

Constraints on Geological Strain Rates: Arguments From Finite Strain States of Naturally Deformed Rocks

O. A. PFIFFNER¹ AND J. G. RAMSAY

Geologisches Institut, Eidgenoessischen Technischen Hochschule-Zentrum, CH-8092 Zurich, Switzerland

A summary of known finite strain states is presented; longitudinal strains ($1 + e$) as measured in many rocks often range from 1 to 40 and 1 to 0.025. The time span available to produce such measurable strains in young orogenic zones seems to be less than 10 m.y., possibly less than 1 m.y., which constrains conventional strain rates into the range of 10^{-13} s^{-1} to 10^{-15} s^{-1} . For both pure and simple shear (the most efficient way and a much less efficient way to accumulate incremental strains, respectively) the ellipticity of the finite strain ellipse increases in a nonlinear manner. Finite strain variations in adjacent layers, which give rise to features such as cleavage refraction, arise with only slight differences in the strain rates within these layers.

INTRODUCTION

The amount of data on the rates at which natural rock deformations take place is rather small. That which is quoted most frequently is based on geodetic surveys in the vicinity of the San Andreas Fault [Whitten, 1956]. Triangulation carried out over a period of 20 years showed systematic displacements that indicated that any initially rectangular block would gradually become changed into a parallelogram with a change of azimuth of 1 second of arc every 10 years. From this observation it is possible to conclude that if the deformation is taking place by simple shear parallel to the fault, the shear strain rate $\dot{\gamma}$ is $1.5 \times 10^{-13} \text{ s}^{-1}$ and the principal extension rates $\dot{\epsilon}_1 = -\dot{\epsilon}_2$ ($\dot{\epsilon}_1 = \dot{\gamma}/2$ in simple shear) is $7.5 \times 10^{-14} \text{ s}^{-1}$. However, the surface movements in these zones might not be truly representative of the deeper crustal levels [Johnston *et al.*, 1977].

Another method of calculating strain rate has been based on the isostatic adjustment that has taken place as a result of removal of bodies of ice or water from the earth's surface [Crittenden, 1967]. Hicks and Shofnos [1965] used measurements of uplifts in Glacier Bay, Alaska, indicating strain rates of from 0.5×10^{-14} to $2.5 \times 10^{-14} \text{ s}^{-1}$.

Heard [1976] suggested that strain rates could be estimated from displacement rates of seafloor spreading and that values generally lie between 10^{-13} and 10^{-14} s^{-1} . However, before such a calculation can be made, some specific model for progressive deformation of the crust must be selected because different strain increment models dissipate the plate displacements at different strain rates.

In the European Alpine orogenic belt it seems likely that 150-400 km of crustal shortening has taken place [Trimpy, 1972, 1973; Gilluly, 1972] over a time period from the Upper Cretaceous to the Oligocene. It seems to us difficult to use this data to determine the average strain rate as proposed by Heard [1976] without presupposing some specific model for the strain history of the plate collision zone.

The aim of this paper is to attack the strain rate problem from a new viewpoint. Structural geologists have collected much data on finite strains in naturally deformed rocks. In certain regions we have some knowledge on the time taken for

the total deformation to have taken place. In the sections which follow we discuss the possibility of combining this data to arrive at values of the geologically representative average strain rate that could have produced the observed finite strain.

STRAIN RATE

Strain rate is defined as the proportional change in length of a line element in an infinitesimal time interval, which in the geological sciences is a unit of 1s duration. For example, if a line extends by one tenth (10^{-1}) of its length prior to the strain increment in 1s, the strain rate is defined as

$$\dot{\epsilon} = 10^{-1} \text{ s}^{-1}$$

Two types of strain rates may be defined [Nadai, 1950, p. 74]: The conventional strain rate, where the length prior to the strain increments is always chosen the same (l_0),

$$\dot{\epsilon}_c = dl_i/l_0 = \text{const}$$

and the natural strain rate, where the length prior to the strain increments includes the changes in length of the preceding increments,

$$\dot{\epsilon}_n = \frac{dl_i}{l_0 + dl_1 + dl_2 + \dots + dl_{i-1}}$$

It will be seen from the above equations that for constant incremental length changes dl_i the natural strain rate $\dot{\epsilon}_n$ will decrease in the course of the deformation history, whereas the conventional strain rate $\dot{\epsilon}_c$ will remain constant. Since a constant strain rate relates better to the concept of steady flow of rocks, we use conventional strain rate throughout this paper. How can strain rate per second be derived from finite length changes which have taken place over a longer period of time than 1 s? We solve this problem by superposing strain increments and comparing the resulting finite strains with the incremental strains (i.e., the strain rate). Under these circumstances the finite elongation $1 + e$ will increase in a linear or nonlinear manner, depending upon whether one uses natural or conventional strain rates respectively (cf. Figure 1). Thus, if one simply divides strain e by time t (as proposed by Price [1975]), one determines a natural strain rate which is much larger than a corresponding conventional strain rate producing the same finite strain after the same number of increments.

In steady state flow processes, where identical increments of

¹ Now at Institut de Géologie, Université de Neuchâtel, CH-2000 Neuchâtel, Switzerland.

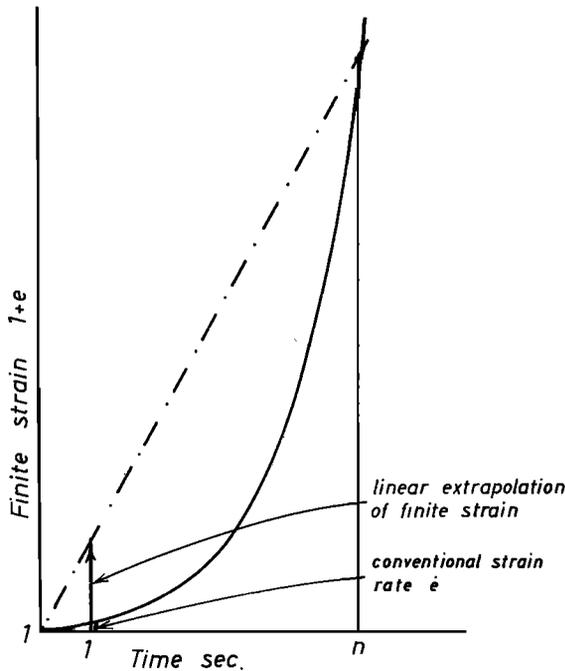


Fig. 1. Growth of finite strain in a time period of n seconds, illustrating the errors resulting from linearly extrapolating the finite strain.

distortion are developed during each second, the changes in longitudinal strain rate along any chosen physical line element in the deforming body vary because the line progressively changes its orientation with respect to the principal axes of strain during the deformation sequence. The incremental length changes then become very complex.

Strain rate is a second-order tensor; to define it completely, we need to specify first three angles defining the spatial orientations of the orthogonal principal strain rate axes with reference to three chosen coordinate reference axes; second, the values of the three principal strain rates ($\dot{e}_1, \dot{e}_2,$ and \dot{e}_3); and third, three rotation rates or vorticities of these principal strain rate directions with respect to the chosen coordinate reference axes ($\dot{\omega}_1, \dot{\omega}_2,$ and $\dot{\omega}_3$). The values taken by the three vorticities are especially important in controlling the finite strains that are built up during a progressive deformation.

In order to simplify the analysis, yet without losing relevance to problems of deformation in the crust of the earth, we have made a few assumptions and approximations. We have investigated systems which are those of plane strain, considering that changes in the intermediate strain rate \dot{e}_2 and vorticities $\dot{\omega}_1$ and $\dot{\omega}_3$ (around the \dot{e}_1 and \dot{e}_3 axes, respectively) can be neglected. We know from our analyses of finite strain that the shapes of strain ellipsoids do not always agree with the plane strain constant volume relationships expressed by

$$(1 + e_2)^2 = (1 + e_1)(1 + e_3)$$

However, many of these ellipsoids can be satisfactorily explained by plane strain under conditions of volume change [Ramsay 1967, p. 162; Ramsey and Wood, 1973; Graham, 1978] or by superposing successive plane strains in a non-coaxial manner [Ramsay, 1967, p. 326].

We are also of the opinion that large-scale displacement and average strain patterns that come about during the forcing together of relatively rigid crustal plates in subduction zones are constrained by geometric boundary conditions such

that least differential displacement, and therefore least absolute values of strain occur in directions parallel to plate intersections. Furthermore, many of the local deformations seen in naturally deformed rocks are constrained by local conditions which tend to impose plane strains (block faulting, simple shear zone formation, ideal bedding plane slip during buckle folding in stratified rocks).

In two-dimensional plane strain, which we will examine in detail below, four terms are needed to specify a general steady state flow process:

- Θ orientation of the principal strain rate axes from the x and y coordinate directions;
- \dot{e}_1, \dot{e}_2 values of the principal strain rates;
- $\dot{\omega}$ rotation rate or vorticity of the principal strains.

These four strain rate components are related to the displacement rate components \dot{u} (parallel to x) and \dot{v} (parallel to y) of all points with coordinates (x, y) in the system (see Figure 2).

The effect of a two-dimensional steady state process is illustrated in Figure 3. An initial body ($opqr$) is, after a given time (t_1), transformed to a parallelogram shape ($op_1q_1r_1$). In this deformed material we now draw a new standard grid ($op'q'r'$) of the same shape as $opqr$ and allow this to become similarly modified after another interval of time t_1 . Now after a total time ($t_2 = 2t_1$) ($op'q'r'$) is transformed into ($op_2q_2r_2$) of identical form to ($op_1q_1r_1$), and ($op_1q_1r_1$) becomes transformed to ($op_2q_2r_2$). Thus we are able to transform geometrically an initial marker shape by successive identical incremental steps to develop a large finite strain. Mathematical analysis of sequences like this to compute the properties of the finite strain can be easily handled using a computer to produce the successive matrix products [Ramsay, 1967, pp. 322-332] and to analyze the final displacement geometry in terms of principal finite strains (eigenvalues and eigenvectors of the matrix product) and body rotations [Ramsay and Graham, 1970, p. 790]. In a steady state or constant incremental process it is possible to describe the movements to particles in the deforming medium by a series of path lines (Figure 3e), and Ramberg [1975a, b] has shown how an analysis of such particle paths can be used to establish the geometry of the finite displacement and strain state.

The manner whereby an incremental process builds up a

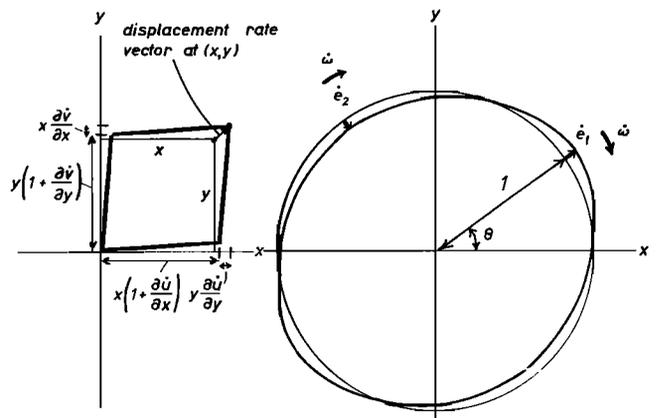


Fig. 2. Relations between displacement rate vector of a point (x, y) with components \dot{u} and \dot{v} parallel to x and y , respectively, displacement rate gradients, strain rate components \dot{e}_1 and \dot{e}_2 and vorticity rate $\dot{\omega}$.

Progressive deformation by progressive displacement increments

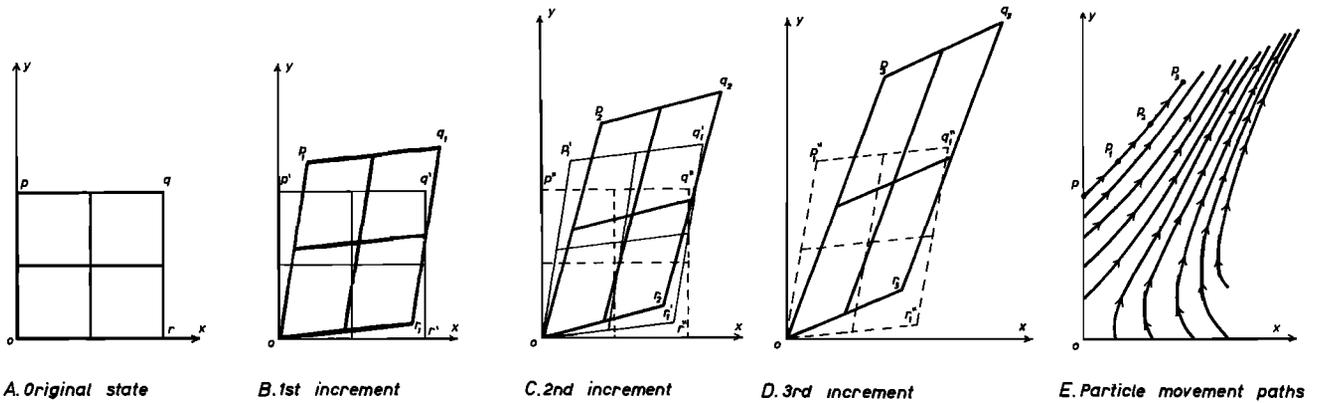


Fig. 3. Progressive deformation of an element by the superposition of successive displacement increments.

large finite strain is quite complex, depending upon the nature of the displacement increments and therefore upon the values and orientations of the two principal strain rates and the vorticity of the system. The vorticity is perhaps one of the most critical aspects of the geometry relating to effectiveness by which large strains grow with time. We will now examine the nature of the finite strains which can be developed from a variety of types of steady state flow.

FINITE STRAIN ARISING FROM STEADY STATE FLOW

Figures 4 and 5 illustrate some of the types of strain sequences that can arise from steady state flow. The basic incremental strain was considered as an incremental plane distortion without dilation ($\dot{\epsilon}_1 = -\dot{\epsilon}_2, \Theta = 0$) followed by an incremental rotation (governed by the vorticity ω). Successive matrix products were computed for different proportions of distortion and vorticity. The value of the principal incremental strain e_i , used in these calculations was 0.1, and the incremental rotation ω_i , varied from zero (pure shear, with coaxial increments) through $\omega_i = 5.455^\circ$ (simple shear) to values of $\omega_i = 20^\circ$. The graphs shown in Figure 4 show how the finite strain values (strain ellipse axes of length $1 + e_1$, and $1/(1 + e_1)$) vary with their orientation θ , and Figure 5 illustrates successions of strain ellipses arising with different values of incremental rotation, plotted for every two increments.

With pure shear (Figure 5a), because the increments are superposed coaxially (the incremental rotation being zero), the finite strains grow in the most rapid way possible, and high finite strains are produced after only a few increments. The ellipticity of the finite strain ellipse is a power series of the incremental distortion:

$$1 + e_1 = (1 + e_i)^n$$

Ellipticity

$$\frac{1 + e_1}{1 + e_2} = (1 + e_i)^{2n}$$

where n is the number of increments.

With simple shear (Figure 5c) the ellipticity of the finite strain ellipse also increases in a nonlinear manner but not at such a rapid rate as was the case with pure shear. The principal axes of successive finite strains rotate in the direction of

the incremental rotation, but the rate of rotation of the finite ellipse axes progressively decreases, and the ellipse gradually approaches an asymptote oriented at 45° to the axes of the first incremental strain ellipse (see Figures 4 and 5c).

A whole spectrum of possibilities of strain sequences lies between simple shear and pure shear (e.g., see Figure 4, curves with incremental rotation lying between 0.0 and 5.455). These strain paths accumulate total finite strains with an efficiency between those of pure shear and simple shear. They also have an interesting characteristic that for each value of incremental rotation the axes of the finite strain ellipse approach asymptotically an orientation which lies between the one for pure and simple shear.

Where the incremental rotation exceeds that for simple shear, several other important new characteristics appear in the finite strain sequences (Figures 5a and 5b and Figure 4, curves where $\omega_i > 5.455$). Each strain path begins with an increase in finite strain with successive increments. However, at some particular stage in the sequence the rate of growth of the finite strain declines, eventually to zero, and the finite strain ellipse reaches a maximum value of ellipticity. The value of this maximum finite strain is a function of the value of the incremental rotation component; rotations equal to that for simple shear are infinite, and the maximum finite strain decreases as the incremental rotation increases (see curves in Figure 4). With increasing deformation, the finite strain ellipse axes are no longer constrained to an asymptotic position like those of simple shear. They continue to rotate through the position at 45° to the initial increment, and as this rotation continues, the finite strain decreases. With increasing increments the finite strain ellipse axes eventually align themselves perpendicular to those of the initial increment, and when they reach this position, the finite strain becomes completely removed. The strain ellipse passes through a circular condition, and the sequence begins once more as it did with the initial undeformed circular marker. The number of increments required to complete a deformation-undeformation cycle depends upon the value of the incremental rotation (see Figures 5a and 5b), the highest incremental rotations give rise to the most rapid turnover cycles (and also gives those systems with the lowest maximum finite strain ellipticities). The possibility of producing finite strain pulsations was first appreciated by Ramberg

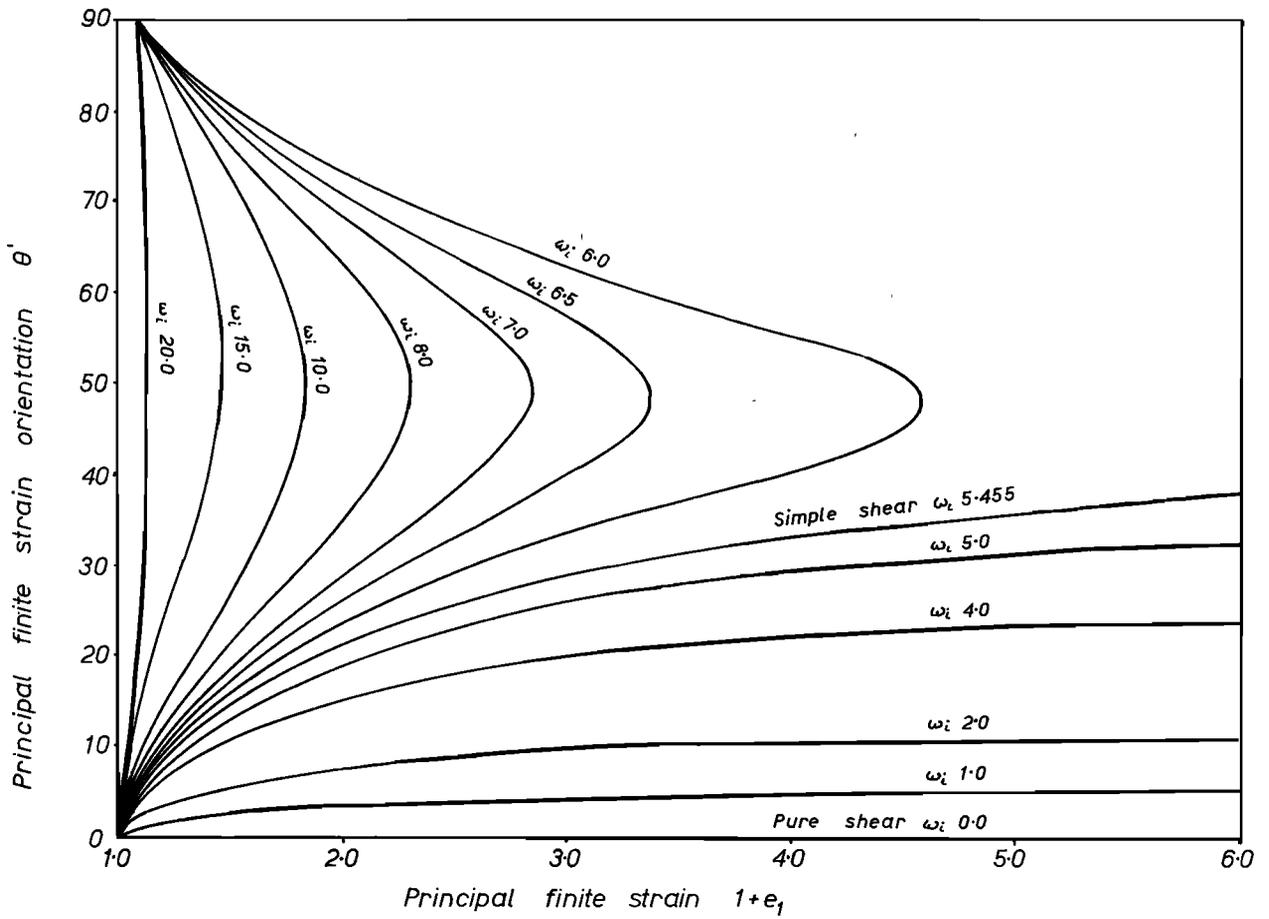


Fig. 4. Curves for finite strain and finite rotation derived by superposing successively increments of distortion ($e_{1i} = 0.1$) and rotation ω_i .

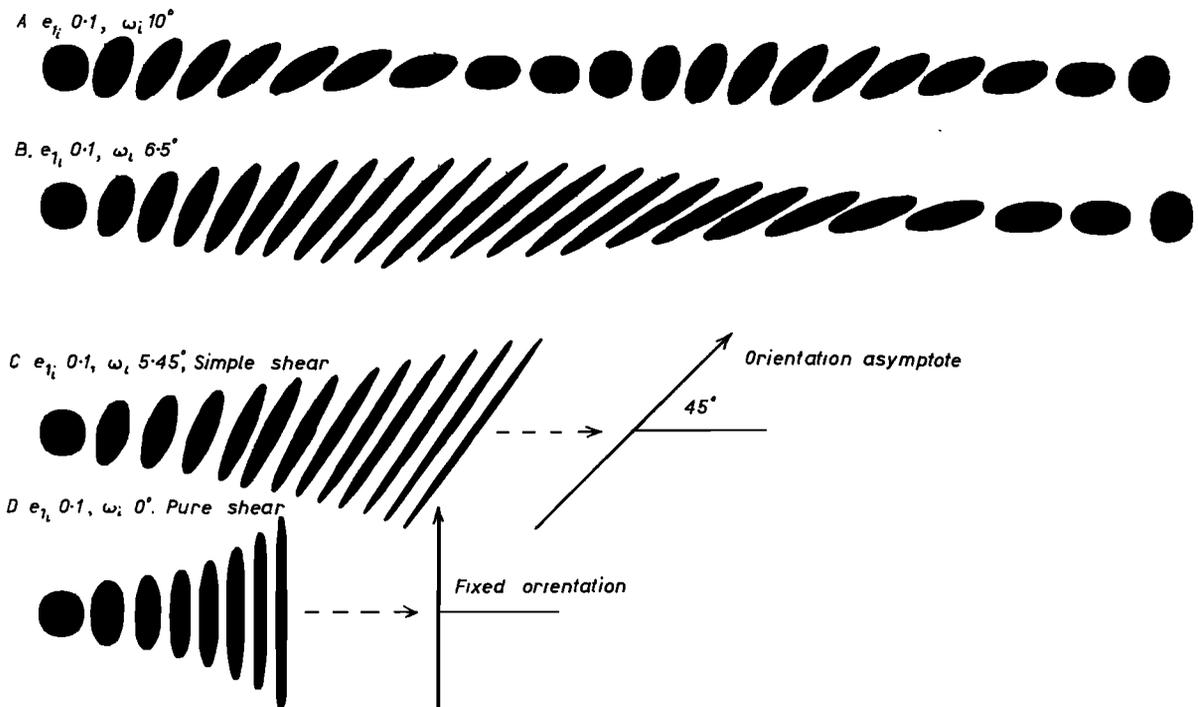


Fig. 5. Diagrammatic representation of the successions of finite ellipses in four of the parts illustrated graphically in Figure 4.

[1975a,b] when he investigated the types of flow systems produced by successively superposing alternating increments of pure and simple shear.

It should be clear from this general discussion that steady state flow processes with constant distortional strain rate can produce an enormous range of possible finite strain states depending on the vorticity of the system. For a given time of deformation the largest strains occur in irrotational pure shear. Progressively increasing, but smaller strains occur with finite rotation in simple shear, and where vorticities exceed those for simple shear, periodic deformation and removal of deformation take place with large finite rotations.

It can be seen from this analysis of the complete spectrum of possibilities that arise from steady state flow that if the rotations and vorticities are unconstrained, there is no simple rule relating finite strain to distortional strain rate (Figure 6).

LIMITATIONS ON FLOW IN GEOLOGICAL SYSTEMS

We have discussed the geometrical effect of flow in some detail because now we wish to justify our choice of particular types of flow processes as end members limiting realistic types of geological deformation.

The first end-member is that type of steady state flow which leads to maximum finite strain from a given incremental or steady state flow process. There is no difficulty in selecting progressive pure shear as the most rapid of the finite strain growth processes (Figure 5d).

The end-member defining the minimum effectiveness of building large finite strain with a given flow process requires more detailed discussion. The general analysis of steady state flow has shown that certain processes lead to finite strains periodically increasing and decreasing in a pulsating way. How common is this effect in tectonic processes? Ramberg's [1975b, pp. 32-34] discussion of this point shows that rock flow of this type in nappe sheets and in fold formation is unlikely to be common, or if it does occur, it is likely to be for only short periods during the deformation history. He pointed out that the rotation of less ductile inclusions such as crystal porphyroblast or pebbles in a more ductile matrix could produce such a pulsatory strain effect in the inclusions. Such a process only occurs on a very local scale, and we cannot think of any tectonic process likely to have significance on a regional scale which

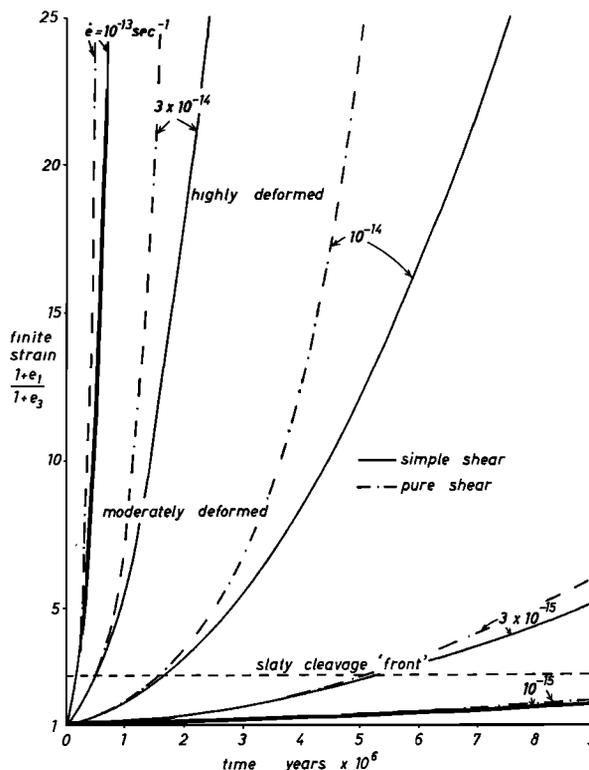


Fig. 7. Computations of finite strain state arising by processes of pure shear and simple shear with steady state flow of differing rates over a particular time interval.

could build pulsatory finite strains in this way. The steady state process which forms the boundary to such pulsatory processes is simple shear (Figure 5c). The principal strain rate axes during steady state flow by simple shear are oriented at 45° to the shear displacement direction of the shear, whereas the finite strain axes come to lie closer to the shear direction. During the flow process shown in this figure the distortional effects of the increment move the established finite strain axis anticlockwise, but the incremental rotation or vorticity always move it clockwise at a rate just slightly greater than that of the anticlockwise rotation. With large shears and large finite strains, the two effects are almost identical in their positive and negative rotational effects: the principal extension axis of the finite strain comes to lie closer and closer to the shear direction but never passes through it. This means that the finite strain can never acquire increments which lead to a decrease of its previously established total strain state. Because simple shear is the limiting case of effectiveness of the vorticity to pass into the 'pulsating' strain field and because we do not believe that this field has regional geological significance, we think it justified to take simple shear as the lower most bound of any steady state processes which lead to large strain states in tectonic processes.

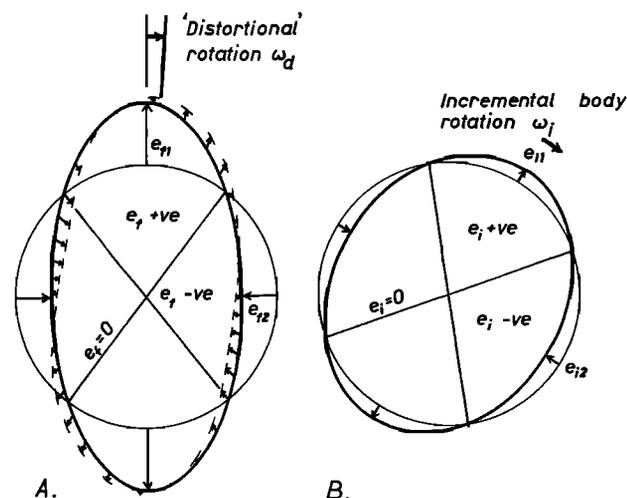


Fig. 6. General effects of superimposing an incremental strain B on already established finite strain state A.

FINITE STRAIN STATES AND TIME IN TECTONIC PROCESSES

There is now available a very large bank of data giving measured finite strains from many different types of naturally deformed rock in many differing environments, and a summary is set out in Appendix A, Figure A1, and Table 1. These data have been acquired from the measurement of a whole

variety of strain markers, thus yielding different types of strain parameters. To facilitate comparison, the data have been referred to one of the following parameters: longitudinal strain ($1 + e$), shear strain (γ), or axial ratio (R) of the strain ellipse. A review of this information shows the following minimum and maximum finite strains:

Longitudinal strains from

$$1 + e_1 = 1 \text{ to } 3 \quad 1 + e_3 = 1 \text{ to } 0.13$$

Shear strains from

$$\gamma = 0 \text{ to } 42.55$$

Axial ratios from

$$R = 1 \text{ to } 13.5$$

(Table 1) and

$$R = 1 \text{ to } 25$$

Some of the data in Figure A1 and Table 1 represent regionally penetrative deformations probably occurring through rock masses of one or more cubic kilometers in volume. In many instances, possible ductility contrasts (e.g., between fossils and matrix) means that the strain quoted is a minimum value, and in others, significant volume reductions may be present. High strains of γ up to 40 (equivalent to 'axial ratios' of 1600) do occur and can occasionally be measured, but they seem to be typically localized in narrow planar zones, having a special evolutionary history (thrust and shear zones, mylonite belts).

The duration of time necessary to develop these finite strains is very difficult to assess. Precise stratigraphical control for upper and lower time brackets for individual 'phases of deformation' are difficult to obtain, and the errors involved may be critical for the arguments presented here; moreover, they always give maximum intervals and deformation throughout these intervals was not necessarily continuous. Detailed structural analyses of fold-and-thrust and imbricate thrust terrains often indicate that such time periods may be subdivided into sequences of subphases any one of which could produce the finite strain in a comparatively short time period [e.g., *Dahlstrom*, 1970; *Pfiffner*, 1978].

In Figure B1, some data on orogenic movements are listed. The time interval for penetrative deformation (e.g., indicated by folding) typically range from 1 to 30 m.y., with a maximum of the data investigated lying between 1 and 5 m.y. But it is possible the finite strains may have been developed over a much shorter time interval, perhaps of the order of 100,000 years.

STRAIN RATES AND FINITE STRAIN CALCULATIONS

We now wish to show how the pure and simple shear models for progressive deformation can be used to predict the finite strains arising by steady state constant strain rate flow.

The most effective way of building up a large finite strain from strain increments in plane strain is that of progressive pure shear. Clearly, this is a highly specialized incremental process, but finite strains might arise in this way from geological processes. It can easily be shown that the general case of heterogeneous finite strain leads to general states of rotational strain [*Ramsay and Graham*, 1970], and clearly such rotational finite strains cannot have been produced by a progressive irrotational process. However, at a few singular points in a het-

erogeneously strained body it may be possible to have finite strains close to pure shear. For example, the strains built up along the inner arc of a buckled competent layer approximate to pure shear, especially at the fold hinge zones.

The build up of finite strain by progressive pure shear with no volume dilation gives the following values for finite strain

$$1 + e_{1f} = (1 + \dot{e}_1)^n$$

$$1 + e_{2f} = 1$$

$$1 + e_{3f} = (1 + \dot{e}_1)^{-n}$$

where $1 + e_{1f}$, etc. refer to the lengths of the axes of the finite strain ellipsoid, and n the number of increments of the deformation. The actual calculation of the curves in Figure 7 is speeded up by using

$$\lim_{\gamma \rightarrow \infty} \left(1 + \frac{1}{\gamma} \right)^\gamma = 2.718$$

(the exponential constant e). This limit rewritten in terms of the above equations

$$\lim_{\substack{e \rightarrow 0 \\ n \rightarrow \infty}} (1 + e)^n = 2.718$$

Figure 7 shows strains arising over periods of several million years from different principal strain rates.

What is very striking here (Figure 7) is, first, the markedly nonlinear accumulation of finite strain with time and, second, how a comparatively small variation in strain rate leads to great differences in the finite strain accumulation in a specific period of time. If, for example, the deformation were continuous and took place over a period of 5 m.y., strain rates of $3 \times 10^{-14} \text{ s}^{-1}$ would produce very high finite strains, whereas strain rates of 10^{-15} s^{-1} would produce strains below the slaty cleavage front.

Pure shear gives rise to the most rapid growth of finite strain. We now investigate the effects of a similar range of strain rates but with the incremental process being that of simple shear, a process which we have shown to possibly mark the geologically least effective method of building finite strains. The various strain rates for pure shear have been transformed to shear displacement rates using $\dot{\gamma} = 2\dot{e}$, integrated over time periods from 0 to 10 m.y. and the finite shear strains γ_f transformed back into values for finite strains

$$\frac{1 + e_{1f}}{1 + e_{2f}} = \frac{1}{2} (n^2 \gamma^2 + 2 + n^2 (n^2 \gamma^2 + 4)^{1/2})$$

The curves illustrating strain accumulation with time (Figure 7) show broadly similar features to those for pure shear. For a given total deformation time, the finite strain for a given strain rate is less than that for pure shear.

As these two sets of calculations represent certain upper and probable lower bounds of effectiveness of accumulation of strain, we arrive at a most interesting conclusion: to satisfy geologically values of moderate finite strains built up by steady state flow over time periods of less than 5 m.y., our strain rates have to be constrained between the limits 10^{-13} s^{-1} and 10^{-15} s^{-1} . Strains faster than 10^{-13} s^{-1} produce very high strains (realized, e.g., in mylonite zones; see *Schmid* [1975] and *Pfiffner* [1977] for the Lochseiten calc mylonite) or necessitate deformation to take place in a time of much less than 1 m.y., whereas strain rates slower than 10^{-15} s^{-1} lead to very small strains.

TABLE 1. Strain Data Compilation

Source	Location	Rock Type	Strain Marker	Stretching $1 + e$	Shortening $1 - e$
<i>Badoux</i> [1963]	Alps/Helvetics	calcschistes	belemnites	1-3	
<i>Badoux</i> [1965]	Alps/Helvetics	limestone	belemnites	1.05-2.15	
<i>Badoux</i> [1970]	Alps/Helvetics	limestone	oöids	1.2-1.7	0.6-0.13
<i>Borradaile and Johnson</i> [1973]	Caledonides/Scotland	sandstone, siltstone	dykelets	1.25-2.57	0.67-0.34
<i>Bredden</i> [1956a]	Rheinisches Schiefergebirge	limestone, sandstone, slate, marl	fossils	1.02-1.33	0.87-0.51
<i>Bredden</i> [1956b]	Rheinisches Schiefergebirge	shale	fossils	1.05-1.1	0.8-0.7
<i>Bredden</i> [1957]	Rheinisches Schiefergebirge	sandstone, slate, graywacke	fossils	1.14-1.34	0.45-0.17
<i>Bredden</i> [1958a]	Rheinisches Schiefergebirge	shale	fossils	1.0-1.1	0.9-0.73
<i>Bredden</i> [1958b]	Rheinisches Schiefergebirge	slate	fossils	1.09	0.9-0.75
<i>Bredden</i> [1964]	Rheinisches Schiefergebirge	marl	fossils		0.82-0.67
<i>Chapple and Spang</i> [1974]	Appalachians	limestone	calcite twins	1.002-1.086	0.994-0.922
<i>Débat</i> [1974]	Variscides/Montagne Noire	gneiss	feldspar crystals	1.03-2.37	0.34-0.23
<i>Furtak</i> [1965]	Rheinisches Schiefergebirge	slate, sandstone	fossils, minor folds	1.13-1.28	0.75-0.65
<i>Gairola</i> [1976]	Lesser Himalaya	shale, limestone	nummulites		0.8
<i>Groshong</i> [1975]	Appalachians	limestone	calcite twins	1.0028-1.0419	0.9993-0.9433
<i>Langheinrich</i> [1967a]	Rheinisches Schiefergebirge	sandstone	brachiopods	1.12	0.8
<i>Langheinrich</i> [1967b]	Alps/N Calcareous Alps	marl	ammonites		0.96-0.7
<i>Mukhopadhyay et al.</i> [1969]	India	schist, phyllite	microfolds		0.23-0.15
<i>Nickelsen</i> [1966]	Appalachians	silt, shale	fossils		0.93-0.9
<i>Plessmann</i> [1965]	Rheinisches Schiefergebirge	slate, graywacke	worm tubes		0.9-0.6

Source	Location	Rock Type	Strain Marker	Axial Ratio of Strain Ellipse
<i>Albrecht and Furtak</i> [1965]	Alps/Subalpine Molasse	marl, marly limestone sandstone	fossils	1.1-1.4
<i>Audren et al.</i> [1976]	Variscides/Bretagne	conglomerate, schist	pebbles, quartz grains	1.2-6.2
<i>Bhattacharya</i> [1966]	India	conglomerate	pebbles	9.3
<i>Cloos</i> [1971]	Appalachians	limestone	oöids	1.07-8.04
<i>Dunnet</i> [1969]	Sardinia	oölite, grit	oöids, clasts	1.45-4.5
<i>Dunnet and Siddans</i> [1971]	Sardinia	grit, tuff	clasts	1.2-4.0
<i>Engelder and Engelder</i> [1977]	Appalachians	clastic sediments	crinoid ossicles	1.05-1.23
<i>Furtak and Hellermann</i> [1961]	Central Europe	sandstone, siltstone	fossil plants	1-1.5
<i>Le Corre and Le Théoff</i> [1976]	Variscides/Bretagne	conglomerate, slate	pebbles, quartz grains	1.3-6
<i>Le Théoff</i> [1977]	Variscides/Bretagne	conglomerate	pebbles	1.5-6.5
<i>Mukhopadhyay and Bhattacharya</i> [1969]	India	conglomerate	pebbles	1.87
<i>Pfiffner</i> [1977]	Alps/Helvetics	conglomerate, volcanics	pebbles, vesicles	1.3-13.5
<i>Roberts</i> [1973]	Caledonides/Eire (Donegal)	slate, grit	nodules	1.5-3.0
<i>Tan</i> [1973]	Alps/Helvetics	limestone	oöids, ammonites	1.8-2.3
<i>Wickham</i> [1973]	Appalachians	limestone	fibers	1.3-2.0

Source	Location	Rock Type	Strain Marker	Shear Strain
<i>Burg and Laurent</i> [1978]	Massif Central/France	granodiorite	planes, xenoliths	0-3.64
<i>Escher et al.</i> [1975]	Archean basement/Greenland	gneiss	dykes	2.6-9.4
<i>McLeish</i> [1971]	Caledonides/Scotland	pipe rock	pipes	0.76-42.55
O. A. Pfiffner (unpublished manuscript 1979)	Alps/Helvetics	limestone	bedding planes	35-40
<i>Ramsay and Graham</i> [1970]	Caledonides/Scotland	metagabbro	planes	0-22

Because quite small differences in strain rate lead to dramatic variations in finite strain, we are able to develop another interesting conclusion about variations in strain rate: it is well known that when layers of differing properties become folded together they take up differing amounts of finite strain.

These strain variations lead to changes in the orientation of planar deformation fabrics related to the XY plane of the strain ellipsoid and give rise to the phenomenon of cleavage refraction [*Sorby*, 1853; *Harker*, 1885; *Furtak*, 1962]. These strain variations may be quite marked; for example, principal

finite strain ratios $(1 + e_1)/(1 + e_2)$ typically seen in the limbs of many folded limestone-shale or sandstone-shale multi-layers are generally in the range competent layer 2:1 to incompetent layers 6:1. From the calculations we have made above it can be deduced that these variations in finite strains can be accomplished with differences in strain rate of less than one order of magnitude ($1.1 \times 10^{-14} \text{ s}^{-1}$; cf. $3.2 \times 10^{-14} \text{ s}^{-1}$ if these strains accumulated over a period of 1 m.y. by a simple shear mechanism).

CONCLUSIONS

1. Many rocks in orogenic zones showing features like cleavage occupy a somewhat limited deformation field, typical values for axial ratios ranging between 1 and 10.
2. In relatively young orogenic zones where we have good control of the deformation, it appears that in many cases these measurable finite strains took less than 10 m.y. and maybe as little as 100,000 years to form.
3. To produce such strains over these time spans, one arrives at (conventional) strain rates between 10^{-13} s^{-1} and 10^{-15} s^{-1} . Slower and faster strain rates have to be expected in apparently 'undeformed' rocks and in mylonite zones, respectively.
4. The observed differences in finite strains between competent and incompetent layers (e.g., quartzite and shale) can be accounted for by differences in strain rate of less than one order of magnitude (e.g., 10^{-14} s^{-1} versus $3 \times 10^{-14} \text{ s}^{-1}$).

APPENDIX A: BIBLIOGRAPHY FOR FIGURE A1

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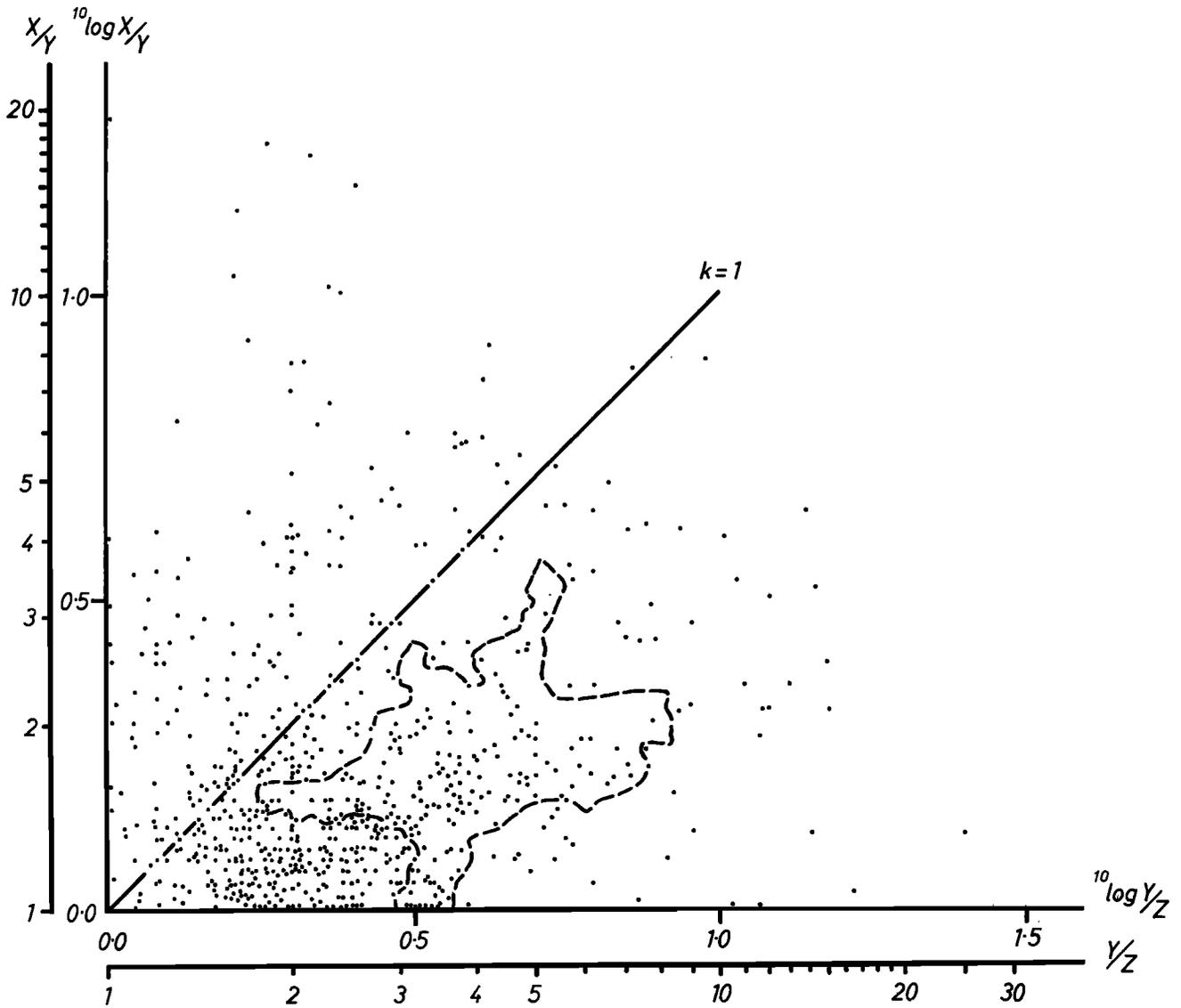


Fig. A1. Graphical representation of three-dimensional finite strain states based on measurements of naturally deformed objects. The ratio X/Y represents the measured principal plane ellipticity $(1 + e_1)/(1 + e_2)$ and Y/Z the ellipticity $(1 + e_2)/(1 + e_3)$. Data from Appendix A. The field inside the dashed line represents the strains from some 990 slates [Ramsay and Wood, 1973].

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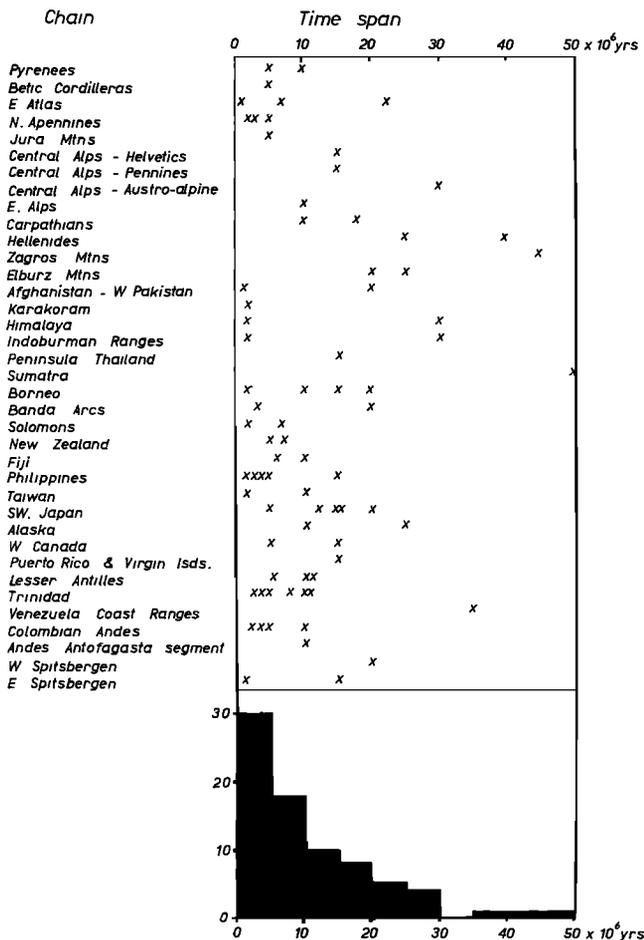


Fig. B1. Time span of deformation phases in orogenic chains. References from Appendix B.

APPENDIX B: BIBLIOGRAPHY FOR FIGURE B1

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