Modelling Lake Kivu water level variations over the last seven decades

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**Abstract**

This study aimed at analysing the hydrological changes in the Lake Kivu Basin over the last seven decades with focus on the response of the lake water level to meteorological factors and hydropower dam construction. Historical precipitation and lake water levels were acquired from literature, local agencies and from global databases in order to compile a coherent dataset. The net lake inflow was modelled using a soil water balance model and the water levels were reconstructed using a parsimonious lake water balance model. The soil water balance shows that 370 mm yr\(^{-1}\) (25\%) of the precipitation in the catchment contributes to the runoff and baseflow whereas 1100 mm yr\(^{-1}\) (75\%) contributes to the evapotranspiration. A review of the lake water balance resulted in the following estimates of hydrological contributions: 55\%, 25\%, and 20\% of the overall inputs from precipitation, surface inflows, and subaquatic groundwater discharge, respectively. The overall losses were 58\% and 42\% for lake surface evaporation and outflow discharge, respectively. The hydrological model used indicated a remarkable sensitivity of the lake water levels to hydrometeorological variability up to 1977, when the outflow bed was artificially widened.

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**Introduction**

The variations of water level of natural (unregulated) lakes are an indicator of changes in the hydrological budget of the lake catchment. Such changes may be caused by climatic variations (precipitation, evapotranspiration and other meteorological components) or by changes in the runoff characteristics (such as land-use changes) in the catchment (Vuglinskii et al., 2009). Depending on the ratio of the catchment area per lake surface area, lake levels change within time scales ranging from hours to years (Mason et al., 1994). Also the sensitivity of lake water levels to rainfall evidently depends on the catchment-to-lake surface ratios (Vuglinskii et al., 2009). For example, a significant relationship has been observed between rainfall variability and lake water level in the Lake Victoria Basin (Mistry and Conway, 2003).

The seasonal rainfall distribution in the East-African region is bimodal due to the twice-annual passage of the Intertropical Convergence Zone (Verschuren et al., 2009). A recent study suggests that long-term variations in East-African rainfall are mainly driven by sea surface temperatures in the Indian Ocean (Tierney et al., 2013). East-African lakes experienced a rise in their water levels, the so-called “

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ungauged except for the lake level. In addition, records from most rain gauge stations in the catchment are discontinuous.

For Lake Kivu, in addition subaqueous groundwater discharge (SGD) that enters the lake below 100 m is of high relevance. The SGD drives a slow upwards advective transport within the lake that is the main source of nutrients for primary production in the lake surface layer (Pasche et al., 2012; Schmid and Wüest, 2012). An increase in precipitation may be expected to also lead to an increase of the SGD and thus an increase in the availability of nutrients for primary production.

The hydrological modelling of the lake water levels has already been identified as a relevant information because the lake serves as the principal reservoir for the downstream hydropower dam cascade. In addition, lake level variability has an impact on fisheries, especially the littoral zone ecological functions such as fish breeding and feeding. In the case of Lake Kivu, the littoral zone plays an important role as it is the permanent habitat for 27 of the only 29 fish species of this lake (Snoeks et al., 2012 and references therein). The littoral zone is the breeding and growing area of Limnothrissa miodon on which the fisheries resource is largely based (Isumbisho et al., 2004; Masiyila et al., 2011).

This study aimed to evaluate the lake level response to the hydrological variability in the catchment and to dam operation. The importance of Lake Kivu as a source of water resources, in the context of increasing demography and demand, is expected to increase in the forthcoming decades for further electricity production, irrigation as well as domestic and industrial uses. Thus, the assessment of the hydrological patterns and their effect on the water resource is crucial for monitoring and predicting the evolution of the water level of Lake Kivu and the discharge of the Ruzizi River (Vodacek et al., 2010). This analysis will contribute in providing the information needed to allow policy-making for an integrated water resource management in the lake catchment.

**Study site**

Lake Kivu is one of the equatorial East-African rift lakes (Fig. 1). The lake is situated at the feet of the volcanically active region of Nyiragongo between the Democratic Republic of the Congo and Rwanda. The lake surface is 2370 km² with a drainage basin of 4940 km² (excluding the lake, Ballatore, 2012). Most of the drainage basin consists of a river-active area (4255 km²) dominated by Hablic Acrisols (clay-rich but nutrient- and mineral-deficient acidic soils) in the Northwest and Southeast, by Humic Ferralsols (lateritic soils rich in iron, low clay soils; IUSS Working Group WRB, 2007) in the Southwest and by Humic Acrisols in the East. A river-free area (685 km²) is situated in the North of the lake and dominated by Mollic Andosols (Muvundja et al., 2009) which are black volcanic ash soils and consist of a mixture of volcanic ashes, stones and gases (Driessen et al., 2001). The SGD into the lake is most probably at least partially fed by infiltration in this river-free area. The land-use in the catchment is currently dominated by Dryland Cropland and Pasture (65%) whereas Evergreen Broadleaf Forest accounts for only 17%, Shrubland for 11% and other land-uses for 7% (Muvundja et al., 2009).

The climate is humid with a bimodal precipitation regime (~1400 mm yr⁻¹ over the lake catchment; Muvundja et al., 2009). The rainy season spans from September to May and the dry season from June to August (Bultot, 1971; Fehr, 1984; Bergonzini, 1998). The evaporation over the lake surface was estimated to ~1530 mm yr⁻¹ (CGIAR-CSI, http://www.cgiar-csi.org/data/global-aridity-and-pet-database). For comparison, Bultot (1971) estimated evaporation to ~1410 mm yr⁻¹, while estimates from other sources ranged from 800 to 1800 mm yr⁻¹ (TRACTIONEL and Rhein-Ruhr-Ingenieur (RRI), 1980). The potential evapotranspiration in the catchment estimated by different authors ranges from 900 to 1500 mm yr⁻¹ (Kilauni, 1976; Vangu, 1981; Bigororande, 1982; Kombi, 1982; CGIAR-CSI, http://www.cgiar-csi.org/data/global-aridity-and-pet-database).

An increase in evaporation and evapotranspiration is expected in East African climatic zone as a response to global warming (Verburg et al., 2003; Taylor et al., 2006). The surface runoff coefficient for this region is ~0.3 according to Shahin (2002) which contributes to feed the more than 100 rivers and streams that flow into the lake (Muvundja et al., 2009; Schmid and Wüest, 2012).

In previous studies, the water balance of Lake Kivu was estimated to be composed of inputs of 3.3 km³ yr⁻¹ by precipitation, 2.0 km³ yr⁻¹ by river inflows, 1.3 km³ yr⁻¹ by SGD and outputs of 3.6 km³ yr⁻¹ by lake surface evaporation and 3.0 km³ yr⁻¹ by the Ruzizi River outflow (Muvundja et al., 2009; Schmid and Wüest, 2012). The SGD are permanent underground water springs with most of the discharge attributed to cool and fresh SGD that mainly drive the upwelling in the lake, and a smaller contribution of hydrothermal sources that maintain the permanent stratification of the lake (Degens et al., 1973; Schmid et al., 2005; Ross, 2014; Ross et al., 2014).

Regarding the outlet, it is important to consider the construction and the operation of the Ruzizi I Hydropower Dam since 1959, located 3 km downstream of the lake (TRACTIONEL and RRI, 1980, FICHTNER, 2008). In 1977, dredging and widening operations were conducted, and a by-pass was erected at the lake outlet to regulate the amount of water in the river channel (FICHTNER, 2008). However the by-pass did not work properly and was decommissioned shortly afterwards. All these operations may have induced some bias to the “natural” lake level versus discharge relationship (Bergonzini, 1998; TRACTIONEL and RRI, 1980; FICHTNER, 2008) and sometimes to an unknown extent.

**Data**

Rain data from 34 meteorological stations (1928–1993; Fig. 1 and Table 1) were compiled from the literature (Bultot, 1954, 1971; INEAC, 1960; Kilauni, 1976; Bitacibera and Gatsimbanyi, 1978; Vangu, 1981; Bigororande, 1982; Bikoba, 1984) and local meteorological services (Météo-Rwanda as well as Division Provinciale de Météorologie and Division Provinciale d’Agriculture, Pêche et Élevage in D.R. Congo; Fig. 1). Arithmetic means were used in rainfall data compilation as the variation between the individual stations was comparably small (coefficient of variation: 17.8%).

Furthermore, two global precipitation databases were used for the analysis: the Global Precipitation Climatology Centre database (GPCC; Rudolf and Schneider, 2005; Rudolf et al., 2010; http://gpcp.dwd.de) and the satellite-based Tropical Rainfall Measuring Mission 3B43 product (TRMM; Jiang et al., 2011 and references therein: http://trmm.gsfc.nasa.gov/) which combines estimates generated by the TRMM and other satellite products as well as available rain gauge data from various sources available at: http://disc.sci.gsfc.nasa.gov/precipitation/documentation/TRMM_README/TRMM_3B43_readme.shtml.

The monthly GPPC data were averaged for the three grid cells covering most of the catchment area of the lake and compared to the average of the rain gauge measurements for the years 1941–1993 (Fig. 2). The correlation between the two time series is excellent (R² = 0.94; Fig. 3), with the GPPC data being on average ~7% higher. After 1993, both the rain gauge and the GPPC data cannot be considered reliable due to the absence of a sufficiently dense local in situ measurement network. For the water balance calculations, the GPPC data were used until 1997, while for the years 1998–2012 the average values of the TRMM 3B43 products for the grid cells shown in Fig. 1 were used. However, these TRMM...
Fig. 1. Map of Lake Kivu and its catchment. The numbers indicate the locations of the meteorological stations used in this study as listed in Table 1. The hatched area represents the river-free catchment area to the North of the lake. The large grey squares and the small black squares indicate the grid cells of the GPCC and TRMM data, respectively, that were used to calculate average precipitation in the catchment.

Fig. 2. Time series of annual precipitation for the basins of Lake Victoria (blue line; calculated back using lake surface precipitation data and relationship provided by Nicholson and Yin (2002)) and of Lake Kivu (different sources indicated by the other lines). For other data sources, see text. TRMM data are corrected by a factor of 1.2.

Fig. 3. Correlation between monthly rainfalls calculated from the rain gauge data (Table 1) and average rainfall in the GPCC dataset for the three grid cells marked in Fig. 1. The regression line is defined by the equation $P_{GPCC} = 1.01 \times P_{gauges} + 7$ mm month$^{-1}$, $R^2 = 0.94$. 

Table 1
Meteorological stations used in this study as located in Fig. 1.

<table>
<thead>
<tr>
<th>Station no.</th>
<th>Station name</th>
<th>Altitude (m asl)</th>
<th>Rainfall (mm yr⁻¹)</th>
<th># of years</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Tamira</td>
<td>2300</td>
<td>1196</td>
<td>9</td>
</tr>
<tr>
<td>2</td>
<td>Kora</td>
<td>2500</td>
<td>1272</td>
<td>11</td>
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<td>3</td>
<td>Goma</td>
<td>1493</td>
<td>1196</td>
<td>44</td>
</tr>
<tr>
<td>4</td>
<td>Kisinya-Airport</td>
<td>1554</td>
<td>1164</td>
<td>23</td>
</tr>
<tr>
<td>5</td>
<td>Prefecture</td>
<td>1540</td>
<td>1185</td>
<td>67</td>
</tr>
<tr>
<td>6</td>
<td>Pfunda</td>
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</tr>
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<td>7</td>
<td>Kanaama</td>
<td>1900</td>
<td>1477</td>
<td>8</td>
</tr>
<tr>
<td>8</td>
<td>Murunda</td>
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<td>1348</td>
<td>49</td>
</tr>
<tr>
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<td>Rutsiro</td>
<td>2300</td>
<td>1482</td>
<td>13</td>
</tr>
<tr>
<td>10</td>
<td>Crête Congo-Nil</td>
<td>2300</td>
<td>1231</td>
<td>3</td>
</tr>
<tr>
<td>11</td>
<td>Musumbi</td>
<td>1800</td>
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<tr>
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</tr>
<tr>
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<td>Nyamishaba</td>
<td>1470</td>
<td>1200</td>
<td>18</td>
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<tr>
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<td>Kalehe</td>
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<td>19</td>
</tr>
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<td>Mubuga</td>
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<tr>
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<td>Mugonero</td>
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<tr>
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<td>Shangi</td>
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</tr>
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<td>26</td>
<td>Kamatsira</td>
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<td>1729</td>
<td>12</td>
</tr>
<tr>
<td>27</td>
<td>Bamabi</td>
<td>1600</td>
<td>1621</td>
<td>29</td>
</tr>
<tr>
<td>28</td>
<td>Mwaga</td>
<td>1850</td>
<td>1877</td>
<td>11</td>
</tr>
<tr>
<td>29</td>
<td>Gisakura</td>
<td>1946</td>
<td>2191</td>
<td>16</td>
</tr>
<tr>
<td>30</td>
<td>Kamerbe-Airport</td>
<td>1591</td>
<td>1390</td>
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<tr>
<td>31</td>
<td>Cyangugu</td>
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<td>49</td>
</tr>
<tr>
<td>32</td>
<td>Shagasha</td>
<td>1700</td>
<td>1612</td>
<td>14</td>
</tr>
<tr>
<td>33</td>
<td>Bugatu</td>
<td>2025</td>
<td>1846</td>
<td>31</td>
</tr>
<tr>
<td>34</td>
<td>Bukavu</td>
<td>1635</td>
<td>1317</td>
<td>50</td>
</tr>
</tbody>
</table>

(PET) data have been characterized and tested for Africa and South America using different temperature-based methods applied to the WorldClim Global Climate data (available at http://worldclim.org; Zomer et al., 2008). The Hargreaves model (Hargreaves et al., 1985) yielded the best agreement and was applied (Zomer et al., 2008). The model was validated by these authors using PET measurements calculated from direct observations provided by the FAOCLIM 2 Climate station dataset (Allen et al., 1998) available on the FAO website. Many other studies have successfully used these global PET data (e.g., Trabucco et al., 2008; MacDonald et al., 2013; Metzger et al., 2013).

Historical records of lake water levels (1941–2011) and the outflow discharge calibration curves were collected from the Ruzizi I Hydropower Dam company in Bukavu-Mururu (Société Nationale d’Électricité, SNEL). Furthermore, lake levels determined by remote sensing measurements were retrieved from the global hydrological database HYDROWEB (Crétaux et al., 2011) and compared to ground measurements. Discharges of the Ruzizi outflow were calculated from the lake water level using the calibration curves provided by TRACTIONEL and RRI (1980) and by Bergonzini (1998) as summarized in Table 2.

Model description
Runoff model

The water balance of Lake Kivu and its catchment was calculated with a monthly time step Δt based on the meteorological data described above. Since only few actual discharge measurements from the tributaries of Lake Kivu were available (Bergonzini, 1998; Muvundja et al., 2009), we used a runoff model for estimating the monthly runoff from the catchment as an input to the lake water balance model.

Many authors have used hydrological models based on the Budyko framework (Budyko, 1958) in their studies for various purposes. For example, Zhang et al. (2008) applied the Budyko framework to develop and test a water balance model over variable time scales which allows predicting streamflow for ungauged catchments. Donohue et al. (2010) studied the importance of vegetation dynamics to improve Budyko’s model. Chen et al. (2013) used modified Budyko-type equations to estimate the seasonal evaporation and annual water storage in catchments. Van der Velde et al. (2013) used Budyko’s framework to identify regions with contrasting hydroclimatic change during the past 50 years in Sweden. In this study, we estimated the runoff of the Lake Kivu catchment by applying a monthly hydrological model based on the Budyko framework, the water partition and balance (WAPABA) model developed for diverse ungauged catchments by Wang et al. (2011).

The model comprises five steps summarized as below:

1. Rainfall, P(t) (mm month⁻¹), is partitioned into the catchment water yield, Y(t) (mm month⁻¹) and the catchment water consumption, X(t) (mm month⁻¹):

\[ Y(t) = P(t) - X(t) \]  

2. Y(t) comprises surface runoff, Q_s(t) (mm month⁻¹) and groundwater recharge, R(t) (mm month⁻¹) such as:

\[ Q_s = Y(t) - R(t) \]  

A supply–demand–consumption equation is applied to calculate X(t) from rainfall:

\[ X(t) = P(t) \left\{ 1 + \frac{X_0(t)}{P(t)} - \left[\left(\frac{X_0(t)}{P(t)}\right)^{aq_1}\right]^{1/a_1} \right\} \]
Here, $\alpha_1$ is the catchment consumption curve coefficient; $X_0(t)$ (mm month$^{-1}$) is the potential catchment water consumption or water demand limit given by:

$$X_0(t) = ET_0(t) + \frac{S_{\text{max}} - S_{t-1}}{\Delta t}$$  \hspace{1cm} (4)

where $ET_0(t)$ (mm month$^{-1}$) is the catchment potential evapotranspiration; $S_{\text{max}}$ (mm) is the maximum water holding capacity of the soil in the catchment; $S_{t-1}$ is the amount of water held in the soil for the prior time step $t-1$; and $\Delta t = 1$ month is the simulation time step.

2. The amount of water available for evapotranspiration, $W(t)$ (mm month$^{-1}$), is then given by:

$$W(t) = \frac{S(t-1)}{\Delta t} + X(t)$$  \hspace{1cm} (5)

The actual evapotranspiration is calculated from:

$$ET = W(t) \left\{ 1 + \frac{(ET_0(t) + (S_{\text{max}}/\Delta t))}{W(t)} \right\} - \left\{ 1 + \left( \frac{(ET_0(t) + (S_{\text{max}}/\Delta t))}{W(t)} \right)^{a_2} \right\}^{1/a_2}$$  \hspace{1cm} (6)

where $a_2$ is the catchment evapotranspiration curve coefficient.

The soil water storage at the end of the time $t$, $S(t)$ is:

$$S(t) = S(t-1) + [W(t) - ET(t)] \Delta t$$  \hspace{1cm} (7)

3. The catchment water yield at time step $t$, $Y(t)$ is partitioned into $R(t)$ (mm month$^{-1}$) and $Q_b(t)$ (mm month$^{-1}$) by:

$$R(t) = \beta Y(t)$$  \hspace{1cm} (8)

where $\beta$ is the proportion of the water yield and the groundwater recharge rate, $R(t)$.

The rest of $Y(t)$ contributes to the surface runoff, $Q_s(t)$ given by:

$$Q_s = Y(t) \times (1 - \beta)$$  \hspace{1cm} (9)

4. The groundwater storage is drained to generate a baseflow $Q_b(t)$ (mm month$^{-1}$) given by:

$$Q_b(t) = \frac{G(t)}{k}$$  \hspace{1cm} (10)

where $G(t)$ (mm) is the groundwater storage and $k$ (months) the groundwater residence time. The baseflow here indicates the amount of infiltrated groundwater which returns to the surface.

Given the steepness of the basin topography, the residence time of the groundwater should be comparably short. However, we have no concrete observational evidence for the residence time. We therefore chose to estimate this parameter during the model calibration (see 'Model parameterization and calibration' section). Thus the remaining water in the groundwater storage at the end of time $t$ is:

$$G(t) = G(t-1) + \Delta t \left( R(t) - Q_b(t) \right)$$  \hspace{1cm} (11)

5. The sum of surface runoff and the baseflow results in the total flow, $Q(t)$, during the time step $\Delta t$ and closes the hydrological cycle by:

$$Q(t) = Q_s(t) + Q_b(t)$$  \hspace{1cm} (12)

The catchment runoff coefficient, $k_r$ is calculated by:

$$k_r = \frac{Q(t)}{P(t)}$$  \hspace{1cm} (13)

Finally, the inflow into the lake, $Q_l(t)$ (m$^3$ s$^{-1}$), is calculated from $Q(t)$ by:

$$Q_l(t) = c \times Q(t) \times A_r$$  \hspace{1cm} (14)

Here $A_r$ (m$^2$) is the river-active area of the catchment, and $c$ is a conversion factor to convert from mm month$^{-1}$ to m$^3$ s$^{-1}$. The procedures for estimating or calibrating the five model parameters $\alpha_1$, $a_2$, $\beta$, $k$, and $S$ are described in 'Model parameterization and calibration' section below and the values of the parameters are given in Table 2.

### Lake water balance model

A parsimonious water balance model was used to reconstruct the lake level dynamics from the knowledge on lake hydrological and morphological parameters (Table 2). The calculations of the hydrological inputs to the model were made from January 1941 to December 2011.

The model used is based on the following equation:

$$\Delta Q(t) = A_L \times [P(t) - E(t)] + Q_l(t) + Q_{\text{SGD}}(t) - Q_{\text{out}}(t)$$  \hspace{1cm} (15)

where $\Delta Q$ (m$^3$ s$^{-1}$) is the net water inflow to the lake; $A_L$ is the lake surface area (m$^2$), $P(t)$ is the rainfall (m s$^{-1}$) on the lake surface at time $t$ (s), and $E(t)$ is the evaporation rate (m s$^{-1}$) from the lake surface.

$Q_l(t)$ (m$^3$ s$^{-1}$) is the total catchment flow to the lake (except SGD) calculated from the sum of catchment runoff and baseflow as given by Eqs. (12) and (14).
The long-term mean total discharge of the SGD, \(Q_{\text{SGD}}(t)\), is relatively well constrained by the salt balance of the lake (Schmid and Wüest 2012), but nothing is known about the residence time of the water before entering the lake or the temporal dynamics of the SGD. We therefore used two different approaches for estimating \(Q_{\text{SGD}}\), either as constant:

\[
Q_{\text{SGD}}(t) = Q_{\text{SGD}} = 41.2 \, \text{m}^3\text{s}^{-1} (= 1.3 \, \text{km}^3\text{yr}^{-1})
\]

or as variable in time, and thus, as a function of the precipitation during the previous year:

\[
Q_{\text{SGD}}(t) = \overline{Q_{\text{SGD}}} \times \gamma \left[ 1 + \frac{P_n - \bar{P}}{\bar{P}} \right]
\]

where \(P_n\) is the mean precipitation during the past year, and, \(\bar{P}\) is the average long-term precipitation; \(\gamma\) is a non-dimensional fit parameter describing the extent to which the SGD discharge varies with precipitation.

\[Q_{\text{out}}(t) = \text{discharge of the outflow given by:}
\]

\[
Q_{\text{out}}(t) = aH(t) + b
\]

where \(H(t)\) is the lake water level gauged at the outflow (m, above 1460 m asl); \(a\) (m² s⁻¹) and \(b\) (m³ s⁻¹) are the slope and the intercept of the rating curve, respectively (Table 2). Two different rating curves were used for the periods before and after the year 1977 when the outflow was modified by dredging and widening.

The lake water level was then calculated from the net water inflow by:

\[H_i = H_{i-1} + \frac{\Delta Q_{\text{in}} - \Delta Q_{\text{out}}}{A_i} \Delta t\]

Where \(H_i\) is the simulated water level for the month \(i; H_{i-1}\) is the simulated water level for the previous month \(i-1\); \((\Delta Q_{\text{in}} - \Delta Q_{\text{out}})\) the net inflow of the previous month calculated using Eq. (14); \(\Delta t\) the time elapsed from the first day of the previous month to the first day of the month under consideration.

Model parameterization and calibration

The model parameters were defined or calibrated as follows: For the soil water holding capacity, \(S_{\text{max}}\), a value of 300 mm was used, which is the value given for the region by Bultot (1971) and agrees with average values around Lake Kivu in the FAO Soil Map of the World. Of the two parameters \(\alpha_1\) and \(\alpha_2\) only one could be used for model calibration, as their effects on the total runoff from the catchment are qualitatively very similar. Therefore parameter \(\alpha_2\) was arbitrarily set to 2.0, a typical value observed in 331 test catchments by Wang et al. (2011). Then, \(\alpha_1\) was optimized to set the mean difference between observed and calculated lake levels for the entire time series to zero. This resulted in \(\alpha_1 = 2.2\).

Finally, the parameters \(\beta\) and \(k\) were calibrated to reduce the difference between the observed and simulated seasonality of the lake level. Here, seasonality is defined as the difference between the monthly lake levels and their 12-months running mean, averaged for the period 1942–1997, i.e. not including the years for which the TRMM data were used. The best fit between observed and simulated seasonality was achieved with \(\beta = 0.6\) and \(k = 5\) months, meaning that 60% of the water yield is contributed by the baseflow, which resides on average 5 months in the catchment (the value of 5 months was chosen to optimize the model but we have no concrete observational evidence).

Model evaluation

The predictive power of the model was assessed using the Nash-Sutcliffe efficiency (NSE) index (Nash and Sutcliffe, 1970) as well as the ratio of the root mean square error and the standard deviation of the observations (RSR) as described by Moriasi et al. (2007 and references therein).

Observations and results

Precipitation

The precipitation record for Lake Kivu shows a shift towards wetter conditions around 1961. Similar observations were made for the Lake Victoria Basin (Nicholson and Yin, 2002; Kizza et al., 2009; Fig. 2) indicating that rainfall in the catchment of Lake Kivu is driven by the same regional meteorological patterns as for Lake Victoria. In order to support this, we give in the following the respective values for Lake Kivu (in italics) and Lake Victoria (in parentheses, data are from Nicholson and Yin, 2002). The annual mean precipitation (± standard deviation) in the rain gauge data for the period 1941–1960 was 1417 ± 118 mm yr⁻¹ for the Lake Kivu Basin (1244 ± 129 mm yr⁻¹). The minimum precipitation of 1090 mm yr⁻¹ (1070 mm yr⁻¹) was observed in 1952 (1943), the maximum of 1500 mm yr⁻¹ (1640 mm yr⁻¹) occurred in 1951 (Fig. 2). Subsequently, the mean rainfall rose to 1415 ± 118 mm yr⁻¹ (1367 ± 167 mm yr⁻¹), in the period 1961–1993, corresponding to an increase by 8% (10%) compared to the average before 1961. The minimum values for this period were 1140 mm yr⁻¹ (1110 mm yr⁻¹) in 1993 (1984), whereas the maxima were 1590 mm yr⁻¹ in 1963 and 1680 mm yr⁻¹ in 1988 (1870 mm yr⁻¹ in 1961 and 1640 mm yr⁻¹ in 1963).

Based on the classification of Fehr (1984), the long-term series indicate that June to August are dry months with 46, 29 and 57 mm month⁻¹ respectively whereas the months from September to May are wet with precipitation ranging between 121 and 199 mm month⁻¹ (Fig. 4). Among the wet months, September and January are the least wet with 121 and 128 mm month⁻¹, respectively, while November and April are the wettest with 171 and 199 mm month⁻¹, respectively, according to a bimodal rainfall regime (Fig. 4).

Runoff

The runoff model indicated an annual mean land potential evapotranspiration rate of 1100 mm yr⁻¹ and mean baseflow of 220 mm yr⁻¹ (Table 3; Fig. 4). The surface runoff was 150 mm yr⁻¹ (Table 3; Fig. 4). Except for the baseflow, all soil water balance components showed lower values in the dry season (Fig. 4). The average runoff coefficient for the entire basin was estimated at \(k_b = 0.25\) (Table 3). The runoff was estimated to have increased by 19% in the period 1961–1993 compared to 1941–1960.
Lake water levels

A comparison of lake levels observed in situ and with remote sensing confirmed that both time series are accurate within a few cm (Fig. 5). Remotely sensed lake levels for neighbouring Lakes Edward and Victoria show very similar temporal dynamics as for Lake Kivu, indicating that the lake level fluctuations are driven mainly by regional meteorological variations. This is also supported by a comparison of historical trends of lake levels and rainfall in the drainage area (Fig. 6). Periods of high annual precipitation matched with high lake water levels and vice versa both before and after the dam construction of 1959 (Fig. 6). Both curves indicate higher water levels for the period after 1960 with a maximum peak in 1963. The average lake levels increased from 1462.40 m asl for 1941–1960 to 1462.86 m for 1961–1993, and fell back to 1462.41 m in the years 1994–2011, albeit with a twice as large interannual variability than before.

![Fig. 5. Comparison of satellite (Crétaux et al. 2011) water level variation (relative to an arbitrary average level) of selected East-African great lakes with the levels observed in situ for Lake Kivu. “Kivu” indicates the satellite-based data and “Kivu ground” the in situ gauged data.](image1)

![Fig. 6. Annual mean Lake Kivu water level (grey line with circles; data from SNEL) and precipitation (black bold line; data from GPCC until 1997 and TRMM multiplied with a factor 1.2 afterwards). The lake water levels are relative to a height of 1460 m asl. Note that the lower number of precipitation data (Fig. 7) affected the quality of the agreement after 1993.](image2)

Lake water balance

Observed and simulated lake levels are compared in Fig. 7. The mean absolute difference between observed and simulated monthly lake levels in the model with constant SGD inflow was 0.17 m. Adding a variable SGD inflow depending on the precipitation of the previous years (Eq. (17)), improved the agreement of extreme (maximum and minimum) lake levels between observations and simulations, but did not remarkably decrease the mean absolute differences or strongly modify the their relationship. We therefore do not see sufficient justification in the observed data to support or reject the hypothesis of a variable SGD inflow depending on precipitation. For the study analysis we used the results of the model with constant SGD inflow, but none of the conclusions would have been different using the model with variable SGD inflow.

The model evaluation suggested that its performance was satisfactory (NSE = 0.60 and RSR = 0.64) for 1941–1958 and good (NSE = 0.72 and RSR = 0.53) for 1959–1976. However for the period after 1977, the predictive power of the model was lower (NSE = 0.34 and RSR = 0.81) most likely due to turbine operating problems (TRACTIONEL and RRI, 1980; Fichtner, 2008) which induced large uncertainties in the lake discharge.

The correlation between mean annual observed and simulated water levels was good before the outlet of the river was modified in 1977, for both periods before and after the dam construction (Fig. 8). The same was true for the correlations between observed and simulated lake level increase during the rainy season from October to May (Fig. 9). Correlations for the lake level decrease during the dry season were weaker, and the slope was only 0.42 before dam construction and 0.34 thereafter (Fig. 10). After the modification of the outlet, the predictive capability of the model for all three quantities (mean annual level, increase during the wet and decrease during the dry season) became consistently weaker, both for the period 1977–1991 when still sufficient precipitation data was available, and for the period after 1992 for which almost no rain gauge data was available (Figs. 9 and 10).

The observed and simulated lake levels show a consistent seasonality. Maximum lake levels are reached in May (0.16 m above annual average) and minimum lake levels in September (0.10 m below annual average; Fig. 11). Interestingly, the reproduction of the mean seasonal lake water level was equally good (with residuals generally lower than 0.02 m) for all periods, independent of dam construction or modification of the river outlet (Fig. 11). It is only somewhat worse for the period where TRMM data was used for driving the model, which might indicate a seasonal bias in the TRMM data.
The mean annual flows of the calculated lake water balance are summarized in Table 4 and their seasonal variability is shown in Fig. 12. Table 4 highlights the importance of direct precipitation on the lake surface and evaporation (3.5 and 3.6 km³ yr⁻¹, respectively), which contribute more than half to the total inputs and outputs. The estimated surface inflows (1.6 km³ yr⁻¹) are lower than the previous estimates of 2.4 km³ yr⁻¹ (Muvundja et al., 2009) and of 1.6 to 2.4 km³ yr⁻¹ (Schmid and Wüst, 2012), but similar to the 1.8 km³ yr⁻¹ proposed by Rinta (2009) from the application of the Soil and Water Assessment Tool (SWAT) model. However, the SWAT estimates for evaporation (2.2 km³ yr⁻¹) and precipitation (2.8 km³ yr⁻¹) were lower than the estimates found in the literature (Bultot, 1971; Bergonzini, 1998; Muvundja et al., 2009) probably due to large uncertainties in the data sources and comparably low precipitation during the study period (1998–2008) of the SWAT model. Precipitation and its seasonal variability are the same as for the runoff model (Fig. 4), while the river inflows correspond to the sum of the surface runoff and the baseflow.

The SGD inflows were estimated in previous studies to close the salt balance of the lake (Schmid et al., 2005). They are assumed to be constant in the model, and their small apparent temporal variability in Fig. 12 is due to the different number of days per month. The seasonal variation of the water balance is mainly due to the variation in precipitation and the resulting seasonality. The total output is almost constant throughout the year, as the seasonal variation of the outflow that results from water level variations is almost exactly compensated by the seasonal variation of evaporation from the lake surface.

**Discussion**

The hydro-meteorological features of the Lake Kivu Basin are in accordance with the regional climate (Fig. 4) where the altitude-moderated equatorial climate is bimodal with rainy months (September to May) interrupted by dry months (June to August) because of the twice-annual passage of the Intertropical

<table>
<thead>
<tr>
<th>Table 4</th>
<th>Lake Kivu water balance as calculated with the model for the years 1941–1991.</th>
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</thead>
<tbody>
<tr>
<td>Lake water balance</td>
<td>m³ s⁻¹</td>
</tr>
<tr>
<td>Precipitation</td>
<td>111</td>
</tr>
<tr>
<td>Inflows</td>
<td>50</td>
</tr>
<tr>
<td>Subaquatic springs</td>
<td>41</td>
</tr>
<tr>
<td>Evaporation</td>
<td>115</td>
</tr>
<tr>
<td>Discharge</td>
<td>86</td>
</tr>
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*related to the lake surface area.
Convergence Zone (Verschuren et al., 2009). Less seasonal variation is noticed in evaporation and potential evapotranspiration (Figs. 4 and 10) due mostly to low variation in air temperatures near the equator. Evaporation rates of East-African lakes are similar to the precipitation they receive: 1537 mm yr$^{-1}$ for Lake Victoria (Nicholson and Yin, 2002, 2004), and 1695 mm yr$^{-1}$ for Lake Tanganyika (Bultot, 1962, 1971).

This study shows a strong similarity of the dynamics of precipitation and lake levels between the basins of Lakes Kivu and Victoria (Fig. 3). Results in Fig. 12 indicate that the Lake Kivu level takes about two months lag to react from precipitation inputs and one month from catchment runoff. The Lake Victoria Basin experienced drought conditions in the 1930s, 1950s, 1970s and 1980s (Nicholson and Yin, 2002; Mbungu et al., 2012). Corresponding low precipitation (Mbungu et al., 2012) was observed in the Lake Kivu Basin (Fig. 2) and led to lake water level low stands (Fig. 6). However, the two basins underwent remarkable increasing and decreasing hydrological trends since the 1960s and the 1990s, respectively (Fig. 6), as also reported by Mbungu et al. (2012). The increase in rainfall for the period from 1961 (which was an extreme rainfall year for Lake Victoria; Conway, 2002 and references therein) until 1993 compared to 1941–1960 is very similar in both basins (Fig. 2). These observations are in agreement with those of Hulme et al. (2001) who estimated that there was a wetting trend over the East-African region, as a part of a more coherent zone of wetting across most of the equatorial Africa where some areas experienced increasing rainfall trends of up to 10% or more per century. Meanwhile, an increasing trend in natural hazards mostly due to hydro-meteorological events from the 1960s has recently been reported by Vandecasteele et al. (2010) for the African Great Lakes region (Kivu, Rwanda and Burundi). IPCC (2007) also forecasts a rainfall increase of ~10 to ~20% for East Africa for the next century, which has been confirmed by a more recent simulation project (Bony et al., 2013).

The low lake levels of East-African lakes during the period of 2005/2006 which were felt as an emergency case by the hydropower companies on Ruzizi River (SNEL and SINELAC, 2006), were related to the El-Niño Southern Oscillation cycle and a forcing by the 2006 Indian Ocean dipole (Becker et al., 2010). The response of Lake Kivu to these events was similar to those of Lakes Victoria and Edward (Fig. 5). Bergonzini et al. (2002) discussed the interannual variation of the water balance of Lake Tanganyika and found that its current status is related to precipitation variability. However he argued that the change in runoff conditions due to human activities might also have led to a change in the runoff coefficient relatively to the period before 1960.

The similarity of the agreement before and after dam construction indicates that the dam had no significant influence on the lake level (Figs. 7–10). The correlations for the rainy season are better than those for the dry season indicating that our predictions for runoff (which characterize the rainy season) are better than those for evaporation. This is probably caused by the lack of information on the interannual variation of lake surface evaporation as well as the overall uncertainties of this parameter on the basin scale.

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**Fig. 9.** Comparison of simulated and observed lake level differences between 1 October and 1 May next year (Wet Season).
Another major source of uncertainty in the lake level model might be the quality of the outflow rating curves.

After 1977, when the hydropower bypass was set up at the Ruzizi outlet together with the Ruzizi channel dredging and widening, the lake level regime seems to have been disturbed considerably as the model is much less successful in predicting the lake levels. TRACTIONEL and RRI (1980) reported that the dam has occasionally operated inadequately during this period causing a slowing down of the river flow. In contrast, the average seasonal variation of the lake level was still perfectly reproduced by the model. The average absolute residuals between the calculated and the observed seasonality were 0.01 m for all periods studied until 1998 (Fig. 11) and only increased to 0.03 m for the period where the TRMM data were used. This confirms that the modification on the Ruzizi outlet did not modify the seasonality of the outflow, but induced some interannual variability in the outlet rating curve. Possible causes might be that the outlet was further modified by changes in flow conditions after the construction work made in 1977, that the modification of the outlet allowed the dam operations to take some influence on the mean annual water level, e.g. in cases of malfunction of the turbines as reported above, or that the outflow of the lake was to some extent managed.

Despite of the uncertainties in the raw data and the model setup, the water balance devised in this study matches well with the ranges provided by previous studies (Schmid and Wüest, 2012). The long-term average precipitation estimate used in this study (1470 mm yr$^{-1}$) is very close to the estimate of 1497 mm yr$^{-1}$ used by Bergonzini (1998), while he used 8% lower lake surface evaporation (1412 mm yr$^{-1}$ from Bultot, 1971). However, previous evaporation estimates range from 1060 mm yr$^{-1}$ (Verbeke, 1957) to 1690 mm yr$^{-1}$ (UNESCO, 1978).

The model estimated average baseflow and surface runoff to 220 mm yr$^{-1}$ and 150 mm yr$^{-1}$, respectively. Together they yield 370 mm yr$^{-1}$, which corresponds to a runoff coefficient of 0.25. Similar values have been predicted in several studies for this region (Shahin, 2002). The baseflow is estimated to be more important than surface runoff, which may be due to the volcanic soils which retain much water (Driessen et al., 2001; IUSS, 2007). The subaquatic groundwater discharge (SGD) is an important component of the lake water balance (Schmid et al. 2005; Schmid and Wüest, 2012). The inflow by SGD is assumed to be at least partially derived from infiltration in the volcanic soils on the river-free area of 685 km$^2$ in the North of the lake. However, the estimated SGD of 1.3 km$^3$ yr$^{-1}$ would correspond to 1900 mm yr$^{-1}$ relative to this sub-catchment area, which is higher than the precipitation received. Further investigations are therefore required to determine the origin of these water masses as well as their residence time. Recent findings revealed that groundwater resources in East Africa are dependent on extreme rainfall rather than average rains (Taylor et al., 2013).

Previous lake discharge estimates of 3.2 km$^3$ yr$^{-1}$ (Degens et al., 1973) and 3.6 km$^3$ yr$^{-1}$ (Muvundja et al., 2009) were rather
applicable to a certain period of the time series or overestimates. However our estimate of 2.7 km$^3$ yr$^{-1}$ is close to the value of 2.8 km$^3$ yr$^{-1}$ suggested by Bergonzini (1998) despite of the difference in the method he used to establish the outflow data for the period of 1951–1973. Although Bergonzini (1998) accorded low confidence to the lake level records up to 1950, our compilation showed only a slight difference of +5% between the lake discharge (1.9 km$^3$ yr$^{-1}$) for the period of 1941–1950 and that of 1951–1959 (2.0 km$^3$ yr$^{-1}$). In addition, Bulot (1962) estimated the lake discharge to be 2.1 km$^3$ yr$^{-1}$ for the period of 1951–1973, which is similar to our estimations. From the early 1960s, the lake level (Fig. 8) as well as the discharge significantly increased with the latter rising to 2.9 km$^3$ yr$^{-1}$ for the period 1961–1993 due to an increase in rainfall. Recently, the mean lake level has fallen back to the level before 1961, but with a twice as high interannual variability than before (Fig. 7).

Precipitation and net inflow (runoff + SGD) represent 55% and 45% of the overall inputs (Table 4) in agreement with estimations (54 vs. 46%) of Bergonzini (1998). Evaporation and outflow represented 57 and 43% (Table 4) of the total water losses, respectively, indicating a high lake level sensitivity to hydro-meteorological changes (Russell and Johnson 2006). By reducing the precipitation values in the model input, we can roughly estimate at which average of long-term precipitation the lake would get closed, assuming that evaporation from the lake surface as well as the SGD remain unchanged. This would be the case if precipitation in the basin were reduced to ~60% of its current value or ~900 mm/yr.

The results of the present study and the discussion of the uncertainties involved highlight the necessity to better monitor the hydrology of Lake Kivu and its basin. Continuous time series of quality-assured data of precipitation and other meteorological observations on the lake and in the catchment, as well as of the discharge of selected tributaries to the lake would help to better constrain the water balance of the lake. This will be necessary in order to be able to observe and quantify potential effects of climate change on the water level and the hydrological balance of the lake in the future.

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