Observation of tau neutrino appearance in the CNGS beam with the OPERA experiment

OPERA Collaboration

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The OPERA experiment is searching for $\nu_{\mu} \rightarrow \nu_{\tau}$ oscillations in appearance mode, i.e., via the direct detection of $\tau$ leptons produced in $\nu_{\tau}$ charged-current interactions. The evidence of $\nu_{\mu} \rightarrow \nu_{\tau}$ appearance has been previously reported with three $\nu_{\tau}$ candidate events using a sub-sample of data from the 2008–2012 runs. We report here a fourth $\nu_{\tau}$ candidate event, with the $\tau$ decaying into a hadron, found after adding the 2012 run events without any muon in the final state to the data sample. Given the number of analyzed events and the low background, $\nu_{\mu} \rightarrow \nu_{\tau}$ oscillations are established with a significance of 4.2$\sigma$.

Subject Index  C04, C32

1. Introduction  Neutrino oscillations have been studied by many experiments in disappearance mode [1]. In 2010 the OPERA experiment, searching for $\nu_{\mu} \rightarrow \nu_{\tau}$ oscillations in appearance mode by detecting $\tau$ leptons produced in $\nu_{\tau}$ charged-current interactions, observed a first $\nu_{\tau}$ candidate [2]. Recently the Super-Kamiokande experiment reported the evidence of a $\nu_{\tau}$ appearance signal in atmospheric neutrino data [3], with a signal-to-noise ratio of about one-tenth. In parallel, OPERA and T2K, both operating with accelerator-based neutrino beams, have shown the first proof of flavor transitions in appearance mode with a high signal-to-noise ratio [4]. While the T2K experiment has observed $\nu_{\mu} \rightarrow \nu_{e}$ oscillations [5], the OPERA experiment, operating in low background conditions and with a signal-to-noise ratio of about ten, has reported the 3$\sigma$ evidence of $\nu_{\mu} \rightarrow \nu_{\tau}$ appearance [6].
Table 1. Number of events used in this analysis.

<table>
<thead>
<tr>
<th></th>
<th>2008</th>
<th>2009</th>
<th>2010</th>
<th>2011</th>
<th>2012</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>pot ($10^{19}$)</td>
<td>1.74</td>
<td>3.53</td>
<td>4.09</td>
<td>4.75</td>
<td>3.86</td>
<td>17.97</td>
</tr>
<tr>
<td>$0\mu$ events</td>
<td>148</td>
<td>250</td>
<td>209</td>
<td>223</td>
<td>149</td>
<td>979</td>
</tr>
<tr>
<td>$1\mu$ events ($p_\mu &lt; 15$ GeV/c)</td>
<td>534</td>
<td>1019</td>
<td>814</td>
<td>749</td>
<td>590</td>
<td>3706</td>
</tr>
<tr>
<td>Total events</td>
<td>682</td>
<td>1269</td>
<td>1023</td>
<td>972</td>
<td>739</td>
<td>4685</td>
</tr>
</tbody>
</table>

using a subsample of the data collected in the 2008–2012 runs. In this paper, we describe an additional $\nu_\tau$ candidate event, with the $\tau$ decaying into a hadron, found in the analysis of an extended data set, including also the events of the 2012 run without any muon in the final state. We finally report the achieved significance in the observation of $\nu_\mu \rightarrow \nu_\tau$ oscillations.

2. The OPERA detector and the data sample

In order to meet the experimental requirements of a large target mass and a micrometric spatial accuracy to detect short-lived $\tau$ lepton decays, a target made of lead plates interspaced with emulsion films acting as tracking devices is used. The OPERA detector [7] is composed of two identical parts called super modules, each consisting of a target section followed by a spectrometer. The target has an average mass of about 1.2 kt and a modular structure with an average number of 141 431 target units, called bricks. A brick consists of 57 emulsion films [8], interleaved with 1 mm thick lead plates. Bricks are arranged in walls alternated with scintillator strip planes (target tracker or TT). Magnetic spectrometers, consisting of iron core magnets instrumented with resistive plate chambers (RPC) and drift tubes (high-precision tracker or PT), are used for the measurement of the muon charge [9] and momentum. In order to reduce the emulsion scanning load, removable pairs of emulsion films called changeable sheets [10] are used as interface trackers between the TT and the bricks.

The OPERA detector was exposed to the CERN Neutrinos to Gran Sasso (CNGS) beam [11,12] from 2008 to 2012. A sample of 19 505 contained neutrino interactions corresponding to $17.97 \times 10^{19}$ protons on target (pot) has been registered by the detector. A 3D track is tagged as a muon if the product of its length and the density along its path is larger than 660 g/cm$^2$ [13]. An event is classified as $1\mu$ if either it contains at least one track tagged as a muon or the total number of fired TT or RPC planes is larger than 19. The complementary sample is defined as $0\mu$. $0\mu$ events contain the signals of $\tau \rightarrow 1\,h$, $\tau \rightarrow 3\,h$, and $\tau \rightarrow e$ decay channels. $1\mu$ events contain the $\tau \rightarrow \mu$ decay channel. Most of the signal events occur at low muon momentum, thus a muon momentum cut at 15 GeV/c was introduced to accelerate the finding of signal for $\nu_\mu \rightarrow \nu_\tau$ oscillations.

The data set used in the present analysis consists of the $0\mu$ events and the $1\mu$ events with a muon momentum smaller than 15 GeV/c that were collected during the 5 years of run. With respect to our most recent study [6], it now includes the last missing sample, the $0\mu$ events of the 2012 run. For runs 2008–2009, all events have been searched for in the two most probable bricks, but so far only in the first most probable brick for runs 2010–2012. The numbers of analyzed events are summarized in Table 1.\(^1\)

\(^1\) An additional sample of 835 $1\mu$ events with a muon momentum larger than 15 GeV/c from runs 2008–2009 has also been analyzed for the purpose of probing our understanding of the beam spectrum and the detector response. They are not included in the data set used for this paper. The grand total number of fully analyzed events is therefore 5520.
Fig. 1. Display of the $\nu_\tau$ candidate event as seen by the electronic detectors in the $x$–$z$ projection (top) and $y$–$z$ projection (bottom). Neutrinos are coming from the left side. The brick containing the neutrino interaction is highlighted in magenta. Solid lines show the position of tracks measured in the primary and downstream bricks. Dashed lines show the linear extrapolation of the tracks using positions and slopes at the last measured point in the bricks. Labeled tracks are discussed in the text. The pattern of hits starting from the daughter track visible in the $x$–$z$ projection in the PT is consistent with a backscattered proton or pion from an interaction of the daughter track.

The selection criteria of $\nu_\tau$ interactions and the evaluation of efficiencies and backgrounds are described in detail in Ref. [14]. The observation of three $\nu_\tau$ candidate events has been reported in previous articles [2,6,14]. A new $\nu_\tau$ candidate event was found in this new sample and is reported here.

3. Description of the new $\nu_\tau$ candidate event

This neutrino interaction occurred on 9 September 2012 in the second super module, ten brick walls upstream of the spectrometer. The event is classified as $0\mu$. Figure 1 shows a display of the event as seen by the electronic detectors.

A converging pattern of 10 tracks was found in the changeable sheets and the primary vertex was located, 18 plates from the downstream face. The primary vertex consists of four tracks, of which one exhibits a kink topology (decay vertex). No nuclear fragment associated with the decay vertex was found by a dedicated scanning procedure with an extended angular acceptance (up to $\tan \theta = 3.5$, $\theta$ being the angle of the track with respect to the $z$ axis) [15,16]. Two electromagnetic showers initiated...
by conversions of γ-rays have been detected, both pointing to the primary vertex as described below. Figure 2 shows a display of this event as reconstructed in the brick. Momenta of the reconstructed tracks are determined by multiple Coulomb scattering (MCS) in the bricks [17].

- Track 1 is the parent track of a kink topology with an angle of \((137 \pm 4)\) mrad. The flight length is \((1090 \pm 30)\) μm. The longitudinal coordinate of the decay vertex with respect to the downstream face of the lead plate containing the primary vertex \((z_{\text{dec}})\) is \((406 \pm 30)\) μm. The kink angle and \(z_{\text{dec}}\) satisfy the topological selection for the \(\nu_\tau\) interaction search, which is \(\theta_{\text{kink}} > 20\) mrad and \(z_{\text{dec}} < 2600\) μm. This track is the τ candidate.

- Track 2 has a momentum of \((1.9^{+0.3}_{-0.2})\) GeV/c and was followed in the downstream bricks till the end of the target. It exits the target and enters the spectrometer leaving hits in the PT but not in the RPC, as can be seen from Fig. 1.

- Track 3 has a momentum of \((1.1^{+0.2}_{-0.1})\) GeV/c and has an interaction just before entering the 2nd downstream brick, producing two charged tracks in the brick.

- Track 4 is a heavily ionizing particle having \(p\beta = (0.4 \pm 0.1)\) GeV/c. It stops between the 1st and 2nd downstream bricks. From its range, \((94 \pm 1)\) g/cm², the particle is identified as a proton with a momentum of \((0.7 \pm 0.1)\) GeV/c.

- The kink daughter track has a momentum of \((6.0^{+2.2}_{-1.2})\) GeV/c. Its impact parameter with respect to the primary vertex is \((146 \pm 5)\) μm. It was followed in the downstream bricks till the end of the target. It exits the target, stopping in the spectrometer after leaving a signal in three RPC planes (Fig. 1).

None of the charged particles at both vertices is identified as an electron due to the absence of electromagnetic showers. All tracks were followed down in the downstream bricks and a total of 20 bricks were analyzed.

The momentum of track 2 was measured at each downstream brick over 10 bricks and the values were combined to estimate the momentum at the primary vertex. Track 2 is not classified as a muon since the total material crossed is 604 g/cm², which is below the lower cut for μ identification, set at 660 g/cm². To separate muons from hadrons, momentum-range correlations are characterized by a discriminating variable \(D_{\text{TFD}} = \frac{L}{R(p)} \frac{\langle \rho \rangle}{\rho}\), where \(L\) is the track length, \(R(p)\) is the range in lead of a muon with momentum \(p\), \(\langle \rho \rangle\) is the average density along the path, and \(\rho\) is the lead density [14]. A track is classified as a muon if \(D_{\text{TFD}}\) is above 0.8 while for track 2 we have \(D_{\text{TFD}} = 0.40^{+0.04}_{-0.05}\). Thus the muon hypothesis for track 2 is rejected. A further test of the hadron/muon hypothesis

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**Fig. 2.** Event display of the fourth \(\nu_\tau\) candidate event in the \(y-z\) projection longitudinal to the neutrino direction (left) and in the view transverse to the neutrino direction (right). The primary and decay vertices are indicated as “v1” and “v2” respectively. Labeled tracks are discussed in the text.
was performed using the track length in the TT and the RPC [18]. Track 2 crosses 12 planes. Figure 3 shows the Monte Carlo distribution of track lengths for hadrons and muons with momentum \((1.9^{+0.3}_{-0.2})\) GeV/c originating in the same target position as the observed event. The probability of a muon crossing fewer than 13 planes is 0.4% while the probability of a pion crossing more than 11 planes is 9.2%. This result confirms the rejection of the muon hypothesis.

Track 3 is identified as a hadron due to the presence of an interaction. The kink daughter track is identified as a hadron based on \(D_{TD} = 0.18 \pm 0.04\).

The conversion point of \(\gamma\)-ray 1 is in the lead plate containing the primary vertex, 376 \(\mu\)m upstream of the decay vertex. The energy of \(\gamma\)-rays is measured by MCS of the \(e^+\) and \(e^-\) pair [17] taking their energy loss into account. \(\gamma\)-ray 1 has an energy of \((0.7^{+0.2}_{-0.1})\) GeV and its impact parameter to the primary vertex is \((2.8 ^\pm 8)\) \(\mu\)m.

The conversion point of \(\gamma\)-ray 2 is 5 lead plates downstream of the primary vertex. \(\gamma\)-ray 2 has an energy of \((4.0^{+4.7}_{-1.4})\) GeV. Its impact parameter is \((33^{+43}_{-33})\) \(\mu\)m with respect to the primary vertex while it is \((267 \pm 36)\) \(\mu\)m with respect to the decay vertex. The probability that it originates from the decay vertex is less than \(10^{-3}\). Neither \(\gamma\)-ray is from \(\tau\) decay and the candidate is \(\tau \rightarrow 1\) h decay.

The invariant mass of \(\gamma\)-ray 1 and \(\gamma\)-ray 2 is \((0.59^{+0.20}_{-0.15})\) GeV/c\(^2\), indicating that they are not the decay products of the same \(\pi^0\).

The scalar sum of the momenta of all particles measured in the emulsion films \((p_{sum})\) is \((14.4^{+3.9}_{-2.7})\) GeV/c.

The momentum of the daughter track \((p_{2\gamma})\) is \((6.0^{+2.2}_{-1.2})\) GeV/c, well above the cut value of 2 GeV/c [14]. The transverse momentum \((p_T^{2\gamma})\) at the decay vertex is \((0.82^{+0.30}_{-0.16})\) GeV/c, which is above the lower cut of 0.6 GeV/c. The missing transverse momentum at the primary vertex \((p_T^{missing})\) is \((0.55^{+0.30}_{-0.20})\) GeV/c, thus below the maximum allowed value, which is set at 1 GeV/c. As shown in Fig. 4, the angle between the \(\tau\) candidate direction and the sum of the transverse momenta of the other primary particles \((\Delta\phi_{1H})\) is \((166^{+2}_{-31})\) degrees, well above the lower cut at 90 degrees. The values of the kinematical variables for this event are summarized in Table 2. The Monte Carlo distributions of the variables and the measured values are shown in Fig. 5. The measured values are well within the expected signal region.
Fig. 4. The $\tau$ direction (red arrow) and the other primary particles (black arrows) in the plane transverse to the beam. The blue arrow shows the vectorial sum of the primary particles except the parent.

Table 2. Selection criteria for the $\nu_{\tau}$ interaction search in the $\tau \rightarrow 1h$ decay channel and the values measured for the fourth $\nu_{\tau}$ candidate event. The cut marked with * is applied if there is at least one $\gamma$-ray originating from the decay vertex.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Selection</th>
<th>Measured value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\theta_{\text{kink}}$ (mrad)</td>
<td>$&gt;20$</td>
<td>$137 \pm 4$</td>
</tr>
<tr>
<td>$z_{\text{dec}}$ ($\mu$m)</td>
<td>$&lt;2600$</td>
<td>$406 \pm 30$</td>
</tr>
<tr>
<td>$p_{2\gamma}$ (GeV/c)</td>
<td>$&gt;2$</td>
<td>$6.0^{+2.2}_{-1.2}$</td>
</tr>
<tr>
<td>$p_{T}^{\gamma}$ (GeV/c)</td>
<td>$&gt;0.6$ (0.3*)</td>
<td>$0.82^{+0.30}_{-0.16}$</td>
</tr>
<tr>
<td>$p_{T}^{\text{miss}}$ (GeV/c)</td>
<td>$&lt;1$</td>
<td>$0.55^{+0.30}_{-0.20}$</td>
</tr>
<tr>
<td>$\Delta \phi_{1\mu}$ (degrees)</td>
<td>$&gt;90$</td>
<td>$166^{+2}_{-31}$</td>
</tr>
</tbody>
</table>

4. Results The estimated signal and background for the observation of $\nu_{\tau}$ candidates in the data sample analyzed in this paper are obtained as described in Ref. [14] and summarized in Table 3. The systematic uncertainties are estimated to be 20% on the signal, 20% on the charm background, 30% on the hadronic background, and 50% on the large-angle muon scattering background, i.e. muon scatterings mimicking $\tau \rightarrow \mu$ decays. The expected signal consists of $(2.11 \pm 0.42) \nu_{\tau}$ events in all decay channels, using $\Delta m_{23}^{2} = 2.32 \times 10^{-3}$ eV$^{2}$ and $\sin^{2} 2\theta_{23} = 1$. The total expected background for the sample is $(0.233 \pm 0.041)$ events.

Four $\nu_{\tau}$ candidate events have been detected in the analyzed samples: two in the $\tau \rightarrow 1h$ decay channel, one in $\tau \rightarrow 3h$, and one in $\tau \rightarrow \mu$ [2,6,14]. The values of $p_{\text{sum}}$ measured for the four events are compatible with the corresponding signal Monte Carlo distribution as shown in Fig. 6.

The significance of the observation of the four $\nu_{\tau}$ candidate events is estimated by considering the confidence for excluding the null hypothesis. Individual $p$-values of the $\tau$ decay channels are combined independently according to Fisher’s rule into an estimator $p^{*} = p_{h}p_{3h}p_{\mu}p_{e}$ [19,20]. In order
Fig. 5. Monte Carlo distributions of the kinematical variables for $\nu_\tau$ events passing all the cuts in the $\tau \rightarrow 1h$ decay channel. Red lines show the measured values for the candidate event reported here and red bands their error. Gray areas show the region excluded by the selection criteria.

Table 3. Estimated signal and background for the analyzed sample and the number of observed events.

<table>
<thead>
<tr>
<th>Decay channel</th>
<th>Expected signal</th>
<th>Number of observed events</th>
<th>Expected background</th>
<th>Hadronic re-interactions</th>
<th>Large-angle muon scattering</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\tau \rightarrow 1h$</td>
<td>0.41 ± 0.08</td>
<td>2</td>
<td>0.033 ± 0.006</td>
<td>0.015 ± 0.003</td>
<td>0.018 ± 0.005</td>
</tr>
<tr>
<td>$\tau \rightarrow 3h$</td>
<td>0.57 ± 0.11</td>
<td>1</td>
<td>0.155 ± 0.030</td>
<td>0.152 ± 0.030</td>
<td>0.002 ± 0.001</td>
</tr>
<tr>
<td>$\tau \rightarrow \mu$</td>
<td>0.52 ± 0.10</td>
<td>1</td>
<td>0.018 ± 0.007</td>
<td>0.003 ± 0.001</td>
<td>–</td>
</tr>
<tr>
<td>$\tau \rightarrow e$</td>
<td>0.62 ± 0.12</td>
<td>0</td>
<td>0.027 ± 0.005</td>
<td>0.027 ± 0.005</td>
<td>–</td>
</tr>
<tr>
<td>Total</td>
<td>2.11 ± 0.42</td>
<td>4</td>
<td>0.233 ± 0.041</td>
<td>0.198 ± 0.040</td>
<td>0.021 ± 0.006</td>
</tr>
</tbody>
</table>

to take into account the systematic uncertainties of the backgrounds, 100 sets of randomized backgrounds are generated. A mean $p$-value of $1.24 \times 10^{-5}$ is obtained by Monte Carlo calculation of the tail probability corresponding to the observed value of $p^*$. The absence of signal can be excluded with a significance of 4.2$\sigma$.

Alternatively a hypothesis test employing a likelihood-based approach [21] was performed. The likelihood function is $L(\mu) = \prod_{i=1}^{4} e^{-(\mu s_i + b_i)} (\mu s_i + b_i)^{n_i} / n_i!$. The index $i$ runs over decay channels, the parameter $\mu$ determines the strength of the signal process ($\mu = 0$ corresponds to the background-only hypothesis), $s_i$ and $b_i$ are the numbers of expected signal and background events, $n_i$ the number of observed events. The systematic uncertainties of the backgrounds were taken into account in a similar way as above. A $p$-value of $1.03 \times 10^{-5}$ corresponding to a significance of 4.2$\sigma$ for the exclusion of the null hypothesis is obtained.

Given the 4 observed events and the expected background of $(0.233 \pm 0.041)$ events, the confidence interval of $\Delta m^2_{\tau\bar{\tau}}$ is estimated with the Feldman–Cousins method [22], assuming maximal
Fig. 6. Monte Carlo distribution of the scalar sum of the momenta of all particles measured in the emulsion films, $p_{\text{sum}}$, for $\nu_\tau$ events passing all the cuts in all decay channels. Red lines show the measured values for the four $\nu_\tau$ candidate events: “1” and “4” in the $\tau \rightarrow 1h$ decay channel, “2” in $\tau \rightarrow 3h$, and “3” in $\tau \rightarrow \mu$ [2,6,14].

mixing. The systematic uncertainties of signal and background are taken into account to marginalize the likelihood function used for the ordering principle. The 90% confidence interval of $\Delta m_{23}^2$ is $[1.8, 5.0] \times 10^{-3} \text{eV}^2$. An alternative analysis employing a Bayesian approach [1] with a flat prior on $\Delta m_{23}^2$ was performed. The credible interval of $\Delta m_{23}^2$ is $[1.9, 5.0] \times 10^{-3} \text{eV}^2$. More precise measurements by other experiments [23–28] are within these intervals.

5. Conclusions and prospects A new $\nu_\tau$ candidate event, with the $\tau$ decaying into a hadron, found after adding an extended data sample is reported. Given the analyzed sample, $\nu_\mu \rightarrow \nu_\tau$ oscillations are established at the 4.2$\sigma$ level. The search for events, not found in the most probable bricks in the 2010–2012 runs, is being extended to the second most probable bricks for future results.

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