and d_{hard} is the distance to the next discrete event. Usually, a maximum step length d_{max} can be introduced to constrain the step length^{83,84,96}.

According to ICRU Report 46, only a few elements are necessary to describe human tissues, e.g., Hydrogen, Carbon, Nitrogen, Oxygen, Phosphorus, and Calcium. Based on the element concentration, a truncation on the number of elements to be simulated can be predetermined, carefully balancing efficiency and accuracy. Human tissue related materials are constructed as a composition of the simulated elements, with those recommended by Schneider being the most commonly utilized⁹⁷. These materials are then calibrated to the Hounsfield Unit (HU) in the CT image. The physical properties of each material that are necessary for dose calculation in proton therapy have been intensively studied by theoretical and experimental physicists, resulting in well tabulated datasets for direct queries and derivative interpolations.

A.1 Continuous interactions

For the Coulombic interactions with the atomic electrons, protons are continuously slowing down, with production of δ -electrons (ionizations) above the kinetic energy threshold T_e^{min} . In each step, protons lose an amount of energy, subject to energy straggling, described by the formula,

$$d = \int_{E_i - \Delta E}^{E_i} \frac{dE}{L(E)} (1)$$

where E_i is the kinetic energy at the beginning of the step, ΔE is the energy loss. L(E) denotes the restricted or unrestricted stopping power, depending on whether δ -electrons are explicitly considered (> T_e^{min}) or not. In the restricted scenario, the effective stopping power of δ -electrons production process^{81,98} is subtracted from the unrestricted stopping power. The unrestricted and restricted stopping power were well described by the Bethe equation with corrections^{98,99}. PSTAR¹⁰⁰, Geant4, and International Committee for Radiological Units (ICRU) Report 49¹⁰¹ provide tabulated stopping powers of common materials for convenient query and calculations. Alternatively, the stopping power of a material can be expressed by the water stopping power with a correction i.e., the stopping power ratio of the material to water⁸¹. The δ -electrons (no matter explicitly addressed or not) can be considered to deposit energies locally for most scenarios, since the maximum energy T_e^{max} transferred from the most energetic therapeutic protons to δ -electrons corresponds to an electron range around 2 mm in water (Using the T_e^{max} calculated by Eq. (2), the electron range can be estimated by the continuously-slowing-down-approximation (CSDA) range, which can be acquired by searching the corresponding look-up-tables, such as those provided by the National Institute of Standards and Technology, ESTAR, PSTAR, and ASTAR¹⁰²), which is similar to voxel sizes commonly used for dose calculation (2~3 mm). T_e^{max} was given by the formula,

$$T_{e}^{max} = \frac{2m_{e}\beta^{2}\gamma^{2}}{1 + 2\gamma m_{e}/m_{p} + (m_{e}/m_{p})^{2}}(2)$$

where m_e and m_p are the electron and proton rest masses, β is the ratio of proton velocity to the velocity of light (c), γ is the relativistic parameter given by $\gamma = E_p/m_p$ with E_p denoting the total proton energy. However, when it comes to air-inflated tissues like lungs, the such δ -electrons can travel a larger distance, which requires an implicit consideration of the electron transport to further increase the calculation accuracy^{81,98}.

The production of the δ -electrons in the continuously slowing down model of protons (i.e., electrons with subthreshold energies) leads to energy fluctuations of the primary protons (i.e., energy straggling). Two different models of fluctuations are applied depending on the thickness of the absorber material, which is determined by a parameter $\kappa = \Delta E / T_e^{max}$ with ΔE denoting the mean continuous energy loss that can be calculated by Eq. (1)⁹⁹ and approximated by only considering the leading term in the Bethe-Bloch model for $L(E)^{103}$.

Due to the large rest mass ratio between proton and electron, therapeutic protons influenced by Coulombic interactions with the atomic electrons nearly travel a straight line. In contrast, when passing close to the atomic nucleus, protons will be elastically scattered or defected by the repulsive force from the positive charge of the nucleus. In proton therapy, most objects of interest are thick enough to produce a huge number of scattering events (i.e., MCS, multiple Coulomb scattering), whose net influence on the passing proton is a scattering angle ($\Delta\theta$) with negligible energy loss. The overall scattering angle of the MCS is well described by the Moliere's theory¹⁰⁴. A zero mean, θ_0 width Gaussian distribution is an excellent approximation for central 98% of the full Moliere distribution^{85,98}, which corresponds to the small-angle events. The calculation formula for the width θ_0 was initially proposed by Rossi and Greisen¹⁰⁵, and later modified by Highland¹⁰⁶. However, large-angle events can result in a long tail in the Moliere distribution, which cannot be sufficiently reproduced by the Gaussian or even the Gaussian mixture (multiple Gaussian, usually double) distribution. Therefore, a Rutherford-like distribution is added to the central Gaussian distribution to account for the wide tails^{85,107,108}.

A.2 Discrete interactions

With respect to the continuous interactions, the discrete interactions (mainly elastic and nonelastic nuclear interactions for therapeutic protons) are characterized by short-range hard interactions that cause a more profound impact on the proton transport. The occurrence of a discrete event is determined by d_{hard} setup method. If the "fictitious" strategy is used, d_{hard} is calculated by the formula $d_{hard} = -\ln(\eta)/\Sigma_{hard}^{max}$, where η is a random number sample from uniform distribution from zero to unity^{83,96,109}. If d_{hard} is the decisive constraint for the step length d ($d = d_{hard}$), then another number ξ is sampled from a uniform distribution from zero and unity and determined whether ξ is less than $\sum_{hard} / \sum_{hard}^{max}$. If yes, a discrete event occurs. If the d_{hard} is determined by the real total cross section, d_{hard} is sampled by the formula $d_{hard} = -\ln(\eta)/\Sigma_{hard}$ at the very beginning or just after a discrete event^{85,99}. If d_{hard} is larger than the actual step length d, the current step length d will be subtracted from d_{hard} until d_{hard} becomes the decisive constraint for d, triggering a discrete event. For cases where d_{hard} is not the decisive constraint for d, or d_{hard} is the decisive constraint for d yet a discrete event is rejected, the proton is simply transported with continuous interactions (see A. 1) within step length d. Once a discrete event happens, the specific type is determined according to the corresponding contribution to the total cross section and the proton undergoes the determined type of discrete event following the transport with continuous interactions (see A. 1) within step length d.

To reach the nucleus and trigger nuclear interactions, protons need to have adequate kinetic energy to overcome the repulsive Coulomb potential of the nucleus. The elastic nuclear interaction is described in a two-body scheme and the kinetics is usually solved in the center of mass (CM) system. For the *proton-proton elastic interactions*, the partial-wave analysis database Scattering Analysis Interactive Dial-in (SAID)¹¹⁰ tabulated the microscopic cross sections that can be used to calculate the macroscopic cross sections. Meanwhile, Fippel and Soukup⁸¹ generated a formula to calculate the macroscopic cross section based on the SAID database using analytical fitting. Alternatively, total and differential proton-proton elastic cross sections can be calculated by parameterization of Cugnon et al^{82,111}. The angular distribution of protons after the collision is almost isotropic in the CM system, therefore it can first be sampled from a uniform distribution in the CM system and then transformed to the laboratory system. For the proton-nucleus elastic interactions, ICRU 63 and Evaluated Nuclear Data File (ENDF)¹¹² provided total and double differential (proton energy and scattering angle) cross sections for commonly used elements in proton therapy. Tripathi et al¹¹³ also proposed a method for calculating proton-nucleus elastic cross sections. Scattering angles in the CM system can alternatively be sampled according to the parameterization of the elastic differential cross sections proposed by Ranft^{82,108,114}. The scattered protons (both protons in the proton-proton elastic interactions) can be continuously simulated as the primary protons, while the heavier recoils deposit the transferred energy from the incident protons locally due to the large mass ratio between the recoils and protons, leading to negligible transport range compared to the voxel size⁸⁷. It is worth noting that, large angle scattering (Rutherford tails) can either be considered in the cross section used here, or in the MCS previously mentioned.

During proton-nucleus nonelastic interactions, nuclear interactions can lead to a variety of reaction products, including neutrons, protons, deuterons, tritons, alphas, gamma-rays, and heavier fragments. To take full consideration of all these effects requires complicated algorithms like the Geant4 Binary Cascade and pre-compound models⁹⁹. However, in the context of proton therapy, specific simplifications can be made while retaining a high degree of accuracy in terms of therapeutic dose calculation. Neutrons are usually neglected due to the trivial contribution to the local dose distribution^{81,112,115}. Heavy fragments, having such a short range, do not require tracking and can be adequately simulated by depositing energy locally. The angle and emission energy of protons, deuterons, tritons, and alphas can be directly sampled from the double-differential cross sections given in ICRU 63. Secondary electrons, tritons, alphas, other heavy ions, and nuclear fragments deposit energy locally^{81,83} in the simplest approximation where either the range of these particles are within one voxel of a certain scoring resolution or the scoring contribution of these particles are negligible compared to the primary protons. The secondary deuterons are either tracked or converted into protons in some fast MC codes such as Virtual Particle MC (VPMC). In less simplified models, such secondaries (not necessarily all of them) are simulated as if they were protons with energy and mass corrections to conserve energy and the proton-equivalent range^{83,116}. More explicit simulations of such secondaries can also be carried out in the same manner as protons using the ENDF database. Prompt gamma-rays, which may be of fundamental importance for proton range verification¹¹⁷ and imaging^{118,119} techniques, are typically neglected when only proton dose is desired, however their inclusion in Monte Carlo dose calculations may become important if prompt gamma-ray detection techniques are implemented for clinical use.

B. Monte Carlo-based Dose Calculation and Robust Optimization of a PBS proton therapy

plan

In the dose calculation and robust optimization (essentially the calculation of the influence matrices) of a PBSPT plan, protons are simulated starting from the exit of the treatment gantry nozzle before any beam modification devices. Within the whole simulating domain, two different coordinates are used, i.e., the beam eve view (BEV) coordinate corresponding to the configuration of each treatment field (field angle, field isocenter, and lateral scanning position of each spot) and the associated devices (range shifters and apertures), and the CT coordinate corresponding to the patient setup. In both the BEV and CT coordinates, the governing physics models for proton transport are the same, described in the previous sections. When protons finish the propagation in the BEV coordinate (range shifters, apertures, or air gaps) and reaches the surface of the patient, a coordinate transformation is carried out based on the configuration of each treatment field and the CT coordinate will be used in the patient body. A common difference between the proton simulation outside and inside the patient body is that the simulation inside the patient body is voxelized with dose and linear energy transfer (LET) scoring¹²⁰, while the simulation outside the patient body may treat beam modifying devices as coherent 3D objects where the dose and LET are not necessarily scored.

For dose calculation and robust optimization, the dose resolution (i.e., voxel size) is usually not adopted from the CT image resolution, but instead usually set to be 2 to 3 mm, sometimes 1 mm in stereotactic body radiation therapy (SBRT)¹²¹. As a result, to correctly score the dose and LET within a dose voxel, either the CT can be resampled to be identical to the dose resolution via HU number interpolation¹²² or the scored dose in a dose voxel can be weighted by the volume or mass of nearby CT voxels (i.e., CT voxels that have volume overlapping with the dose voxel).

B.1 Dose Calculation of a PBSPT plan

In the dose calculation of a PBSPT plan, the proton energy, lateral scanning position, and the Monitor Unit (MU) of each beamlet are pre-defined through institution-specific machine properties and treatment planning. The dose calculation is carried out beamlet by beamlet, therefore dose calculation of one beamlet is taken as an example for the following detailed implementation. At the beginning, the initial phase space of protons is randomly sampled according to the spatial distribution of the proton beamlet measured/modelled during the beam commissioning process. Then the trajectory of each proton is simulated through the models described in previous sections, with dose or energy deposition scored within each voxel. The corresponding secondary protons to be simulated are treated in the same workflow as the primary proton, with their initial phase space sampled from the nonelastic nuclear interaction model where they are generated. For other secondaries except proton, certain approximations or additional simulations are needed according to physics models described in Section A. In a Monte Carlo simulation of the dose distribution of one primary proton, the simulation should be repeated enough times to achieve reasonably low statistical uncertainty (usually around 1% in the target voxels for a plan with all beamlets considered). Then the averaged dose distribution of one primary proton can be calculated, which is then multiplied by the number of protons from the beamlet determined by the weight of the beamlet (MU number), which is converted to number-of-protons based on the MU-proton number conversion curve. After finishing the dose calculation for each beamlet, a summation over the dose distributions of all beamlets is done to obtain the final dose distribution of a PBSPT plan.

B.2 Robust Optimization of a PBSPT plan

In the clinical practice of robust optimization of a PBSPT plan, the fundamental procedure is to calculate the influence matrices¹²³, $D_{i,j}$, i.e., the contribution of *j*-th spot with unit intensity at *i*-th

voxel in the region of interests (ROIs), which can be considered as spot-by-spot dose distributions in proton therapy. Though the basic dose calculation method is the same as the method in the dose calculation of a PBSPT plan, a few differences need to be emphasized. First, in the robust optimization, constraints to shape the dose distribution are structure-based. Therefore, the voxels to be considered are the Boolean summation of the contained voxels of each selected structure (i.e., the region of interests), where constraints are placed upon, usually resulting in a much smaller number of dose voxels than the total dose voxels in the case of dose calculation of a PBSPT plan. Second, the beamlets (energy and position) to be used are not pre-determined but can be selected via raytracing to the target volume. Third, the number of protons within each selected beamlet (i.e., MU) is not pre-determined, but is set to be unit intensity across all selected beamlets during the calculation of influence matrices, which are then used to optimize the MU for each beamlet, according to the constraints, yielding the optimized dose distribution in terms of target coverage and OARs sparing.

As for the PBSPT plan robustness¹²⁴⁻¹²⁶, the patient setup uncertainties and the proton range uncertainties^{42,43} are usually considered in the robust optimization. For patient setup uncertainties, the isocenter of each treatment field is usually shifted a distance (usually 3-5 mm), up and down in three cardinal directions. For proton range uncertainties, the stopping powers (or stopping power ratios) of all the materials are scaled up and down usually by between 2% - 3.5%. Then the patient setup and proton range uncertainties are combined to construct a space of perturbation scenarios (including the nominal one without uncertainties considered). For each robust scenario, a corresponding influence matrix can be calculated. Worst-case robust optimization^{14,17} is one of the most widely used methods where for each voxel, the worst-case dose value (maximum dose for OARs, minimum dose for target coverage, and maximum dose for target hot spot) is select to

evaluate the plan quality and guide the robust optimization process. While we have presented common practices above, note that more advanced/comprehensive considerations could be done per the clinical case and the institution's capability, such as random setup uncertainties, respiratory motion uncertainties, and delivery specific uncertainties¹²⁷ (aperture positioning or aperture shape), etc.

Recent Developments and Applications

A. Graphic Processing Unit Acceleration

Graphic Processing Unit (GPU) with the Compute Unified Device Architecture (CUDA) framework is a commonly used tool to accelerate Monte Carlo simulations in PBSPT^{82,84,88,89,128,129}, while Open Computing Language (OpenCL) framework is also used⁸⁵. In CUDA, every 32 threads are grouped into one warp, in which the same instructions are executed for each thread simultaneously. However, if control flow branches (if... else...) exist, the runtime of the threads may diverge, significantly reducing the parallel efficiency⁸⁸.

In the Monte Carlo simulation, there are generally two particle tracking strategies, eventbased^{129,130} and history-based. In the event-based technique, particle history is split into basic components (such as continuous interactions, ionizations, elastic nuclear interactions and nonelastic nuclear interactions), which are first accumulated and then processed by different corresponding kernels. This technique is friendly for GPU acceleration and is inherently immune to the thread divergence problem. Although event-based techniques avoid the divergence problem, they suffer from global memory latency¹³⁰. In contrast, the history-based technique is more widely adopted, in which the particle history is continuously tracked until the termination condition is satisfied. Since proton histories differ, with secondary particle generation being the biggest branch, the thread divergence problem is inevitable.

Several techniques have been developed to address the divergence problem in GPUaccelerated proton dose engines implemented in a history-based fashion. In gPMC⁸⁴, protons were simulated in batches with a size of *M*, with a special stack created to store secondary protons. In each batch, *M* protons were simulated while the daughter protons were stored in the stack. All other secondary particles were not tracked and were locally deposited for simplification. When the stack contains *M* or more daughter protons, the stack would pop up *M* protons to GPU to be simulated in the following batch. The gMC method⁸² introduced two loops of particle simulation; primary protons are simulated in the first loop, and secondary protons generated are stored and processed only after all primary protons have been simulated. This process repeats until all secondary protons are simulated. Lastly, MOQUI⁸⁹ adopted a similar strategy to gMC and gPMC for managing thread divergence by queuing secondary particles for later simulation, but it innovated by utilizing a hash-table to efficiently manage the limited GPU memory, allowing for the scoring of quantities that would otherwise require extensive memory.

B. Track-Repeating Algorithm

Track-repeating is a concept to sample particle tracks from a pre-calculated database of particle histories instead of on-the-fly calculation in Monte Carlo simulation of particles not only for protons⁹⁰, but also for photons, electrons, and carbons^{131,132}. To generate the tracks, one could use protons of multiple energies (including the highest) or the protons of the highest energy only to balance the memory consumption and simulation time. For each step in the track, a complete set of particle's information without degeneracy can be recorded, such as phase space, energy at the start of the step and energy deposit within the step¹³² or the transport length, angles relative to the

previous step, energy loss, and energy deposit⁸⁶. The tracks can be generated using only water phantom, complemented by modification of the particle's information during the repeating of one selected track⁸⁶, or using different materials so as to select the track corresponding to the material at the location of the particle¹³². Since only the tracks of protons of a few (or the maximum) energies are pre-generated, whereas protons of a wide range of energies (compared to the tracked protons) are used in a PBSPT plan, the starting step corresponding to protons of a certain energy used in a PBSPT plan needs to be searched out to truncate the corresponding tracks. For this, the "in-track search" method can be used¹³², potentially done during pre-processing. The tracks of secondaries (usually only secondary protons) are also recorded, and secondaries can be treated the same as primary protons. Such a technique is very GPU-friendly, since by assigning the same proton history within a CUDA block only with different starting positions in the normal direction of the beam, each GPU thread essentially performs the same operations all the time.

C. Virtual Particle Monte Carlo

Virtual Particle (VP) is a novel concept proposed as a counterpart to a realistic particle, the particle conventionally considered in a Monte Carlo simulation of proton therapy, i.e., primary protons and the corresponding secondaries generated during the tracking history of the primary protons⁸⁸. VP is a statistical concept that equivalently converts the histories of realistic particles (i.e., primary and secondary protons with further simplifications) to the histories of VPs, in terms of particle transport and energy deposit (thus dose and LET calculation^{133,134}). For a conventional Monte Carlo simulation of proton therapy, the user does not know how many secondary particles will be generated prior to the simulation. Therefore, the primary protons are sampled initially and secondary particles generated during the simulation are first stored and then simulated using similar methods as primary protons. For VPMC, there are no secondary particles generated during

the simulation. Each VP corresponds to one realistic proton (either primary or secondary). The user determines the number of VPs to be simulated at the very beginning. Every VP is simulated equivalently with the same control logic and the same memory buffer, which is very friendly to the GPU hardware architecture.

For continuous physics interactions, realistic protons and VPs are treated similarly. In contrast, for nuclear reactions where secondary particles are generated, conventional MCs usually employ physics parameters of the nuclear reaction probability (cross section), the deposited energy, the energy loss (energies from neutrons and gamma rays escaped from human bodies), and the deflection angle to describe the evolution of realistic particles (primary and secondary). Since there are no secondary particles generated in VPMC, those physics parameters used in conventional Monte Carlo codes are not sufficient to correctly describe the situation and score the energy due to the mass change (i.e., generation of secondary particles in conventional Monte Carlo codes). Thus, besides the conventional physics parameters, another virtual parameter "weight gain" specific to VP is proposed for the correct dose calculation of the VPs in the final scoring stage. In other words, weight gain is proposed for conservation in terms of particle transport and energy deposit between conventional Monte Carlo codes and VPMC statistically. In continuous process, the status of VP will be updated with weight gain unchanged, while for a nuclear reaction, VP status as well as weight gain will be updated.

In order to more efficiently update the status of VP, the pre-calculated physics parameters (the deposited energy, energy straggling, the deflection angle, weight gain, and the ionization probability) databases (i.e., probability density functions), which are generated based on the simulation records of realistic particles using a conventional Monte Carlo dose engine in phantoms

 with different materials, are also used for database querying instead of on-the-fly calculation, taking advantage of CUDA's powerful capability of texture.

D. Beamlet-free dose optimization

As previously discussed, current methods for dose optimization typically include the calculation of the dose influence matrix for a number of perturbation scenarios, followed by optimizing the intensity of each beamlet. These influence matrices can be extremely large, requiring significant memory. Additionally, the matrix multiplications required during gradient descent of the objective function can be costly, reducing the speed of the optimization. Although the optimization process itself is typically separated from the Monte Carlo dose calculations when utilizing the dose influence matrix, it is also possible to optimize the spot weights during the dose calculation¹³⁵. A recently proposed method, known as "beamlet-free optimization"¹³⁶, eliminates the dose influence matrix by combining the dose calculation and optimization process, thereby requiring far less memory (95% reduction) and reducing the overall time from plan creation to the final optimized dose calculation by up to 75% for complex clinical cases.

The beamlet-free dose optimization method utilizes the same cost function as conventional methods, typically including maximum and minimum dose constraints of ROIs and the targets. However, rather than optimizing the intensities of individual beamlets, the beamlet-free algorithm optimizes the dose directly by sampling the cost function during the simulation. This is achieved by simulating a small number of protons at random spot locations and estimating the gradient of the cost function (the difference of the cost function before and after). Given the gradient estimate at the spot position, the spot weight (number of protons to be delivered) is adjusted towards minimizing the gradient. This process is similar to the stochastic gradient descent method. Once optimization is complete, after sampling the cost function sufficiently throughout the dose volume.

the result is the final optimized dose. Unlike dose influence matrix-based optimization methods, no additional final dose calculation or aggregation is required. Although memory demand is not necessarily a concern for modern computation systems, this method may become more important to allow for increasingly complex optimization methods in the future.

E. AI-based Monte Carlo dose calculation and denoising

AI-based image processing can achieve near real-time, ultra-high-quality outputs in many applications^{137,138,139}. Benefiting from AI's rapid progress in image processing, AI-based Monte Carlo dose generation has gradually become a popular research topic in recent years¹⁴⁰. The ultimate goal is to achieve super-fast or even real-time high-precision Monte Carlo dose generation with the aid of AI. AI-based Monte Carlo dose generation can be categorized into two classes: 1) AI-based Monte Carlo dose calculation: This involves determining the precise dose based on a specific set of machine parameters and patient anatomy. 2) AI-based Monte Carlo dose denoising: This method utilizes AI to convert noisy low-statistic Monte Carlo doses to high-statistic Monte Carlo doses.

In contemporary research, the application of advanced deep learning techniques for AI-based MC dose calculation has become increasingly prevalent. This process typically involves the use of patient CT images to generate individualized phantoms, with Monte Carlo simulations employed to produce accurate dose distributions. State-of-the-art models often leverage deep learning networks. These deep learning models are adept at capturing the intricate nonlinear relationships between input data and dose distributions, thereby enabling precise dose predictions. During the training phase, Mean Squared Error (MSE) or Mean Absolute Error (MAE) are commonly utilized as loss functions, and the Adam optimizer is employed for parameter optimization. Empirical evidence suggests that these AI models generally surpass traditional methods in terms of both

computational efficiency and accuracy. Neishabouri et al. demonstrated a long short-term memory (LSTM) network which achieved high accuracy in proton Monte Carlo dose calculations with up to 98.57% γ -index passing rate, and offered a substantial reduction in calculation times ranging from 6 to 23 ms¹⁴¹. Zhang et al. introduced a novel deep learning-based DiscoGAN framework for Monte Carlo dose calculation in proton therapy, achieving consistent performance across various treatment sites and beam energies¹⁴². Pastor-Serrano et al. presented a deep learning algorithm DoTA that calculates proton therapy doses with high accuracy, achieving a 99.37% gamma pass rate compared to Monte Carlo simulations and delivering results in 5 ms¹⁴³. Wu et al. developed a deep learning model that converts the low-precision doses calculated by a pencil beam algorithm to high-precision doses calculated by Monte Carlo methods for proton therapy across multiple disease sites¹⁴⁴.

Another approach in AI-based Monte Carlo dose generation is AI-based dose denoising. This involves using noisy low-statistic doses as inputs, which are then converted into high-precision doses calculated by Monte Carlo methods through AI -based denoising. To implement AI-based Monte Carlo (MC) dose denoising, patient CT images are used to create patient-specific phantoms, and MC simulations generate both noisy and clean dose distributions. Deep learning models, typically convolutional neural networks (CNNs) like UNet, are constructed with enhancements such as voxel shuffle/unshuffle operators to maintain information while reducing computational complexity. During training, these models employ weakly supervised learning frameworks, using noisy input-target pairs to learn the mapping between noisy and clean dose distributions efficiently, thereby improving the speed and accuracy of MC dose calculations for real-time clinical applications. Bai et al. developed a real-time, deep learning-based dose denoiser plugin to covert the noisy low-statistic Monte Carlo dose to high-statistic Monte Carlo dose, enabling the entire

calculation time to be completed in 0.15 s¹⁴⁵. Further studies have reported the application of AIbased Monte Carlo dose denoising in MRI-guided radiotherapy¹⁴⁶, proton therapy^{147,148}, carbonion radiotherapy¹⁴⁹, and also CT imaging dose¹⁵⁰.

Dose generation is a key component in radiation therapy planning, especially in the context of adaptive radiotherapy, involving iterative plan design/finetuning, re-planning, and rapid plan quality assurance^{151,152}. AI-based Monte Carlo dose calculation and denoising techniques have demonstrated remarkable capabilities in providing ultrafast computation speeds and high-precision dose outputs. These advancements enable the rapid generation of high-precision Monte Carlo doses for future online adaptive radiotherapy. Recently, dose prediction is an emerging research area in AI-based dose generation¹⁵³⁻¹⁵⁵, but it's crucial to note that AI-based dose prediction is distinct from AI-based dose calculation and denoising. Dose calculation and denoising refer to determining the precise dose based on a specific set of machine parameters and patient anatomy. In contrast, dose prediction involves determining an optimal dose distribution for a given patient's anatomy. However, the pursuit of AI-based optimal dose prediction, particularly those achieving Monte Carlo-level accuracy, remains a noteworthy direction for research^{156,157}.

F. Apertures in Monte Carlo dose calculations

Apertures are difficult to simulate for two main reasons, their extreme density as compared to normal tissues or bones, and their upstream position, which amplifies poorly approximated aperture interactions downstream due to geometric scaling. Because protons may interact with the aperture and still reach the patient, they cannot be well approximated in analytical approaches. Monte Carlo-based dose calculation methods are currently the preferred methods for simulating apertures in hadron therapy¹⁵⁸. It is for this reason, as well as due to an increasing interest in apertures used in pencil beam scanning hadron therapy, that fast Monte Carlo dose calculators

should support the inclusion of apertures^{71,159-166}. It should be noted that the use of apertures will result in neutron production, however neutrons are not simulated in proton therapy-specific dose calculators. Rather, where there is concern due to neutron production, it is common practice to investigate neutron production in one of the general-use Monte Carlo codes for a subset of patients.

The conventional approach to simulating apertures in proton therapy is to voxelize the aperture. In principle, the aperture can be accurately simulated using a voxelization approach so long as any features in the aperture opening are much larger than the size of the aperture voxels. For small aperture openings, this method can potentially become problematic and inefficient. The voxelization of apertures is intrinsically not well-aligned with how aperture-openings are defined since they are typically defined by an ordered list of points forming a closed polygon in the planes normal to the beam direction. Another method of simulating apertures is to determine whether particles are within the aperture or not based on the crossing number algorithm^{158,159}. This method simulates the aperture in the same geometric manner in which it is defined, avoiding voxelization and using the minimal amount of information to define the aperture geometry, making it a fast and efficient method as well as easily modelling small apertures precisely.

G. Reducing run times of general-use Monte Carlo physics codes

There is a long history of medical physicists implementing general-use Monte Carlo codes such as MCNPX, FLUKA, and Geant4, for radiation therapy applications¹⁶⁷⁻¹⁷² that continues to this day. While these codes are typically viewed as gold standards in terms of dose calculation accuracy, their clinical use has typically been limited to commissioning, verification, or evaluation of clinical software due to long run times. Because these codes track the history of individual particles, allowing for the generation of secondary particles, they are not well suited for acceleration via GPU processing (see Section A). On the other hand, Monte Carlo dose calculations are intrinsically well suited to parallelization using "embarrassingly parallel" methods – distributing the simulation of primary particles across separate nodes (threads, processors, physical nodes, virtual nodes), tracking them to their end, then joining the results from each distributed workload – since no communication is necessary between each processor. Perhaps due to the proliferation of fast, proton therapy-specific Monte Carlo dose calculators, or due to general-use Monte Carlo methods not being well suited for GPUs as-is, there has been relatively little effort put into reducing run times of general-use Monte Carlo codes for the purpose of radiation therapy dose calculation. However, we will highlight some research that has been conducted to this end.

General-use Monte Carlo codes are not merely dose calculators - rather, they are physics simulators, able to account for many radiation-related effects and secondary particles that are mostly neglected by modern, fast Monte Carlo dose calculators (as discussed before), and may therefore take on more important roles as the precision of radiation therapy continues to advance. A few platforms have been envisioned for reducing run times of general-use Monte Carlo codes, notably – MPEXS, a Geant4-based GPU dose engine¹⁷³, however perhaps the most attractive method today is cloud computing. Cloud computing can provide on-demand access to 10s or 1000s of virtual nodes for computation, establishing a pay-per-use cost model as opposed to purchasing and maintaining on-site computer hardware. The main appeal for cloud computing in the context of general-use Monte Carlo codes is that their underlying code does not require modification. The approach for dose calculation in the cloud is essentially the "embarrassingly parallel" approach, splitting up the total number of protons amongst many virtual machines, each running the generaluse Monte Carlo code, then accumulating the results once each node is done. Using this approach, Keyes et. al. $(2010)^{174}$ were able to simulate about 1×10^4 protons per second in a water phantom with FLUKA, including the time to distribute the simulation parameters (patient geometry and

plan information) to each node as well as simulation initialization time. Green et. al. (2015)¹⁷⁵ were able to simulate 2.7x10⁴ protons per second for a realistic plan using Geant4, end to end. Finally, Wang et. al.¹⁷⁶ used cloud computing with FLUKA to study prompt gamma spectroscopy in the context of proton therapy.

Discussion and outlook

Table 1: Monte Carlo-based proton calculation speeds for select studies published since 2015.

Reference	Year	Method	Notes	Protons/s
Virtual particle Monte Carlo: A new	2022	GPU	Voxels: 2.5 mm	2.9x10^7*
concept to avoid simulating secondary			side-lengths, 13	*virtual-
particles in proton therapy dose			patients	particles/s
calculation ⁸⁸				
MOQUI: an open-source GPU-based	2022	GPU	1 H&N, 1 liver,	4.3x10^5
Monte Carlo code for proton dose			and 1 prostate	
calculation with efficient data structure ⁸⁹			patient	
Clinical validation of a GPU-based Monte	2021	GPU	Voxels: 1-3 mm	8.4x10^6
Carlo dose engine of a commercial			side-lengths,	
treatment planning system for pencil beam			100s of patients	
scanning proton therapy ¹⁷⁷				
Commissioning of GPU-Accelerated	2021	GPU	Voxels: 1.5 mm	2.9x10^5
Monte Carlo Code Fred for Clinical			side-lengths, 90	
Applications in Proton Therapy ¹⁷⁸				

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			H&N/brain	
			patients	
Development and Benchmarking of a	2021	CPU multi-	Voxels: 2.0 mm	1.9x10^5
Monte Carlo Dose Engine for Proton		threaded	side-lengths,	
Radiation Therapy ¹⁷⁹			brain patient	1
Fast multipurpose Monte Carlo simulation	2016	CPU multi-	Voxels: 1.0 mm	4.4x10^5
for proton therapy using multi- and many-		threaded	side-lengths,	
core CPU architectures ¹⁸⁰			heterogeneous	
			phantom	
A fast GPU-based Monte Carlo simulation	2015	GPU	Voxels: 1.0 mm	4.8x10^5
of proton transport with detailed modeling		0	side-lengths, 3	
of nonelastic interactions ⁸²			H&N patients,	
			fast version	
Fast Monte Carlo proton treatment plan	2015	Cloud/CPU	Voxels: 1x1x2	5.0x10^4
validation in the Google Cloud ¹⁷⁵		multi-	mm ³ , H&N	
		threaded	phantom	

This review article has presented a detailed overview of the current state of Monte Carlo methods used in proton therapy dose calculation, robust optimization with Monte Carlo dose engines, and recent advances in further increasing speeds. Table 1 provides the reported proton calculation rates of various Monte Carlo-based dose calculators. The reported speeds depend on many factors including the number of voxels, number of GPU or CPU cores used, the desired accuracy, etc., and should therefore not be considered a fair comparison, nor exhaustive. The purpose of Table 1 Page 29 of 41

is to provide context on the overall state-of-the-art regarding proton calculation rates, by reporting rates that have been achieved in the listed studies. Taking this context into account, the current state-of-the-art for Monte Carlo dose calculation speeds is 10⁶-10⁷ protons per second. Indeed, with so many fast Monte Carlo-based dose calculators available today, it appears that the less accurate analytical methods may be soon retired.

The primary motivations for increasing speeds today are robust optimization and adaptive radiotherapy, however many treatment techniques on the horizon, including FLASH, grid therapy, 4D planning, linear-energy-transfer/relative biological effectiveness optimization, as well as the general trend towards increasing fraction doses, all require increasingly accurate and precise dose calculations in addition to faster speeds^{52,181-187}. The many recent developments discussed in this article are causing the field to quickly approach a point where Monte Carlo methods may completely overtake analytical approaches. The rise of artificial intelligence is introducing new opportunities in speeding up Monte Carlo dose calculations as well.

In terms of new techniques that have been developed for fast Monte Carlo dose calculation, accuracy and speed are often inversely correlated. Clinically, these competing concepts, accuracy and speed, must be delicately balanced depending on the application. This is less true when new hardware-centric methods are developed for increasing dose calculation speed. In the case of GPU-based methods, accuracy is sometimes sacrificed to make the calculations more suited for GPU processing. "Embarrassingly parallel" methods can increase speeds without sacrificing accuracy, albeit typically at a higher monetary cost. In general, hardware-based methods increase the cost of dose calculation in order to increase speeds. While AI methods can greatly speed up dose calculations, they are currently not generalizable, unlike conventional Monte Carlo approaches. A dose calculator using AI will only be valid for scenarios that were well represented in the training

data. Therefore, the tradeoff with utilizing AI based methods in the context of dose calculation is an increase in speed at the cost of generalizability. It should be noted, however, that AI methods will likely increase in generalizability with time. With regards to increasing the speed of Monte Carlo dose calculations, there are many factors and tradeoffs that must be carefully considered.

An important question going forward: At what point may we consider dose calculations to be fast enough? Our answer, in short, is that Monte Carlo dose calculations will not be considered fast enough for the foreseeable future. This is primarily due to the high degree of freedom in dose optimization. For example, "robust" in robust optimization is typically referring to robustness with respect to patient setup and proton beam range uncertainties. However, we could also make plans robust to dose calculation methods, HU or material mapping, simulation techniques, etc. As of today, these ideas may be considered too time consuming. However, in the limit where the time to process Monte Carlo-based dose calculations approach zero, we would surely consider many additional robustness scenarios. Furthermore, there are many parameters that are not typically considered for optimization today, due to the long calculation times that would be required. For example, beam angles, number of beams, spot positions, or even the shape of aperture openings, could be better optimized in a more comprehensive fashion. In addition, for any new parameter that is optimized, the parameter might therefore need to be included as a scenario in robust optimization, even further adding calculation time. In general, the high degree of freedom in dose optimization means that there will always be opportunity to implement increasingly complex and high-quality optimization techniques. Additionally, considering recent developments in adaptive radiotherapy, increasing speeds for Monte Carlo-based dose calculators will continue to be an important aspect of proton therapy for the foreseeable future.

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