Finite element analyses of human vertebral bodies embedded in polymethylmethacrylate or loaded via the hyperelastic intervertebral disc models provide equivalent predictions of experimental strength

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Abstract

Quantitative computer tomography (QCT)-based finite element (FE) models of vertebral body provide better prediction of vertebral strength than dual energy X-ray absorptiometry. However, most models were validated against compression of vertebral bodies with endplates embedded in polymethylmethacrylate (PMMA). Yet, loading being as important as bone density, the absence of intervertebral disc (IVD) affects the strength. Accordingly, the aim was to assess the strength predictions of the classic FE models (vertebral body embedded) against the in vitro and in silico strengths of vertebral bodies loaded via IVDs. High resolution peripheral QCT (HR-pQCT) were performed on 13 segments (T11/T12/L1). T11 and L1 were augmented with PMMA and the samples were tested under a 4° wedge compression until failure of T12. Specimen-specific model was generated for each T12 from the HR-pQCT data. Two FE sets were created: FE-PMMA refers to the classical vertebral body embedded model under axial compression; FE-IVD to their loading via hyperelastic IVD model under the wedge compression as conducted experimentally. Results showed that FE-PMMA models overestimated the experimental strength and their strength prediction was satisfactory considering the different experimental set-up. On the other hand, the FE-IVD models did not prove significantly better (Exp/FE-PMMA: R² = 0.68; Exp/FE-IVD: R² = 0.71, p = 0.84).

In conclusion, FE-PMMA correlates well with in vitro strength of human vertebral bodies loaded via real IVDs and FE-IVD with hyperelastic IVDs do not significantly improve this correlation. Therefore, it seems not worth adding the IVDs to clinical models until fully validated patient-specific IVD models become available.

Keywords: Human vertebra, finite element prediction, mechanical testing, failure strength, intervertebral disc
1. Introduction

Vertebral failure constitutes a serious health problem because of its association with back pain, disability and the impairment of life quality (Lips et al., 1999). The risk of vertebral failure is currently commonly determined by a wide range of bone mineral density (BMD) measurements, e.g. the areal BMD (aBMD) and the volumetric BMD (vBMD). However, studies showed only 50% to 70% of the variability in vertebral strength can be predicted by BMD measurements (Ammann and Rizzoli, 2003; Lochmüller et al., 2002). In order to improve the vertebral failure prediction, attention has been paid to other techniques, e.g. the finite element (FE) method, which can represent the bone microstructure not captured by the BMD measurements (Faulkner et al., 1991). Consequently, the FE modelling approach has recently gained increasing interest in predicting vertebral strength (Chevalier et al., 2010; Dall’Ara et al., 2012; Imai et al, 2008) and has shown better failure prediction than aBMD (Wang et al., 2012) and vBMD (Crawford et al., 2003) alone.

The vertebral strength was only assessed using vertebral bodies, whose endplates were either removed or embedded in polymethylmethacrylate (PMMA) to avoid uncertainties regarding the degree of degeneration of the elderly intervertebral disc (IVD) (Buckley et al., 2007; Crawford et al., 2003; Dall’Ara et al., 2012). These boundary conditions, although equivalent (Maquer et al. 2012a),
are not appropriate for the study of failures in vertebral endplate, which is a major failure pattern in the elderly (Rao and Singrakhia, 2003). On the other hand, the failure mechanisms in the vertebra are altered in the absence of IVD (Hussein et al., 2013), which plays an important role in transferring and distributing the compressive load (Adams et al., 2006). Moreover, the IVD stiffness affects the overall ductility of the vertebral bodies (Nekkanty et al., 2010) and the vertebral failure site (Pollintine et al., 2004). Finally, numerical simulations showed that FE models of embedded vertebral body provided different strength and failure patterns compared to models bonded to healthy IVDs (Maquer et al., 2012b). Accordingly, the aim of this study was to investigate whether the classic vertebral body embedded axial compression FE models (referred as FE-PMMA models) are still valid for the prediction of in vitro strength of human vertebral body loaded via IVDs under a wedge compression and if the predictions can be improved using FE spinal models with hyperelastic IVDs and in vitro consistent loading (FE-IVD models).

2. Materials and methods

2.1. In vitro mechanical testing

In this study, 13 T11/T12/L1 spinal segments, without failure, nor osteophytes, were received. The donors were postmenopausal females with a mean age of 79.9 ±
7.9 years [range: 67-90]. DXA bone densitometry (Lunar Prodigy, Lunar Corporation, Madison, WI, USA) was performed for the lumbar spine and both proximal femurs and subsequently all donors were diagnosed with osteoporosis according to the World Health Organization definition with a lumbar or femoral T-score of -2.5 or less. The segments were scanned while frozen using a HR-pQCT scanner (XtremeCT, Scanco Medical AG, Brüttisellen, Switzerland) with an image voxel size of 82 µm³.

Following the standard procedures (Skrzypiec et al., 2013), the specimens were stored and prepared for mechanical testing. The spinal facet joints were removed for the loading to be only transferred via the IVDs. Failures in T11 and L1 were avoided by replacing the cancellous bone with PMMA (Technovit 4004, Heraeus Kulzer, Wehrheim, Germany). The specimens were embedded in metal cups, such that the mid-transverse planes of T12 were horizontal and in neutral posture (no bending).

The embedded specimens were mounted in a computer-controlled servo-hydraulic materials testing machine (MTS Bionix 858.2, Eden Prairie, MN, US). Axial force was applied for 15 min as a preconditioning to account for the post-mortem swelling (Hongo et al., 2008). The applied force was subject-specific and calculated based on the donor’s body weight (300 N for a 70 kg person in standing position) (Nachemson, 1966). After preconditioning, a 4° anterior-posterior wedge
was applied to T11 to induce a wedge fracture loading condition for T12 (Adams et al. 2006) (Figure 1). An x-y-table was installed between the wedge and the actuator to allow free translations in the transverse plane and so to prevent coupled shear loading during assembly.

A quasi static compression loading of 0.1 mm/s was then applied (Brinckmann et al., 1989) and the x-y-table was locked to prevent extensive spinal anterior-posterior movements, eventually leading to rupture between the posterior regions of the IVD and the vertebral body. The test was performed until a dramatic drop of force (>15% of the peak force) was observed on the load-displacement curve. The maximal force measured was defined as the vertebral failure load ($F_{\text{exp}}$).

2.2. Finite element model

Subject-specific FE models of T12 vertebral bodies were created based on the HR-pQCT data. T11 and L1 were not modelled as their deformations were negligible due to PMMA augmentations. T12 models were created using an in-house software (MedTool, Institute of Lightweight Design and Structural Biomechanics, Vienna University of Technology, Vienna, Austria) (Pahr and Zysset, 2008). Quadratic wedge (C3D15) and tetrahedral elements (C3D10) were defined for the cortex and the trabecular bone, respectively, as described in Maquer et al. (2012b). The anisotropic elastic-plastic-damage model from Schwiedrzik and Zysset (2013) was
chosen to simulate the mechanical behaviour of each bone elements based on the local bone content and trabecular morphology.

The solid volume for each IVD was extruded from the superior and inferior endplate surfaces of its adjacent vertebrae (HyperMesh, Version 11.0, Altair Engineering Inc., Troy, MI, USA). The endplate surfaces were extracted from the meshes of T12 or reconstructed from the automatic segmentation of T11 and L1 (MIAF-Spine, Institute of Medical Physics, University of Erlangen, Germany) (Mastmeyer et al., 2006). The IVD volume was discretized with C3D10 and then the elements were organised into annulus fibrosus (AF) and nucleus pulposus (NP) according to the transverse sectional view (Figure 2).

Two IVD materials were used to generate either the classical FE-PMMA models or the FE-IVD models (Figure 3). Hence, linear elastic modulus of 2300 MPa and Poisson’s ratio of 0.3 [Heraeus Kulzer GmbH, Wehrheim, Germany] were applied to both NP and AF elements for FE-PMMA. For FE-IVD, Mooney-Rivlin model was defined for NP and fibre-reinforced hyperelastic model (Moramarco et al., 2010) was chosen for AF. The material parameters are $C_{10}$, $C_{01}$, $C_{20}$, $K_1$, $K_2$ and D, where, $C_{10}$, $C_{01}$ and $C_{20}$ are related to the ground substance; $K_1$ and $K_2$ are parameters characterizing the behaviour of the collagen fibres; D is the incompressibility modulus. Two families of fibres with the angulations of $\pm 30^\circ$
(relative to the transverse plane) (Cassidy et al., 1989) were defined in AF and both families were acting only in tension.

Three different grades of IVD degeneration (healthy, moderately and severely) were identified from the IVD transverse sectional view (Thompson et al., 1990) and simulated in FE-IVD models. It was assumed that IVD degeneration had no effect on AF material properties (Schmidt et al., 2007), which were taken from literature (Moramarco et al., 2010) (Table 1). The material properties for healthy NP were also taken from literature (Schmidt et al., 2007) (Table 1). The dehydration of NP was simulated by changing the incompressibility modulus, whose value was 0.0005 MPa$^{-1}$ for healthy IVD and corresponded to that of AF for severely degenerated IVD (Rohlmann et al., 2006). The incompressibility modulus for moderately degenerated IVD was linearly interpolated (Rohlmann et al., 2006). The stiffening of NP was simulated by modifying the values of $C_{10}$ and $C_{01}$ (Schmidt et al., 2007).

The bone and AF constitutive laws were implemented into Abaqus (Version 6.12, Dassault Systemes SIMULIA Ltd, Providence, RI, USA) via user defined material subroutine. To simulate the axial compression on FE-PMMA models, the bottom nodes from the inferior PMMA block were fully constrained while an axial displacement of 4.0 mm was prescribed to the nodes of the superior PMMA layer. To mimic the experimental loading applied to FE-IVD models, the bottom nodes
from the inferior IVD were fully constrained. A 2-stage loading was conducted on
the cranial nodes of the superior IVD: a first step consisting in a 4° forward
bending was followed by an axial displacement of 4.0 mm to ensure failure of T12.
Non-linear analyses were performed and the FE failure loads \( F_{\text{PMMA}}^{\text{FE}} \) and \( F_{\text{IVD}}^{\text{FE}} \) were computed as the maximal force.

2.3. Statistical analysis

A paired two-tailed t-test was used to compare the vertebral failure loads with the
FE predictions. Regression equations, the coefficients of determination (\( R^2 \)) and
root mean squared errors (RMS) were computed for the linear correlations of the
vertebral failure load with FE predictions (Crawford et al., 2003). Analyses were
performed using PASW statistics 18.0 (SPSS Inc., Chicago, IL, USA) and the
probability of type I error was set to \( \alpha = 0.05 \), i.e. \( p < 0.05 \) was considered
statistically significant.

3. Results

Compared to the experimental failure loads, FE predicted loads were 12% lower in
FE-IVD group (mean \( \pm \) SD, 2.09 \( \pm \) 0.48 kN vs. 1.84 \( \pm \) 0.47 kN, \( p = 0.005 \)) and 18%
higher in FE-PMMA group (2.09 \( \pm \) 0.48 kN vs. 2.46 \( \pm \) 0.62 kN, \( p = 0.002 \)) (Table
2). Both predicted failure loads were significantly correlated (FE-IVD/FE-PMMA:
\( R^2 = 0.94 \)) and showed similar correlation with the experimental vertebral strength
(Exp/FE-PMMA: $R^2 = 0.68$; Exp/FE-IVD: $R^2 = 0.71$) (Figure 4). No significant difference was detected between the absolute value of the residuals from the FE-IVD and FE-PMMA regression models ($p = 0.84$).

4. Discussion

The study confirmed that the PMMA embedding is providing a higher vertebral strength, which is probably because a larger portion of the load is carried by the cortex (Homminga et al. 2001, Maquer et al. 2012b). Yet, despite different loading conditions, the FE-PMMA models provided a satisfactory prediction of the failure loads of vertebral bodies under a $4^\circ$ wedge compression via IVDs and showed the same predictive power as the FE-IVD models ($R^2 = 0.68$ vs. 0.71). FE-PMMA models are more reproducible by avoiding approximation regarding the degree of elderly IVD’s degeneration (Dall’ara et al. 2012), computationally more efficient and ease of clinical implementation. This essentially indicates that FE-PMMA models are satisfactory (Buckley et al., 2006), although rigid boundary conditions are prescribed to the endplates and axial compression conducted. This agreed with Yang et al.’s (2012) study where it was found that a $5^\circ$ forward flexion does not significantly affect the spatial distribution of stress within the vertebral body.

The hyperelastic IVD model, although reasonable for simulation of the kinematic of the spine (Moramarco et al. 2010), and the instantaneous response of IVD (Jones, et al., 2008), is hardly applicable to simulate the \textit{in vitro} load transfer
to the endplates. Indeed, the accuracy of the vertebral strength predictions is highly
dependent on the degree of simplification of those IVD models (Jones, et al.,
2008). While the latest image-based bone models (Pahr, et al., 2012; Hosseini, et al.,
2012) move towards patient-specific modelling (Gefen, 2012), such step is still to
be taken regarding the IVD modelling. In this study, IVD shape was deduced from
the endplates of the neighbouring vertebral bodies (Moramarco, et al., 2010;
Homminga, et al., 2012). MRI is able to accurately capture the IVD morphology,
but the IVD geometry in most FE models are idealised and rarely based on MRI
data (Moramarco, et al., 2010; Schmidt, et al., 2007). The distinction NP/AF is
hardly possible with degenerated IVDs (Ellingson et al. 2012). Moreover, discrete
degrees of degeneration were simulated as commonly done in most degeneration
schemes (Thompson et al. 1990, Pfirrmann et al. 2001). Considering the range of
alterations observed in moderately to highly degenerative IVDs and that the elderly
IVDs in this study were likely having different degenerative levels, a discretization
constitutes a considerable simplification. Quantitative MRI data correlates with the
IVD’s mechanical properties (Périé et al. 2006, Campana et al. 2011, Maquer et al.
2014) but such information have not been applied to an IVD model.

Hence, despite the small sample size, this study showed that the vertebral
strength computed by FE-PMMA models correlated well with the in vitro strength
of human vertebral bodies loaded via real IVDs. The FE-IVD models did not
significantly improve this correlation, probably due to a lack of patient-specific disc models. In conclusion, for clinical assessment of strength, it is probably not worth the trouble of adding the discs to vertebral body models until fully validated patient-specific IVD models become available.

**Ethical approval**

Ethical approval has been obtained from the Ethics Committee of the Hamburg Chamber of Physicians (PV3486).

**Acknowledgement**

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**Table 1.** Material properties for different grades of intervertebral disc

<table>
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<tr>
<th></th>
<th>healthy</th>
<th>moderately degenerated</th>
<th>severely degenerated</th>
<th>Reference</th>
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<tr>
<td>nucleus pulposus</td>
<td></td>
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<td></td>
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<tr>
<td>$C_{10}$ [MPa]</td>
<td>0.12</td>
<td>0.17</td>
<td>0.19</td>
<td>(Schmidt et al. 2007, Rolhmann et al. 2006)</td>
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<tr>
<td>$C_{01}$ [MPa]</td>
<td>0.03</td>
<td>0.041</td>
<td>0.045</td>
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<tr>
<td>$D$ [MPa⁻¹]</td>
<td>0.0005</td>
<td>0.158</td>
<td>0.3</td>
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<tr>
<td>annulus fibrosus</td>
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<tr>
<td>$C_{10}$ [MPa]</td>
<td></td>
<td></td>
<td>0.1</td>
<td>(Moramarco et al., 2010)</td>
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<td>$C_{20}$ [MPa]</td>
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<tr>
<td>$D$ [MPa⁻¹]</td>
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<tr>
<td>$K_{f}$ [MPa]</td>
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<tr>
<td>$K_2$</td>
<td></td>
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**Table 2.** Donor information and failure load data for the 13 T12 vertebral bodies

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<th>Mean ± SD</th>
<th>Range</th>
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<tr>
<td>Age [year]</td>
<td>79.9 ± 7.8</td>
<td>65 – 90</td>
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<tr>
<td>Body weight [kg]</td>
<td>54.9 ± 15.8</td>
<td>41 – 94.7</td>
</tr>
<tr>
<td>$F_{IVD}^{FE}$ [kN]</td>
<td>1.84 ± 0.47</td>
<td>1.03 – 2.50</td>
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<td>$F_{PMM}$ [kN]</td>
<td>2.46 ± 0.62</td>
<td>1.39 – 3.40</td>
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<tr>
<td>$F^{exp}$ [kN]</td>
<td>2.09 ± 0.48</td>
<td>1.01 – 2.73</td>
</tr>
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**Figure 1.** Mechanical testing setup for a representative 3-vertebra segment with disconnected facet joints.

**Figure 2.** Generation of the finite element intervertebral disc (IVD) and comparison with the transverse sectional view of corresponding IVD, (a) surfaces extracted from its adjacent vertebrae, (b) IVD volume created from the two surfaces, (c) IVD meshes with annulus fibrosus (grey) and nucleus pulposus (blue), (d) transverse sectional view of the IVD (the boundary between the nucleus pulposus and annulus fibrosus was marked with blue ink).
Figure 3. (a) Two boundary conditions were simulated for each T12 model: either pure axial compression was prescribed to the nodes of the superior PMMA layer (FE-PMMA) or a 2-stage loading (step 1: 4° forward bending, step 2: axial compression) was conducted to the nodes of the superior IVD (FE-IVD). In both cases, the bottom nodes of the model were fully constrained. Each T12 model was discriminated between 4 regions: HR-pQCT based cortical (yellow) and cancellous bone (blue), annulus fibrosus (grey) and nucleus pulposus (red). (b) Material heterogeneity of the cancellous bone of a T12 model with bone volume fraction (BV/TV) and fabric anisotropy.
Figure 4. Linear regressions of the vertebral failure load as a function of the failure loads predicted by the FE-PMMA (a) and FE-IVD (b) models.