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Abstract

We propose a computationally efficient, bio-mechanically relevant soft-tissue simulation method for cranio-maxillofacial (CMF) surgery. Special emphasis is given to comply with the current clinical workflow. A template-based facial muscle prediction was introduced to avoid laborious segmentation from medical images. In addition, transversely isotropic mass-tensor model (MTM) was applied to realize the directional behavior of facial muscles in short computation time. Finally, sliding contact was incorporated to mimic realistic boundary condition in error-sensitive regions. Mechanical simulation result was compared with commercial finite element software. And retrospective validation study with post-operative scan of four CMF cases was performed.

Keywords: soft-tissue simulation, mass-tensor model, cranio-maxillofacial

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1. Introduction

Cranio-maxillofacial (CMF) surgery is a surgical procedure, which corrects facial bone deformity to improve functional and aesthetic outcome. Computer-assisted surgery (CAS) has been widely applied in this field, and successfully integrated into the clinical workflow. Three-dimensional imaging and rapid-prototyping technique help surgeons to plan the operation both on virtual and tangible models, whereas optical tracking technology enables the intra-operative guidance in the operating theater for various CMF applications (Hallermann et al., 2006; Chapuis et al., 2007). Along with the successful applications on rigid anatomical parts, there have been increasing demands on predicting soft-tissue changes after CMF surgeries. Some of them have been realized as commercial surgical simulation softwares.

There have been many studies on facial soft-tissue modeling from different fields of research. They can be classified into three categories depending on the computational method: mass-spring model (MSM), finite-element model (FEM), and mass-tensor model (MTM). First, MSM was initially accepted for real-time face animation due to its well-known physics and computational efficiency. Terzopoulos and Waters (1990) and Lee et al. (1995) proposed a fast simulation method using MSM with linear facial muscle model. Keeve et al. (1998) presented a MSM with prismatic element, and compared the result with FEM in terms of accuracy and computational cost. Teschner et al. (2000) proposed a multi-layer non-linear MSM with a static constraint to directly compute equilibrium state. Second, FEM has strong bio-mechanical
relevance at the cost of long calculation time. Koch et al. (1996) proposed a non-linear finite-element surface model with linear springs attached to the bone. Sarti et al. (1999) presented a computationally expensive voxel-based FEM running on a super computer. Zachow et al. (2000) suggested a fast tetrahedral volumetric FEM, which can be applicable to clinical practice. Later, Gladilin (2003) extended this to functional simulation with facial muscles. Chabanas et al. (2003) proposed a mesh morphing algorithm to minimize the laborious efforts on preparing finite-element mesh. Third, MTM was originally developed to find a golden mean between speed and accuracy. Cotin et al. (2000) proposed a hybrid method of using MTM for local deformations. Picinbono et al. (2003) extended this approach to non-linear, anisotropic elasticity. Mollemans et al. (2007) first applied MTM to CMF soft-tissue simulation, and the method was validated the results with 10 clinical cases both in quantitative and qualitative aspects. Roose et al. (2006) applied MTM to breast implant augmentation simulation with consideration on various boundary conditions.

Even though comprehensive amount of studies have been performed, most of the previous works have failed to be seamlessly integrated into the clinical workflow in two aspects. On the one hand, due to the natural higher perceptibility of subtle changes on the human face, the simulation accuracy provided by current solutions is not sufficient for CMF surgeons. For instance, existing solutions fail to realize delicate soft-tissue variations around nose and lips area commonly produced by underlying jaw movements. On the other hand, more sophisticated method, such as finite-element model, requires considerable pre-processing work and computation time. All these
factors have shown to hinder the usability and acceptance of available commercial and academic solutions into the clinical routine.

In this study, we propose a method for accurate yet computationally efficient simulation of soft tissue deformation after CMF surgery, while respecting the current clinical workflow. To achieve higher accuracy, we hypothesize that patient-specific muscle characterization is necessary. To avoid the daunting task of segmenting muscle tissue from medical images, we propose an efficient way to incorporate patient-specific facial muscles utilizing template model. We adopted transversely isotropic MTM for efficient calculation and incorporation of muscle fiber directions. From our recent promising result with single case (Kim et al., 2010), sliding contact around teeth and mucosa area was adopted for enhancing the anatomical reality on these error-prone regions. We also performed the sensitivity analysis on the simulation results by varying anatomical landmark definition in muscle morphing procedure. The proposed method is compared with FEM simulation in terms of computation time, and retrospectively validated with four post-operative CT scans for accuracy analysis.

2. Methods

The overview of our simulation pipeline is depicted in Figure 1. Firstly, image segmentation of bone tissues and outer skin layer is performed on conventional Computed Tomography (CT) of the patient without introducing any additional imaging modality such as Magnetic Resonance Imaging (MRI). Secondly, surface and volumetric meshes are generated from segmented masks. Bone segments are prepared by osteotomy planning software,
then corresponding boundary conditions can be defined. Thirdly, patient-specific muscles are reconstructed from the facial template model using an elastic deformation model. The directional property of muscles is then extracted and equivalent material properties are assigned. Finally, numerical simulation with mass-tensor model is performed. Detailed explanations of each procedure are presented in next subsections.

![Diagram of the anatomically considered facial soft-tissue simulation method](image)

Figure 1: The pipeline of the anatomically considered facial soft-tissue simulation method

### 2.1. Extra-cranial soft-tissue modeling

Amira software (Mercury Computer Systems, Germany) was used for segmenting extra-cranial soft-tissue from clinical CT scan. We assumed that only frontal extra-cranial soft-tissue was mainly engaged in deformation of most jaw movements, which enables us to minimize computation time without losing generality. Semi-automatic segmentation tools in Amira such as
lasso or magic wand were effectively used to accelerate segmentation procedures. Based on this segmentation result, surface mesh was generated using conventional marching cube algorithm (Lorensen and Cline, 1987), followed by automated tetrahedral volumetric mesh generation.

2.2. Patient-specific muscle modeling

Since it is almost impossible to identify individual muscles from clinical CT scan, we propose to construct patient-specific facial muscles by morphing muscles from facial template model. We found out one virtual atlas model, which was developed by Smith et al. (2007) for educational purposes, and freely available online. The morphing procedure was driven by landmark-based thin-plate-spline (TPS) deformation (Bookstein, 1989). We adopted 32 anatomical landmarks, which are commonly used for measuring skin depth in forensic science (Phillips and Smuts, 1996).

![Figure 2](image)

Figure 2: Morphing of template muscles to patient-specific anatomy (*left*), and extraction of morphed muscle direction using oriented-bounding boxes (*right*).

In order to obtain the direction of muscles, oriented-bounding boxes
(OBB) were extracted for linear-type muscles. As shown in Figure 2, the number of OBBs for individual muscle can be adjusted according to the curvature of the muscle. For example, masseter was represented by single OBB, while the other muscles were represented by double OBBs. The longitudinal direction of each bounding box was regarded as the direction of muscle for each segment.

2.3. Material property assignment

As far as we investigated, there was no consensus in the literature on mechanical properties of facial soft-tissue. Different material parameters were given by the previous works depending on characterization method and material model. We adopted Young’s modulus of muscle tissue along and across fiber direction from previous study (Duck, 1990). We also referred to the studies on estimating optimal facial tissue properties by comparing their simulation models with real post-operative data (Zachow et al., 2004; Mollemans et al., 2006). The parameters that we selected for our simulation are shown in Table 1. Since there was no previous study found on anisotropic Poisson ratio of muscle, we had to assume isotropic Poisson ratio.

<table>
<thead>
<tr>
<th></th>
<th>Young’s modulus (MPa)</th>
<th>Poisson Ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fat</td>
<td>0.003</td>
<td>0.46</td>
</tr>
<tr>
<td>Muscle across fiber</td>
<td>0.79</td>
<td>0.43</td>
</tr>
<tr>
<td>Muscle along fiber</td>
<td>0.5</td>
<td>0.43</td>
</tr>
</tbody>
</table>

Since it is difficult to remesh volumetric facial tissue according to the
intersection with muscle surfaces, we calculated equivalent material property by considering volumetric portion of muscle in each tetrahedron. We adopted the approach proposed by Uesu et al. (2005), which employs point sampling in tetrahedron. Then, geometrical test, based on directional comparison of surface normal and closest distance vector as shown in Figure 3, was performed to calculate equivalent material properties.

The equivalent material properties can be define by the volumetric portion of muscle ($p_{\text{muscle}}$) in each tetrahedron.

\[
E = E_{\text{fat}} \ast (1 - p_{\text{muscle}}) + E_{\text{muscle}} \ast p_{\text{muscle}}
\]

\[
\nu = \nu_{\text{fat}} \ast (1 - p_{\text{muscle}}) + \nu_{\text{muscle}} \ast p_{\text{muscle}}
\]

2.4. Mass-tensor modeling

MTM can be regarded as a trade-off solution between MSM and FEM. It has bio-mechanical relevance as FEM, while maintaining the computational
efficiency as MSM. We referred to MTM formulations of the works of Cotin et al. (2000), Picinbono et al. (2003) and Mollemans et al. (2007), where the reader can find further details.

In MTM formulation, the internal force on the j-th node of the volumetric mesh can be expressed as

\[ f_j = K_{jj}u_j + \sum_{\forall k \in \Psi_j} K_{jk}u_k \]  

(1)

where \( \Psi_j \) is the group of vertices connected to the j-th node, \( u_j \) is the displacement vector on j-th node. \( K_{jj} \) and \( K_{jk} \) are the stiffness tensors for vertex and edge respectively, which are only dependent on material properties and initial mesh configuration.

2.5. Boundary condition assignment

As shown in Figure 4, the volumetric nodes were classified into four types: fixed, joined, slide and free nodes. We defined fixed nodes along the most posterior plane of volumetric soft-tissue model, which can be assumed to be fixed during the simulation. Joined nodes were defined on the interface between relocated bone segments and soft-tissue. Additionally, we defined sliding nodes on the interface around the teeth and mucosa area.

On sliding nodes, only the tangential component to closest contacting triangle will affect the movement along the contacting surface. Neglecting frictional forces, the tangential force \( f^t_j \) can be calculated by

\[ f^t_j = f_j - (f_j \cdot n_p)n_p \]  

(2)

where \( f_j \) is the nodal force given by Eq.1, and \( n_p \) is the normal vector of nearest contacting triangle.
3. Results

The retrospective validation study was performed with four clinical cases. The first patient was suffered from a craniofacial deformation named Pfeiffer-Syndrom, which showed a mid-facial hypoplasia as leading clinical sign. The second patient was suffering from an Angle class III malocclusion with a maxillary retrognatism and a mandibular prognatism, and was treated with a bimaxillary procedure including genioplastia. The third patient also presented a class III malocclusion accompanied by a laterognatism to the right side. The fourth patient was treated because of a mandibular retrognatism, a long face syndrome and an open bite. These patients were chosen from the database, because they can represent nearly all possible variations of skeletal malocclusions. Details on the patients and the performed movements in the maxilla are presented in Table 2.

The actual displacement of bone segments during the operation has to be reproduced by matching the pre-operative and post-operative images. First,
Table 2: Surgical procedures performed on patient cases

<table>
<thead>
<tr>
<th>Dataset</th>
<th>Surgical Procedure</th>
<th>Maxillary Movement [mm, mm, mm, degree]</th>
</tr>
</thead>
<tbody>
<tr>
<td>P1</td>
<td>MxA</td>
<td>(0.53, -11.58, -3.78, 3.39)</td>
</tr>
<tr>
<td>P2</td>
<td>MSB+G</td>
<td>(-3.24, -0.61, 0.67, 0.00)</td>
</tr>
<tr>
<td>P3</td>
<td>MxA+G</td>
<td>(0.27, -4.98, -0.13, 1.31)</td>
</tr>
<tr>
<td>P4</td>
<td>MxA+MA+G</td>
<td>(1.07, -5.47, 0.74, 2.71)</td>
</tr>
</tbody>
</table>

MA: Mandibular Advancement  
MSB: Mandibular Setback  
MxA: Maxillary Advancement  
MxSB: Maxillary Setback  
G: Genioplasty

the post-operative data was aligned with pre-operative data by using volumetric image registration method on undeformed skull part, as shown in Figure 5(left). Next, the actual bone-related planning was reproduced by performing ICP-based registration between pre- and post-operative bone segments, as shown in Figure 5(right) (Besl and McKay, 1992). The reproduced relocation planning is depicted in Figure 6.

Especially in patient case P1, we used an in-house developed navigation system (Chapuis et al., 2007) to control the distraction vector for the midfacial advancement as shown in Figure 7. By means of computer-assisted planning, a two-step procedure was identified to be the ideal treatment for that patient. In step one, a Le-Fort III osteotomy with osteodistraction of the facial complex was planned as shown in Figure 6(P1). In step two, bimaxillary osteotomy with monobloc advancement was considered.
3.1. Comparison with finite-element simulation

As previously mentioned, MTM was developed to provide a golden mean between accuracy and computation time. We were interested in comparing the computational performance of our MTM implementation with commercial FEM simulation using ABAQUS/CAE 6.7 (Dassault Systems, RI, USA). In this study, we only used patient case 1 data with same elements and boundary conditions for both simulation methods. The differences between FEM and MTM simulation was measured as $0.023mm \pm 0.0061mm$. The overall computation of MTM was almost 18 times faster than FEM (MTM: 3.8 sec, FEM: 67 sec). The computational efficiency can be even higher by considering net computation time of MTM (1.3 sec), since stiffness tensor matrices of MTM can be pre-computed and applied to various surgical plans without recalculation. This computational superiority can be maintained when it is extended to transversely isotropic model. We emphasize that the goal of this

Figure 5: Reproduction of bone-related planning for retrospective validation study: registration of pre- and post-operative images (left), registration of pre-operative bone segments to post-operative yellow skull model (right).
Figure 6: Reproduced relocation planning of four clinical cases
experiment was mainly directed to compare the computational performance of these two approaches. In terms of accuracy, the post-operative CT scan was regarded as the ground truth comparison, presented in next section.

3.2. Validation with post-operative CT scan data

Post-operative CT scan of the patient was used to compare simulation results in different tissue models: homogeneous and transversely isotropic elasticity. In addition, we evaluated the simulation results in the presence of sliding contact. To assess the accuracy of the simulation results, the distance between each simulation and post-operative result was measured based on corresponding points. Instead of using only closest point matching for defining point correspondence, we adopted a combined approach using TPS
deformation and closest point matching to minimize the errors in largely de-
formed area. In the meantime, we used fourteen facial anatomical landmarks
on skin surface for TPS deformation as shown in Figure 8.

![Anatomical landmarks used for defining corresponding points between surfaces](image)

Figure 8: Anatomical landmarks used for defining corresponding points between surfaces

As shown in Figure 9 and Table 3, the mean error is decreased by incorpo-
rating transversely isotropy of muscles and sliding contact. These improve-
ments can also be seen qualitatively as color-coded distance errors as shown
in Figure 10, where negative value means that predicted skin surface lies be-
hind the post-operative skin surface. Statistical analysis using Wilcoxon test
\( (p < 0.05) \) showed that there was statistically significant difference between
the simulation results.

3.3. Sensitivity analysis of muscle morphing in simulation result

In order to measure the sensitivity of morphing muscles in simulation re-
sult, we performed three different trials defining skull anatomical landmarks
proposed by Phillips and Smuts (1996) as shown in Figure 11. The trans-
versely isotropic MTM simulations were then performed using three different
Figure 9: Boxplot of distance errors between simulations and post-operative result for 4 clinical cases (P1,P2,P3,P4); Each graph represents the results with homogeneous (H), muscle template (M), homogeneous + sliding contact (H+S), and muscle template + sliding contact (M+S).
Table 3: Statistical results for 4 patient data.

<table>
<thead>
<tr>
<th></th>
<th>Average Error</th>
<th>Standard Deviation</th>
<th>90th Percentile</th>
<th>95th Percentile</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>P1</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>H</td>
<td>2.50</td>
<td>1.21</td>
<td>4.10</td>
<td>4.40</td>
</tr>
<tr>
<td>M</td>
<td>2.21</td>
<td>1.23</td>
<td>3.39</td>
<td>4.16</td>
</tr>
<tr>
<td>H+S</td>
<td>2.07</td>
<td>1.24</td>
<td>3.68</td>
<td>4.39</td>
</tr>
<tr>
<td>M+S</td>
<td>1.21</td>
<td>0.92</td>
<td>2.15</td>
<td>2.90</td>
</tr>
<tr>
<td><strong>P2</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>H</td>
<td>3.25</td>
<td>1.27</td>
<td>5.13</td>
<td>5.85</td>
</tr>
<tr>
<td>M</td>
<td>2.68</td>
<td>1.07</td>
<td>4.00</td>
<td>4.65</td>
</tr>
<tr>
<td>H+S</td>
<td>2.11</td>
<td>1.06</td>
<td>3.42</td>
<td>4.06</td>
</tr>
<tr>
<td>M+S</td>
<td>2.14</td>
<td>0.98</td>
<td>3.42</td>
<td>4.04</td>
</tr>
<tr>
<td><strong>P3</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>H</td>
<td>2.03</td>
<td>2.41</td>
<td>3.01</td>
<td>3.38</td>
</tr>
<tr>
<td>M</td>
<td>1.80</td>
<td>2.36</td>
<td>2.61</td>
<td>2.87</td>
</tr>
<tr>
<td>H+S</td>
<td>1.75</td>
<td>0.71</td>
<td>2.61</td>
<td>2.78</td>
</tr>
<tr>
<td>M+S</td>
<td>1.58</td>
<td>1.90</td>
<td>2.58</td>
<td>2.84</td>
</tr>
<tr>
<td><strong>P4</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>H</td>
<td>3.23</td>
<td>0.83</td>
<td>4.25</td>
<td>4.48</td>
</tr>
<tr>
<td>M</td>
<td>3.10</td>
<td>0.99</td>
<td>4.27</td>
<td>4.51</td>
</tr>
<tr>
<td>H+S</td>
<td>2.43</td>
<td>0.84</td>
<td>3.46</td>
<td>3.67</td>
</tr>
<tr>
<td>M+S</td>
<td>2.56</td>
<td>0.74</td>
<td>3.39</td>
<td>3.62</td>
</tr>
</tbody>
</table>
morphed muscle models. The average deviation in morphed masseter muscles was 2.29\textit{mm} for template muscle I and 1.84\textit{mm} for template muscle II, while the average deviation in simulation results was 0.49\textit{mm} for template muscle I and 0.46\textit{mm} for template muscle II. This highlights the low sensitivity of simulations results in comparison with errors introduced during muscle template morphing procedure.

4. Discussion and Conclusion

In this study, we developed a fast and patient-specific soft-tissue simulation method for CMF surgery, with emphasis on its integration into the clinical workflow. A template-based facial muscle morphing technique was proposed to minimize the efforts of segmenting muscle structures without requiring additional imaging modality. In order to improve simulation accuracy, transversely isotropic MTM was applied to realize the directional property of muscle, which was obtained by extracting geometric features. Additionally, sliding contact around teeth and mucosa area was introduced to realize del-
Figure 11: Variability of definition in anatomical landmarks with three independent trials. Each color depicts three different trials.

icate soft-tissue variation in these error-sensitive regions. The method was validated with four clinical cases with post-operative CT scans. The results confirmed that improvements are achieved by considering template-based facial muscles and sliding contact.

As future work, the validity of morphing template models to patient-specific anatomy needs to be further investigated. It is known that significant amount of variability in muscle configurations between individuals is present (Pessa et al., 1998). This aspect should be investigated along with different types of CMF surgery, in order to plausibly determine the importance of such variability. Another limitation of the current study is the linear MTM model utilized, which is insufficient for larger deformations. Furthermore, due to the current lack of information regarding facial tissue characterization, isotropic Poisson ratio for muscle was assumed. Additionally more
strict control on post-operative scanning will be required to avoid undesirable
effects caused by physiological changes in-between pre- and post-operative
scans, as well as patient jaw position during scanning. In this sense, combin-
ing post-operative surface scanning and navigated operation could replace
the need for post-operative CT scanning for evaluation study.

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References

Analysis and Machine Intelligence, IEEE Transactions on 14, 239–256.

Bookstein, F., 1989. Principal warps: thin-plate splines and the decompo-
sition of deformations. Pattern Analysis and Machine Intelligence, IEEE
Transactions on 11, 567–585.

model of the face soft tissues for computer-assisted maxillofacial surgery.
Med Image Anal 7, 131–151.

Chapuis, J., Schramm, A., Pappas, I., Hallermann, W., Schwenzer-Zimmerer,


of the 23rd annual conference on Computer graphics and interactive techniques, 428.


gung der Deutschen Gesellschaft für Computer-und Roboter-assistierte Chirurgie eV, München.